Package 'cNORM'

October 14, 2025

Title Continuous Norming

Version 3.5.1

Description A comprehensive toolkit for generating continuous test norms in psychometrics and biometrics, and analyzing model fit. The package offers both distribution-free modeling using Taylor polynomials and parametric modeling using the beta-binomial and the 'Sinh-Arcsinh' distribution. Originally developed for achievement tests, it is applicable to a wide range of mental, physical, or other test scores dependent on continuous or discrete explanatory variables. The package provides several advantages: It minimizes deviations from representativeness in subsamples, interpolates between discrete levels of explanatory variables, and significantly reduces the required sample size compared to conventional norming per age group. cNORM enables graphical and analytical evaluation of model fit, accommodates a wide range of scales including those with negative and descending values, and even supports conventional norming. It generates norm tables including confidence intervals. It also includes methods for addressing representativeness issues through Iterative Proportional Fitting. Based on Lenhard et al. (2016)

```
<doi:10.1177/1073191116656437>, Lenhard et al. (2019)
<doi:10.1371/journal.pone.0222279>, Lenhard and Lenhard (2021)
<doi:10.1177/0013164420928457> and Gary et al. (2023)
<doi:10.1007/s00181-023-02456-0>.
```

License AGPL-3

URL https://www.psychometrica.de/cNorm_en.html,
 https://github.com/WLenhard/cNORM

BugReports https://github.com/WLenhard/cNORM/issues

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bestModel Determine Regression Model

Description

Computes Taylor polynomial regression models by evaluating a series of models with increasing predictors. It aims to find a consistent model that effectively captures the variance in the data. It draws on the regsubsets function from the leaps package and builds up to 20 models for each number of predictors, evaluates these models regarding model consistency and selects consistent model with the highest R^2. This automatic model selection should usually be accompanied with visual inspection of the percentile plots and assessment of fit statistics. Set R^2 or number of terms manually to retrieve a more parsimonious model, if desired.

Usage

```
bestModel(
  data,
  raw = NULL,
  R2 = NULL,
  k = NULL,
  t = NULL,
  predictors = NULL,
  terms = 0,
  weights = NULL,
  force.in = NULL,
  plot = TRUE,
  extensive = TRUE,
  subsampling = TRUE
)
```

Arguments

data	Preprocessed dataset with 'raw' scores, powers, interactions, and usually an explanatory variable (like age).
raw	Name of the raw score variable (default: 'raw').
R2	Adjusted R^2 stopping criterion for model building.
k	Power constant influencing model complexity (default: 4, max: 6).
t	Age power parameter. If unset, defaults to 'k'.
predictors	List of predictors or regression formula for model selection. Overrides 'k' and can include additional variables.
terms	Desired number of terms in the model.
weights	Optional case weights. If set to FALSE, default weights (if any) are ignored.
force.in	Variables forcibly included in the regression.

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plot If TRUE (default), displays a percentile plot of the model and information about

the regression object. FALSE turns off plotting and report.

extensive If TRUE (default), screen models for consistency and - if possible, exclude in-

consistent ones

subsampling If TRUE (default), model coefficients are calculated using 10-folds and averaged

across the folds. This produces more robust estimates with a slight increase in

bias.

Details

The functions rankBySlidingWindow, rankByGroup, bestModel, computePowers and prepareData are usually not called directly, but accessed through other functions like cnorm.

Additional functions like plotSubset(model) and cnorm.cv can aid in model evaluation.

Value

The model. Further exploration can be done using plotSubset(model) and plotPercentiles(data, model).

See Also

```
plotSubset, plotPercentiles, plotPercentileSeries, checkConsistency
```

```
Other model: checkConsistency(), cnorm.cv(), derive(), modelSummary(), print.cnorm(), printSubset(), rangeCheck(), regressionFunction(), summary.cnorm()
```

Examples

```
# Example with sample data
## Not run:
# It is not recommende to use this function. Rather use 'cnorm' instead.
normData <- prepareData(elfe)
model <- bestModel(normData)
plotSubset(model)
plotPercentiles(buildCnormObject(normData, model))
# Specifying variables explicitly
preselectedModel <- bestModel(normData, predictors = c("L1", "L3", "L1A3", "A2", "A3"))
print(regressionFunction(preselectedModel))
## End(Not run)</pre>
```

betaCoefficients

Compute Parameters of a Beta Binomial Distribution

Description

This function calculates the α (a) and β (b) parameters of a beta binomial distribution, along with the mean (m), variance (var) based on the input vector 'x' and the maximum number 'n'.

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Usage

```
betaCoefficients(x, n = NULL)
```

Arguments

x A numeric vector of non-negative integers representing observed counts.

n The maximum number or the maximum possible value of 'x'. If not specified, uses max(x) instead.

Details

The beta-binomial distribution is a discrete probability distribution that models the number of successes in a fixed number of trials, where the probability of success varies from trial to trial. This variability in success probability is modeled by a beta distribution. Such a calculation is particularly relevant in scenarios where there is heterogeneity in success probabilities across trials, which is common in real-world situations, as for example the number of correct solutions in a psychometric test, where the test has a fixed number of items.

Value

A numeric vector containing the calculated parameters in the following order: alpha (a), beta (b), mean (m), standard deviation (sd), and the maximum number (n).

Examples

```
x <- c(1, 2, 3, 4, 5)
n <- 5
betaCoefficients(x, n) # or, to set n to max(x)
betaCoefficients(x)</pre>
```

buildCnormObject

Build cnorm object from data and bestModel model object

Description

Helper function to build a cnorm object from a data object and a model object from the bestModel function for compatibility reasons.

Usage

```
buildCnormObject(data, model)
```

Arguments

data	A data object from 'prepareData', or from 'rankByGroup' and 'computePower'
model	Object obtained from the bestModel function

buildFunction 7

Value

A cnorm object

Examples

```
## Not run:
   data <- prepareData(elfe)
   model <- bestModel(data, k = 4)
   model.cnorm <- buildCnormObject(data, model)
## End(Not run)</pre>
```

buildFunction

Build regression function for bestModel

Description

Build regression function for bestModel

Usage

```
buildFunction(raw, k, t, age)
```

Arguments

raw	name of the raw score variable
k	the power degree for location
t	the power degree for age
age	use age

Value

regression function

8 calcPolyInLBase2

calcPolyInL	Internal function for retrieving regression function coefficients at specific age
-------------	---

Description

The function is an inline for searching zeros in the inverse regression function. It collapses the regression function at a specific age and simplifies the coefficients.

Usage

```
calcPolyInL(raw, age, model)
```

Arguments

raw The raw value (subtracted from the intercept)

age The age

model The cNORM regression model

Value

The coefficients

calcPolyInLBase2	Internal function for retrieving regression function coefficients at spe-
	cific age

Description

The function is an inline for searching zeros in the inverse regression function. It collapses the regression function at a specific age and simplifies the coefficients. Optimized version of the prior 'calcPolyInLBase'

Usage

```
calcPolyInLBase2(raw, age, coeff, k)
```

Arguments

raw	The raw value	(subtracted	from the inte	ercept)

age The age

coeff The cNORM regression model coefficients k The cNORM regression model power parameter

Value

The coefficients

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CDC

BMI growth curves from age 2 to 25

Description

By the courtesy of the Center of Disease Control (CDC), cNORM includes human growth data for children and adolescents age 2 to 25 that can be used to model trajectories of the body mass index and to estimate percentiles for clinical definitions of under- and overweight. The data stems from the NHANES surveys in the US and was published in 2012 as public domain. The data was cleaned by removing missing values and it includes the following variables from or based on the original dataset.

Usage

CDC

Format

A data frame with 45053 rows and 7 variables:

age continuous age in years, based on the month variable

group age group; chronological age in years at the time of examination

month chronological age in month at the time of examination

sex sex of the participant, 1 = male, 2 = female

height height of the participants in cm

weight weight of the participants in kg

bmi the body mass index, computed by (weight in kg)/(height in m)^2

A data frame with 45035 rows and 7 columns

Source

https://www.cdc.gov/nchs/nhanes/

References

CDC (2012). National Health and Nutrition Examination Survey: Questionnaires, Datasets and Related Documentation. available https://www.cdc.gov/nchs/nhanes/ (date of retrieval: 25/08/2018)

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checkConsistency

Check the consistency of the norm data model

Description

While abilities increase and decline over age, within one age group, the norm scores always have to show a monotonic increase or decrease with increasing raw scores. Violations of this assumption are an indication for problems in modeling the relationship between raw and norm scores. There are several reasons, why this might occur:

- 1. Vertical extrapolation: Choosing extreme norm scores, e. g. values $-3 \le x$ and $x \ge 3$ In order to model these extreme values, a large sample dataset is necessary.
- 2. Horizontal extrapolation: Taylor polynomials converge in a certain radius. Using the model values outside the original dataset may lead to inconsistent results.
- 3. The data cannot be modeled with Taylor polynomials, or you need another power parameter (k) or R2 for the model.

Usage

```
checkConsistency(
  model,
  minAge = NULL,
  maxAge = NULL,
  minNorm = NULL,
  maxNorm = NULL,
  minRaw = NULL,
  maxRaw = NULL,
  stepAge = NULL,
  stepNorm = 1,
  warn = FALSE,
  silent = FALSE
)
```

Arguments

model	The model from the bestModel function or a cnorm object
minAge	Age to start with checking
maxAge	Upper end of the age check
minNorm	Lower end of the norm value range
maxNorm	Upper end of the norm value range
minRaw	clipping parameter for the lower bound of raw scores
maxRaw	clipping parameter for the upper bound of raw scores
stepAge	Stepping parameter for the age check. values indicate higher precision / closer checks

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stepNorm Stepping parameter for the norm table check within age with lower scores indi-

cating a higher precision. The choice depends of the norm scale used. With T

scores a stepping parameter of 1 is suitable

warn If set to TRUE, already minor violations of the model assumptions are displayed

(default = FALSE)

silent turn off messages

Details

In general, extrapolation (point 1 and 2) can carefully be done to a certain degree outside the original sample, but it should in general be handled with caution. Please note that at extreme values, the models most likely become independent and it is thus recommended to restrict the norm score range to the relevant range of abilities, e.g. +/- 2.5 SD via the minNorm and maxNorm parameter.

Value

Boolean, indicating model violations (TRUE) or no problems (FALSE)

See Also

```
Other model: bestModel(), cnorm.cv(), derive(), modelSummary(), print.cnorm(), printSubset(), rangeCheck(), regressionFunction(), summary.cnorm()
```

Examples

```
model <- cnorm(raw = elfe$raw, group = elfe$group, plot = FALSE)
modelViolations <- checkConsistency(model, minNorm = 25, maxNorm = 75)
plotDerivative(model, minNorm = 25, maxNorm = 75)</pre>
```

checkWeights

Check, if NA or values <= 0 occur and issue warning

Description

Check, if NA or values <= 0 occur and issue warning

Usage

```
checkWeights(weights)
```

Arguments

weights

Raking weights

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check_monotonicity Check Monotonicity of Predicted Values

Description

This function checks if the predicted values from a linear model are monotonically increasing or decreasing across a range of L values for multiple age points.

Usage

```
check_monotonicity(lm_model, pred_data, minRaw, maxRaw)
```

Arguments

pred_data Matrix with prediction values
minRaw lowest raw score in prediction
maxRaw highest raw score in prediction

Details

The function creates a prediction data frame using all combinations of the provided L values and age points. It then generates predictions using the provided linear model and checks if these predictions are monotonically increasing or decreasing for each age point across the range of L values.

Value

A named character vector where each element corresponds to an age point. Possible values for each element are 1 for "Monotonically increasing" -1 for "Monotonically decreasing", or 0 for "Not monotonic".

cnorm	Continuous Norming	

Description

Conducts continuous norming in one step and returns an object including ranked raw data and the continuous norming model. Please consult the function description 'of 'rankByGroup', 'rankBySlidingWindow' and 'bestModel' for specifics of the steps in the data preparation and modeling process. In addition to the raw scores, either provide

- a numeric vector for the grouping information (group)
- a numeric age vector and the width of the sliding window (age, width)

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for the ranking of the raw scores. You can adjust the grade of smoothing of the regression model by setting the k and terms parameter. In general, increasing k to more than 4 and the number of terms lead to a higher fit, while lower values lead to more smoothing. The power parameter for the age trajectory can be specified independently by 't'. If both parameters are missing, cnorm uses k = 5 and t = 3 by default.

Usage

```
cnorm(
  raw = NULL,
  group = NULL,
 age = NULL,
 width = NA,
 weights = NULL,
  scale = "T",
 method = 4,
  descend = FALSE,
  k = NULL,
  t = NULL,
  terms = 0,
 R2 = NULL
 plot = TRUE,
 extensive = TRUE,
  subsampling = TRUE
)
```

Arguments

raw	Numeric vector of raw scores
group	Numeric vector of grouping variable, e. g. grade. If no group or age variable is provided, conventional norming is applied
age	Numeric vector with chronological age, please additionally specify width of window
width	Size of the sliding window in case an age vector is used
weights	Vector or variable name in the dataset with weights for each individual case. It can be used to compensate for moderate imbalances due to insufficient norm data stratification. Weights should be numerical and positive.
scale	type of norm scale, either T (default), IQ , z or percentile (= no transformation); a double vector with the mean and standard deviation can as well, be provided f. e. $c(10, 3)$ for Wechsler scale index points
method	Ranking method in case of bindings, please provide an index, choosing from the following methods: $1 = \text{Blom } (1958)$, $2 = \text{Tukey } (1949)$, $3 = \text{Van der Warden } (1952)$, $4 = \text{Rankit } (\text{default})$, $5 = \text{Levenbach } (1953)$, $6 = \text{Filliben } (1975)$, $7 = \text{Yu}$ & Huang (2001)
descend	ranking order (default descent = FALSE): inverses the ranking order with higher raw scores getting lower norm scores; relevant for example when norming error scores, where lower scores mean higher performance

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k	The power constant. Higher values result in more detailed approximations but have the danger of over-fit (max = 6). If not set, it uses t and if both parameters are NULL, k is set to 5 .
t	The age power parameter (max = 6). If not set, it uses k and if both parameters are NULL, k is set to 3, since age trajectories are most often well captured by cubic polynomials.
terms	Selection criterion for model building. The best fitting model with this number of terms is used
R2	Adjusted R square as a stopping criterion for the model building (default $R2 = 0.99$)
plot	Default TRUE; plots the regression model and prints report
extensive	If TRUE, screen models for consistency and - if possible, exclude inconsistent ones $% \left(1\right) =\left(1\right) \left(1$
subsampling	If TRUE (default), model coefficients are calculated using 10-folds and averaged across the folds. This produces more robust estimates with a slight increase in bias.

Value

cnorm object including the ranked raw data and the regression model

References

- 1. Gary, S. & Lenhard, W. (2021). In norming we trust. Diagnostica.
- 2. Gary, S., Lenhard, W. & Lenhard, A. (2021). Modelling Norm Scores with the cNORM Package in R. Psych, 3(3), 501-521. https://doi.org/10.3390/psych3030033
- 3. Lenhard, A., Lenhard, W., Suggate, S. & Segerer, R. (2016). A continuous solution to the norming problem. Assessment, Online first, 1-14. doi:10.1177/1073191116656437
- 4. Lenhard, A., Lenhard, W., Gary, S. (2018). Continuous Norming (cNORM). The Comprehensive R Network, Package cNORM, available: https://CRAN.R-project.org/package=cNORM
- 5. Lenhard, A., Lenhard, W., Gary, S. (2019). Continuous norming of psychometric tests: A simulation study of parametric and semi-parametric approaches. PLoS ONE, 14(9), e0222279. doi:10.1371/journal.pone.0222279
- Lenhard, W., & Lenhard, A. (2020). Improvement of Norm Score Quality via Regression-Based Continuous Norming. Educational and Psychological Measurement(Online First), 1-33. https://doi.org/10.1177/0013164420928457

See Also

 $rank By Group, \, rank By Sliding Window, \, compute Powers, \, best Model \,$

Examples

```
## Not run:
# Using this function with the example dataset 'elfe'
```

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```
# Conventional norming (no modelling over age)
cnorm(raw=elfe$raw)
# Continuous norming
# You can use the 'getGroups()' function to set up grouping variable in case,
# you have a continuous age variable.
cnorm.elfe <- cnorm(raw = elfe$raw, group = elfe$group)</pre>
# return norm tables including 90% confidence intervals for a
# test with a reliability of r = .85; table are set to mean of quartal
# in grade 3 (children completed 2 years of schooling)
normTable(c(2.125, 2.375, 2.625), cnorm.elfe, CI = .90, reliability = .95)
# ... or instead of raw scores for norm scores, the other way round
rawTable(c(2.125, 2.375, 2.625), cnorm.elfe, CI = .90, reliability = .95)
# Using a continuous age variable instead of distinct groups, using a sliding
# window for percentile estimation. Please specify continuos variable for age
# and the sliding window size.
cnorm.ppvt.continuous <- cnorm(raw = ppvt$raw, age = ppvt$age, width=1)</pre>
# In case of unbalanced datasets, deviating from the census, the norm data
# can be weighted by the means of raking / post stratification. Please generate
# the weights with the computeWeights() function and pass them as the weights
# parameter. For computing the weights, please specify a data.frame with the
# population margins (further information is available in the computeWeights
# function). A demonstration based on sex and migration status in vocabulary
# development (ppvt dataset):
margins <- data.frame(variables = c("sex", "sex",</pre>
                                    "migration", "migration"),
                      levels = c(1, 2, 0, 1),
                      share = c(.52, .48, .7, .3)
weights <- computeWeights(ppvt, margins)</pre>
model <- cnorm(raw = ppvt$raw, group=ppvt$group, weights = weights)</pre>
## End(Not run)
```

cnorm.betabinomial

Fit a beta-binomial regression model for continuous norming

Description

This function fits a beta-binomial regression model where both the α and β parameters of the beta-binomial distribution are modeled as polynomial functions of the predictor variable (typically age). Setting mode to 1 fits a beta-binomial model on the basis of μ and σ , setting it to 2 (default) fits a beta-binomial model directly on the basis of α and β .

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Usage

```
cnorm.betabinomial(
  age,
  score,
  n = NULL,
  weights = NULL,
  mode = 2,
  alpha = 3,
  beta = 3,
  control = NULL,
  scale = "T",
  plot = T
)
```

Arguments

age	A numeric vector of predictor values (e.g., age).
score	A numeric vector of response values.
n	The maximum score (number of trials in the beta-binomial distribution). If NULL, max(score) is used.
weights	A numeric vector of weights for each observation. Default is NULL (equal weights).
mode	Integer specifying the mode of the model. Default is 2 (direct modelling of γ and β). If set to 1, the model is fitted on the basis of μ and σ , the predicted mean and standard deviation over age.
alpha	Integer specifying the degree of the polynomial for the alpha model. Default is 3. If mode is set to 1, this parameter is used to specify the degree of the polynomial for the μ model.
beta	Integer specifying the degree of the polynomial for the beta model. Default is 3. If mode is set to 1, this parameter is used to specify the degree of the polynomial for the σ model.
control	A list of control parameters to be passed to the 'optim' function. If NULL, default values are used, namely control = list(reltol = $1e-8$, maxit = 1000) for mode 1 and control = list(factr = $1e-8$, maxit = 1000) for mode 2.
scale	Type of norm scale, either "T" (default), "IQ", "z" or a double vector with the mean and standard deviation.
plot	Logical indicating whether to plot the model. Default is TRUE.

Details

The function standardizes the input variables, fits polynomial models for both the alpha and beta parameters, and uses maximum likelihood estimation to find the optimal parameters. The optimization is performed using the L-BFGS-B method.

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Value

A list of class "cnormBetaBinomial" or "cnormBetaBinomial2". In case of mode 2 containing:

alpha_est Estimated coefficients for the alpha model
beta_est Estimated coefficients for the beta model
se Standard errors of the estimated coefficients
alpha_degree Degree of the polynomial for the alpha model
beta_degree Degree of the polynomial for the beta model
result Full result from the optimization procedure

Examples

cnorm.cv

Cross-validation for Term Selection in cNORM

Description

Assists in determining the optimal number of terms for the regression model using repeated Monte Carlo cross-validation. It leverages an 80-20 split between training and validation data, with stratification by norm group or random sample in case of using sliding window ranking.

Usage

```
cnorm.cv(
  data,
  formula = NULL,
  repetitions = 5,
  norms = TRUE,
  min = 1,
  max = 12,
  cv = "full",
  pCutoff = NULL,
```

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```
width = NA,
raw = NULL,
group = NULL,
age = NULL,
weights = NULL
```

Arguments

data Data frame of norm sample or a cnorm object. Should have ranking, powers,

and interaction of L and A.

formula Formula from an existing regression model; min/max functions ignored. If using

a cnorm object, this is automatically fetched.

repetitions Number of repetitions for cross-validation.

norms If TRUE, computes norm score crossfit and R^2. Note: Computationally inten-

sive.

min Start with a minimum number of terms (default = 1). max Maximum terms in model, up to (k + 1) * (t + 1) - 1.

cv "full" (default) splits data into training/validation, then ranks. Otherwise, ex-

pects a pre-ranked dataset.

pCutoff Checks stratification for unbalanced data. Performs a t-test per group. Default

set to 0.2 to minimize beta error.

width If provided, ranking done via 'rankBySlidingWindow'. Otherwise, by group.

raw Name of the raw score variable.
group Name of the grouping variable.
age Name of the age variable.

weights Name of the weighting parameter.

Details

Successive models, with an increasing number of terms, are evaluated, and the RMSE for raw scores plotted. This encompasses the training, validation, and entire dataset. If 'norms' is set to TRUE (default), the function will also calculate the mean norm score reliability and crossfit measures. Note that due to the computational requirements of norm score calculations, execution can be slow, especially with numerous repetitions or terms.

When 'cv' is set to "full" (default), both test and validation datasets are ranked separately, providing comprehensive cross-validation. For a more streamlined validation process focused only on modeling, a pre-ranked dataset can be used. The output comprises RMSE for raw score models, norm score R^2, delta R^2, crossfit, and the norm score SE according to Oosterhuis, van der Ark, & Sijtsma (2016).

This function is not yet prepared for the 'extensive' search strategy, introduced in version 3.3, but instead relies on the first model per number of terms, without consistency check.

For assessing overfitting:

```
CROSSFIT = R(Training; Model)^2 / R(Validation; Model)^2
```

cNORM.GUI

A CROSSFIT > 1 suggests overfitting, < 1 suggests potential underfitting, and values around 1 are optimal, given a low raw score RMSE and high norm score validation R^2.

Suggestions for ideal model selection:

- Visual inspection of percentiles with 'plotPercentiles' or 'plotPercentileSeries'.
- Pair visual inspection with repeated cross-validation (e.g., 10 repetitions).
- Aim for low raw score RMSE and high norm score R^2, avoiding terms with significant overfit (e.g., crossfit > 1.1).

Value

Table with results per term number: RMSE for raw scores, R^2 for norm scores, and crossfit measure.

References

Oosterhuis, H. E. M., van der Ark, L. A., & Sijtsma, K. (2016). Sample Size Requirements for Traditional and Regression-Based Norms. Assessment, 23(2), 191–202. https://doi.org/10.1177/1073191115580638

See Also

```
Other model: bestModel(), checkConsistency(), derive(), modelSummary(), print.cnorm(), printSubset(), rangeCheck(), regressionFunction(), summary.cnorm()
```

Examples

```
## Not run:
# Example: Plot cross-validation RMSE by number of terms (up to 9) with three repetitions.
result <- cnorm(raw = elfe$raw, group = elfe$group)
cnorm.cv(result$data, min = 2, max = 9, repetitions = 3)
# Using a cnorm object examines the predefined formula.
cnorm.cv(result, repetitions = 1)
## End(Not run)</pre>
```

cNORM.GUI

Launcher for the graphical user interface of cNORM

Description

Launcher for the graphical user interface of cNORM

Usage

```
cNORM.GUI(launch.browser = TRUE)
```

Arguments

launch.browser Default TRUE; automatically open browser for GUI

Examples

```
## Not run:
# Launch graphical user interface
cNORM.GUI()
## End(Not run)
```

cnorm.shash

Fit a Sinh-Arcsinh (shash) Regression Model for Continuous Norming

Description

This function fits a Sinh-Arcsinh (shash; Jones & Pewsey, 2009) regression model for continuous norm score modeling, where the distribution parameters vary smoothly as polynomial functions of age or other predictors. The shash distribution is well-suited for psychometric data as it can flexibly model skewness and tail weight independently, making it ideal for handling floor effects, ceiling effects, and varying degrees of individual differences across age groups. In a simulation study (Lenhard et al, 2019), the shash model demonstrated superior performance compared to other parametric approaches from the Box Cox family of functions. In contrast to Box Cox, Sinh-Arcsinh can model distributions including zero and negativ values.

Usage

```
cnorm.shash(
   age,
   score,
   weights = NULL,
   mu_degree = 3,
   sigma_degree = 2,
   epsilon_degree = 2,
   delta_degree = 1,
   delta = 1,
   control = NULL,
   scale = "T",
   plot = TRUE
)
```

Arguments

age

A numeric vector of predictor values (typically age, but can be any continuous predictor).

score

A numeric vector of response values (raw test scores). Must be the same length as age. The value range is unresticted and it can include zeros and negative values.

weights

An optional numeric vector of weights for each observation. Useful for incorporating sampling weights. If NULL (default), all observations are weighted equally.

mu_degree

Integer specifying the degree of the polynomial for modeling the location parameter mu(age). Default is 3. Higher degrees allow more flexible modeling of how the central tendency changes with age, but may lead to overfitting with small samples. Common choices:

- 1: Linear change with age
- 2: Quadratic change (allows one inflection point)
- 3: Cubic change (allows two inflection points, suitable for most developmental curves)
- 4+: Higher-order changes (use cautiously, mainly for large samples)

sigma_degree

Integer specifying the degree of the polynomial for modeling the scale parameter sigma(age). Default is 2. This controls how the variability (spread) of scores changes with age. Lower degrees are often sufficient as variability typically changes more smoothly than location.

epsilon_degree Integer specifying the degree of the polynomial for modeling the skewness parameter epsilon(age). Default is 2. This controls how the asymmetry of the distribution changes with age.

delta_degree

Integer specifying the plynomial for modelling the tail weight parameter delte(age). Default is 1. The tail weight can be fixed as well in case of numerical instability. In that case, set 'delta_degree' to NULL and specify a value for delta instead. Recommendation: Keep delta_degree low to avoid overfitting.

delta

Fixed tail weight parameter (must be > 0). Default is 1. This parameter controls the heaviness of the distribution tails and is kept constant across all ages in this implementation. It is only used, if 'delta degree' is set to NULL. Common values:

- delta = 1: Normal-like tail behavior (baseline)
- delta > 1: Heavier tails, higher kurtosis (more extreme scores than normal distribution)
- delta < 1: Lighter tails, lower kurtosis (fewer extreme scores than normal distribution)

control

An optional list of control parameters passed to the optim function for maximum likelihood estimation. If NULL, sensible defaults are chosen automatically based on the model complexity. Common parameters to adjust:

- factr: Controls precision of optimization (default: 1e-8)
- maxit: Maximum number of iterations (default: n_parameters * 200)
- 1mm: Memory limit for L-BFGS-B (default: min(n_parameters, 20))

Increase maxit or decrease factr if optimization fails to converge.

scale

Character string or numeric vector specifying the type of norm scale for output. This affects the scaling of derived norm scores but does not influence model fitting:

- "T": T-scores (mean = 50, SD = 10) default
- "IQ": IQ-like scores (mean = 100, SD = 15)

- "z": z-scores (mean = 0, SD = 1)
- c(M, SD): Custom scale with specified mean M and standard deviation SD

plot Logical indicating whether to automatically display a diagnostic plot of the fitted model. Default is TRUE.

Details

This implementation uses the Jones & Pewsey (2009) parameterization of the Sinh-Arcsinh distribution. Parameters are estimated using maximum likelihood via the L-BFGS-B algorithm. In case, optimization fails, try reducing model complexity by reducing polynomial degrees or fixing the delta parameter.

The Sinh-Arcsinh Distribution: The shash distribution is defined by the transformation:

$$X = \mu + \sigma \cdot \sinh\left(\frac{\operatorname{arcsinh}(Y) - \epsilon}{\delta}\right)$$

where Y is a standard normal variable, $Y \sim N(0,1)$.

This transformation provides:

- mu: Location parameter (similar to mean)
- sigma: Scale parameter (similar to standard deviation)
- epsilon: Skewness parameter (epsilon = 0 for symmetry)
- delta: Tail weight parameter (delta = 1 for normal-like tails)

Model Selection: Choose polynomial degrees based on:

- Sample size (higher degrees need more data)
- Theoretical expectations about developmental trajectories
- Model comparison criteria (AIC, BIC)
- · Visual inspection of fitted curves

For most applications, mu_degree = 3, sigma_degree = 2, epsilon_degree = 2, delta_degree = 1 provides a good balance of flexibility and parsimony.

Value

An object of class "cnormShash" containing the fitted model results. This is a list with components:

mu_est	Numeric vector of estimated coefficients for the location parameter mu(age). The first coefficient is the intercept, subsequent coefficients correspond to polynomial terms.
sigma_est	Numeric vector of estimated coefficients for the scale parameter $log(sigma(age))$. Note: These are coefficients for $log(sigma)$ to ensure $sigma > 0$.
epsilon_est	Numeric vector of estimated coefficients for the skewness parameter epsilon(age).
delta	The fixed tail weight parameter value used in fitting.
delta_est	Numeric vector of estimated coefficients for the tail weight parameter delta(age) - in case, a degree has been set.
se	Numeric vector of standard errors for all estimated coefficients (if Hessian computation succeeds).

```
mu_degree, sigma_degree, epsilon_degree
```

The polynomial degrees used for each parameter.

result Complete output from the optim function, including convergence information, log-likelihood value, and other optimization details.

Note

• The function requires the input data to have sufficient variability. Very small datasets or datasets with little age spread may cause convergence problems.

- Polynomial models can exhibit edge effects at the boundaries of the age range. Predictions
 outside the observed age range should be made cautiously.
- If convergence fails, try: (1) reducing polynomial degrees, (2) adjusting the delta parameter, (3) providing custom control parameters, or (4) checking for data quality issues.
- The tail weight parameter delta is fixed across ages by default. For applications where tail behavior changes substantially with age, consider setting the delta_degree parameter to 1 or 2.

Author(s)

Wolfgang Lenhard

References

Jones, M. C., & Pewsey, A. (2009). Sinh-arcsinh distributions. *Biometrika*, 96(4), 761-780.

Lenhard, A., Lenhard, W., Gary, S. (2019). Continuous norming of psychometric tests: A simulation study of parametric and semi-parametric approaches. *PLoS ONE*, 14(9), e0222279. https://doi.org/10.1371/journal.pone.0222279

See Also

plot for plotting fitted models, predict for generating predictions, cnorm.betabinomial2 for discrete beta-binomial alternative

Examples

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```
# With sampling weights
model_weighted <- cnorm.shash(</pre>
  age = survey$age,
  score = survey$score,
  weights = survey$sample_weight
)
# Custom optimization control for difficult convergence
model_robust <- cnorm.shash(</pre>
  age = mixed$age,
  score = mixed$score,
  control = list(factr = 1e-6, maxit = 2000),
  delta = 1.5
)
# Compare model fit
compare(model, model_complex)
## End(Not run)
```

compare

Compare Two Norm Models Visually

Description

This function creates a visualization comparing two norm models by displaying their percentile curves. The first model is shown with solid lines, the second with dashed lines. If age and score vectors are provided, manifest percentiles are displayed as dots. The function works with regular cnorm models, beta-binomial models, and shash models, allowing comparison between different model types.

Usage

```
compare(
  model1,
  model2,
  percentiles = c(0.025, 0.1, 0.25, 0.5, 0.75, 0.9, 0.975),
  age = NULL,
  score = NULL,
  weights = NULL,
  title = NULL,
  subtitle = NULL
)
```

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Arguments

model1	First model object (distribution free, beta-binomial, or shash)
model2	Second model object (distribution free, beta-binomial, or shash)
percentiles	Vector with percentile scores, ranging from 0 to 1 (exclusive)
age	Optional vector with manifest age or group values
score	Optional vector with manifest raw score values

weights Optional vector with manifest weights

title Custom title for plot (optional)

subtitle Custom subtitle for plot (optional)

Value

A ggplot object showing the comparison of both models

See Also

```
Other plot: plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(), plotDensity(), plotDerivative(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(), plotRaw(), plotSubset()
```

Examples

```
## Not run:
# Compare different types of models
model1 <- cnorm(group = elfe$group, raw = elfe$raw)
model2 <- cnorm.betabinomial(elfe$group, elfe$raw)
model3 <- cnorm.shash(elfe$group, elfe$raw)

# Compare traditional cnorm with shash
compare(model1, model3, age = elfe$group, score = elfe$raw)

# Compare beta-binomial with shash
compare(model2, model3, age = elfe$group, score = elfe$raw)

## End(Not run)</pre>
```

computePowers Compute powers of the explanatory variable a as well as of the person

location l (data preparation)

26 computePowers

Description

The function computes powers of the norm variable e. g. T scores (location, L), an explanatory variable, e. g. age or grade of a data frame (age, A) and the interactions of both (L X A). The k variable indicates the degree up to which powers and interactions are build. These predictors can be used later on in the bestModel function to model the norm sample. Higher values of k allow for modeling the norm sample closer, but might lead to over-fit. In general k = 3 or k = 4 (default) is sufficient to model human performance data. For example, k = 2 results in the variables L1, L2, A1, A2, and their interactions L1A1, L2A1, L1A2 and L2A2 (but k = 2 is usually not sufficient for the modeling). Please note, that you do not need to use a normal rank transformed scale like T r IQ, but you can as well use the percentiles for the 'normValue' as well.

Usage

```
computePowers(data, k = 5, norm = NULL, age = NULL, t = 3, silent = FALSE)
```

Arguments

data	data.frame with the norm data
k	degree
norm	the variable containing the norm data in the data.frame; might be T scores, IQ scores, percentiles
age	Explanatory variable like age or grade, which was as well used for the grouping. Can be either the grouping variable itself or a finer grained variable like the exact age. Other explanatory variables can be used here instead an age variable as well, as long as the variable is at least ordered metric, e. g. language or development levels The label 'age' is used, as this is the most common field of application.
t	the age power parameter (default NULL). If not set, cNORM automatically uses k. The age power parameter can be used to specify the k to produce rectangular matrices and specify the course of scores per independently from k
silent	set to TRUE to suppress messages

Details

The functions rankBySlidingWindow, rankByGroup, bestModel, computePowers and prepareData are usually not called directly, but accessed through other functions like cnorm.

Value

data.frame with the powers and interactions of location and explanatory variable / age

See Also

bestModel

Other prepare: prepareData(), rankByGroup(), rankBySlidingWindow()

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Examples

```
# Dataset with grade levels as grouping
data.elfe <- rankByGroup(elfe)
data.elfe <- computePowers(data.elfe)

# Dataset with continuous age variable and k = 5
data.ppvt <- rankByGroup(ppvt)
data.ppvt <- computePowers(data.ppvt, age = "age", k = 5)</pre>
```

computeWeights

Weighting of cases through iterative proportional fitting (Raking)

Description

Computes and standardizes weights via raking to compensate for non-stratified samples. It is based on the implementation in the survey R package. It reduces data collection #' biases in the norm data by the means of post stratification, thus reducing the effect of unbalanced data in percentile estimation and norm data modeling.

Usage

```
computeWeights(data, population.margins, standardized = TRUE)
```

Arguments

data data.frame with norm sample data. population.margins

A data frame including three columns, specifying the variable name in the original dataset used for data stratification, the factor level of the variable and the according population share. Please ensure, the original data does not include factor levels, not present in the population margins. Additionally, summing up the shares of the different levels of a variable should result in a value near 1.0. The first column must specify the name of the stratification variable, the second the level and the third the proportion

standardized

If TRUE (default), the raking weights are scaled to weights/min(weights)

Details

This function computes standardized raking weights to overcome biases in norm samples. It generates weights, by drawing on the information of population shares (e. g. for sex, ethnic group, region ...) and subsequently reduces the influence of over-represented groups or increases underrepresented cases. The returned weights are either raw or standardized and scaled to be larger than 0.

Raking in general has a number of advantages over post stratification and it additionally allows cNORM to draw on larger datasets, since less cases have to be removed during stratification. To use this function, additionally to the data, a data frame with stratification variables has to be specified. The data frame should include a row with (a) the variable name, (b) the level of the variable and (c) the according population proportion.

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Value

a vector with the standardized weights

Examples

```
# cNORM features a dataset on vocabulary development (ppvt)
# that includes variables like sex or migration. In order
# to weight the data, we have to specify the population shares.
# According to census, the population includes 52% boys
# (factor level 1 in the ppvt dataset) and 70% / 30% of persons
# without / with a a history of migration (= 0 / 1 in the dataset).
# First we set up the popolation margins with all shares of the
# different levels:
margins <- data.frame(variables = c("sex", "sex",</pre>
                                     "migration", "migration"),
                      levels = c(1, 2, 0, 1),
                      share = c(.52, .48, .7, .3))
head(margins)
# Now we use the population margins to generate weights
# through raking
weights <- computeWeights(ppvt, margins)</pre>
# There are as many different weights as combinations of
# factor levels, thus only four in this specific case
unique(weights)
# To include the weights in the cNORM modelling, we have
# to pass them as weights. They are then used to set up
# weighted quantiles and as weights in the regession.
model <- cnorm(raw = ppvt$raw,</pre>
               group=ppvt$group,
               weights = weights)
```

derivationTable

Create a table based on first order derivative of the regression model for specific age

Description

In order to check model assumptions, a table of the first order derivative of the model coefficients is created.

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Usage

```
derivationTable(A, model, minNorm = NULL, maxNorm = NULL, step = 0.1)
```

Arguments

A the ag	ge
----------	----

model The regression model or a cnorm object
minNorm The lower bound of the norm value range
maxNorm The upper bound of the norm value range

step Stepping parameter with lower values indicating higher precision

Value

data.frame with norm scores and the predicted scores based on the derived regression function

See Also

```
plotDerivative, derive
```

```
Other predict: getNormCurve(), normTable(), predict.cnormBetaBinomial(), predict.cnormBetaBinomial2(), predict.cnormShash(), predictNorm(), predictRaw(), rawTable()
```

Examples

```
# Generate cnorm object from example data
cnorm.elfe <- cnorm(raw = elfe$raw, group = elfe$group)
# retrieve function for time point 6
d <- derivationTable(6, cnorm.elfe, step = 0.5)</pre>
```

derive

Derivative of regression model

Description

Calculates the derivative of the location / norm value from the regression model with the first derivative as the default. This is useful for finding violations of model assumptions and problematic distribution features as f. e. bottom and ceiling effects, non-progressive norm scores within an age group or in general #' intersecting percentile curves.

Usage

```
derive(model, order = 1)
```

Arguments

model The regression model or a cnorm object order The degree of the derivate, default: 1

Value

The derived coefficients

See Also

```
Other model: bestModel(), checkConsistency(), cnorm.cv(), modelSummary(), print.cnorm(), printSubset(), rangeCheck(), regressionFunction(), summary.cnorm()
```

Examples

```
m <- cnorm(raw = elfe$raw, group = elfe$group)
derivedCoefficients <- derive(m)</pre>
```

diagnostics.betabinomial

Diagnostic Information for Beta-Binomial Model

Description

This function provides diagnostic information for a fitted beta-binomial model from the cnorm.betabinomial function. It returns various metrics related to model convergence, fit, and complexity. In case, age and raw scores are provided, the function as well computes R2, rmse and bias for the norm scores based on the manifest and predicted norm scores.

Usage

```
diagnostics.betabinomial(model, age = NULL, score = NULL, weights = NULL)
```

Arguments

model An object of class "cnormBetaBinomial", typically the result of a call to cnorm.betabinomial().

age An optional vector with age values score An optional vector with raw values weights An optional vector with weights

Details

The AIC and BIC are calculated as: AIC = 2k - 2ln(L) BIC = ln(n)k - 2ln(L) where k is the number of parameters, L is the maximum likelihood, and n is the number of observations.

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Value

A list containing the following diagnostic information:

- converged: Logical indicating whether the optimization algorithm converged.
- n_evaluations: Number of function evaluations performed during optimization.
- n_gradient: Number of gradient evaluations performed during optimization.
- final_value: Final value of the objective function (negative log-likelihood).
- message: Any message returned by the optimization algorithm.
- AIC: Akaike Information Criterion.
- BIC: Bayesian Information Criterion.
- max_gradient: Maximum absolute gradient at the solution (if available).

Examples

```
## Not run:
# Fit a beta-binomial model
model <- cnorm.betabinomial(ppvt$age, ppvt$raw)</pre>
# Get diagnostic information
diag_info <- diagnostics.betabinomial(model)</pre>
# Print the diagnostic information
print(diag_info)
# Summary the diagnostic information
summary(diag_info)
# Check if the model converged
if(diag_info$converged) {
 cat("Model converged successfully.\n")
} else {
 cat("Warning: Model did not converge.\n")
}
# Compare AIC and BIC
cat("AIC:", diag_info$AIC, "\n")
cat("BIC:", diag_info$BIC, "\n")
## End(Not run)
```

32 getGroups

Description

A dataset containing the raw data of 1400 students from grade 2 to 5 in the sentence comprehension test from ELFE 1-6 (Lenhard & Schneider, 2006). In this test, students are presented lists of sentences with one gap. The student has to fill in the correct solution by selecting from a list of 5 alternatives per sentence. The alternatives include verbs, adjectives, nouns, pronouns and conjunctives. Each item stems from the same word type. The text is speeded, with a time cutoff of 180 seconds. The variables are as follows:

Usage

elfe

Format

A data frame with 1400 rows and 3 variables:

personID ID of the student

group grade level, with x.5 indicating the end of the school year and x.0 indicating the middle of the school year

raw the raw score of the student, spanning values from 0 to 28

A data frame with 1400 rows and 3 columns

Source

```
https://www.psychometrica.de/elfe2.html
```

References

Lenhard, W. & Schneider, W.(2006). Ein Leseverstaendnistest fuer Erst- bis Sechstklaesser. Goettingen/Germany: Hogrefe.

Examples

```
# prepare data, retrieve model and plot percentiles
model <- cnorm(elfe$group, elfe$raw)</pre>
```

getGroups

Determine groups and group means

Description

Helps to split the continuous explanatory variable into groups and assigns the group mean. The groups can be split either into groups of equal size (default) or equal number of observations.

Usage

```
getGroups(x, n = NULL, equidistant = FALSE)
```

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Arguments

X	The continuous variable to be split
n	The number of groups; if NULL then the function determines a number of groups with usually 100 cases or $3 \le n \le 20$.

equidistant If set to TRUE, builds equidistant interval, otherwise (default) with equal num-

ber of observations

Value

vector with group means for each observation

Examples

```
x \leftarrow rnorm(1000, m = 50, sd = 10)
m \leftarrow getGroups(x, n = 10)
```

getNormCurve

Computes the curve for a specific T value

Description

As with this continuous norming regression approach, raw scores are modeled as a function of age and norm score (location), getNormCurve is a straightforward approach to show the raw score development over age, while keeping the norm value constant. This way, e. g. academic performance or intelligence development of a specific ability is shown.

Usage

```
getNormCurve(
  norm,
  model,
  minAge = NULL,
  maxAge = NULL,
  step = 0.1,
  minRaw = NULL,
  maxRaw = NULL
)
```

Arguments

norm The specific norm score, e. g. T value

model The model from the regression modeling obtained with the cnorm function

minAge Age to start from

Age to stop at

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step Stepping parameter for the precision when retrieving of the values, lower values

indicate higher precision (default 0.1).

minRaw lower bound of the range of raw scores (default = 0)

maxRaw upper bound of raw scores

Value

data.frame of the variables raw, age and norm

See Also

Other predict: derivationTable(), normTable(), predict.cnormBetaBinomial(), predict.cnormBetaBinomial2(), predict.cnormShash(), predictNorm(), predictRaw(), rawTable()

Examples

```
# Generate cnorm object from example data
cnorm.elfe <- cnorm(raw = elfe$raw, group = elfe$group)
getNormCurve(35, cnorm.elfe)</pre>
```

getNormScoreSE Calculates the standard error (SE) or root mean square error (RMSE)

of the norm scores In case of large datasets, both results should be

almost identical

Description

Calculates the standard error (SE) or root mean square error (RMSE) of the norm scores In case of large datasets, both results should be almost identical

Usage

```
getNormScoreSE(model, type = 2)
```

Arguments

model a cnorm object

type either '1' for the standard error senso Oosterhuis et al. (2016) or '2' for the

RMSE (default)

Value

The standard error (SE) of the norm scores sensu Oosterhuis et al. (2016) or the RMSE

References

Oosterhuis, H. E. M., van der Ark, L. A., & Sijtsma, K. (2016). Sample Size Requirements for Traditional and Regression-Based Norms. Assessment, 23(2), 191–202. https://doi.org/10.1177/1073191115580638

modelSummary 35

modelSummary

Prints the results and regression function of a cnorm model

Description

Prints the results and regression function of a cnorm model

Usage

```
modelSummary(object, ...)
```

Arguments

object A regression model or cnorm object

... additional parameters

Value

A report on the regression function, weights, R2 and RMSE

See Also

```
Other model: bestModel(), checkConsistency(), cnorm.cv(), derive(), print.cnorm(), printSubset(), rangeCheck(), regressionFunction(), summary.cnorm()
```

normTable

Create a norm table based on model for specific age

Description

This function generates a norm table for a specific age based on the regression model by assigning raw scores to norm scores. Please specify the range of norm scores, you want to cover. A T value of 25 corresponds to a percentile of .6. As a consequence, specifying a range of T=25 to T=75 would cover 98.4 the population. Please be careful when extrapolating vertically (at the lower and upper end of the age specific distribution). Depending on the size of your standardization sample, extreme values with T<20 or T>80 might lead to inconsistent results. In case a confidence coefficient (CI, default .9) and the reliability is specified, confidence intervals are computed for the true score estimates, including a correction for regression to the mean (Eid & Schmidt, 2012, p. 272).

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Usage

```
normTable(
   A,
   model,
   minNorm = NULL,
   maxNorm = NULL,
   minRaw = NULL,
   maxRaw = NULL,
   step = NULL,
   step = NULL,
   ronotonuous = TRUE,
   CI = 0.9,
   reliability = NULL,
   pretty = T
)
```

Arguments

A	the age as single value or a vector of age values
model	The regression model from the cnorm function
minNorm	The lower bound of the norm score range
maxNorm	The upper bound of the norm score range
minRaw	clipping parameter for the lower bound of raw scores
maxRaw	clipping parameter for the upper bound of raw scores
step	Stepping parameter with lower values indicating higher precision
monotonuous	corrects for decreasing norm scores in case of model inconsistencies (default)
CI	confidence coefficient, ranging from 0 to 1, default .9
reliability	coefficient, ranging between 0 to 1
pretty	Format table by collapsing intervals and rounding to meaningful precision

Value

either data.frame with norm scores, predicted raw scores and percentiles in case of simple A value or a list #' of norm tables if vector of A values was provided

References

Eid, M. & Schmidt, K. (2012). Testtheorie und Testkonstruktion. Hogrefe.

See Also

```
rawTable
```

```
Other predict: derivationTable(), getNormCurve(), predict.cnormBetaBinomial(), predict.cnormBetaBinomial2(predict.cnormShash(), predictNorm(), predictRaw(), rawTable()
```

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Examples

```
# Generate cnorm object from example data
cnorm.elfe <- cnorm(raw = elfe$raw, group = elfe$group)

# create single norm table
norms <- normTable(3.5, cnorm.elfe, minNorm = 25, maxNorm = 75, step = 0.5)

# create list of norm tables
norms <- normTable(c(2.5, 3.5, 4.5), cnorm.elfe,
    minNorm = 25, maxNorm = 75,
    step = 1, minRaw = 0, maxRaw = 26
)

# conventional norming, set age to arbitrary value
model <- cnorm(raw=elfe$raw)
normTable(0, model)</pre>
```

normTable.betabinomial

Calculate Cumulative Probabilities, Density, Percentiles, and Z-Scores for Beta-Binomial Distribution

Description

This function generates a norm table for a specific ages based on the beta binomial regression model. In case a confidence coefficient (CI, default .9) and the reliability is specified, confidence intervals are computed for the true score estimates, including a correction for regression to the mean (Eid & Schmidt, 2012, p. 272).

Usage

```
normTable.betabinomial(
  model,
  ages,
  n = NULL,
  m = NULL,
  range = 3,
  CI = 0.9,
  reliability = NULL
)
```

Arguments

model The model, which was fitted using the 'optimized.model' function.

A numeric vector of age points at which to make predictions.

The number of items resp. the maximum score.

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m	An optional stop criterion in table generation. Positive integer lower than n.
range	The range of the norm scores in standard deviations. Default is 3. Thus, scores in the range of +/- 3 standard deviations are considered.
CI	confidence coefficient, ranging from 0 to 1, default .9
reliability	coefficient, ranging between 0 to 1

Value

A list of data frames with columns: x, Px, Pcum, Percentile, z, norm score and possibly confidence interval

normTable.shash Calculate Norm Tables for Sinh-Arcsinh Distribution

Description

Generates norm tables for specific ages based on a fitted SinH-ArcSinH (shash) regression model. Computes probabilities, percentiles, z-scores, and norm scores for a specified range of raw scores. Optionally includes confidence intervals when reliability is provided.

Usage

```
normTable.shash(
  model,
  ages,
  start = NULL,
  end = NULL,
  step = 1,
  CI = 0.9,
  reliability = NULL
)
```

Arguments

model	Fitted shash model object of class "cnormShash"
ages	Numeric vector of age points for norm table generation
start	Minimum raw score value for the norm table
end	Maximum raw score value for the norm table
step	Step size between consecutive raw scores (default: 1)
CI	Confidence coefficient (0-1, default: 0.9) for confidence intervals
reliability	Reliability coefficient (0-1) for true score confidence intervals

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Details

For continuous shash distributions, probability densities are computed and converted to cumulative probabilities and percentiles. When reliability is specified, confidence intervals include correction for regression to the mean.

Value

List of data frames (one per age) containing:

x Raw scores

Px Probability density values
Pcum Cumulative probabilities
Percentile Percentile ranks (0-100)
z Standardized z-scores

norm Norm scores in specified scale

lowerCI, upperCI

Confidence intervals (if reliability provided)

lowerCI_PR, upperCI_PR

CI as percentile ranks (if reliability provided)

Examples

plot.cnorm

S3 function for plotting cnorm objects

Description

S3 function for plotting cnorm objects

Usage

```
## S3 method for class 'cnorm' plot(x, y, ...)
```

Arguments

X	the cnorm object
у	the type of plot as a string, can be one of 'raw' (1), 'norm' (2), 'curves' (3),
	'percentiles' (4), 'series' (5), 'subset' (6), or 'derivative' (7), either as a string or
	the according index
	additional parameters for the specific plotting function

See Also

```
Other plot: compare(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(), plotDensity(), plotDerivative(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(), plotRaw(), plotSubset()
```

plot.cnormBetaBinomial

Plot cnormBetaBinomial Model with Data and Percentile Lines

Description

This function creates a visualization of a fitted cnormBetaBinomial model, including the original data points manifest percentiles and specified percentile lines.

Usage

```
## S3 method for class 'cnormBetaBinomial' plot(x, ...)
```

Arguments

- x A fitted model object of class "cnormBetaBinomial" or "cnormBetaBinomial2".
- . . . Additional arguments passed to the plot method.
 - age A vector the age data.
 - A vector of the score data.
 - weights An optional numeric vector of weights for each observation.
 - percentiles An optional vector with the percentiles to plot.
 - points Logical indicating whether to plot the data points. Default is TRUE.

Value

A ggplot object.

```
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial2(), plotDensity(), plotDerivative(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(), plotRaw(), plotSubset()
```

Examples

```
## Not run:
# Computing beta binomial models already displays plot
model.bb <- cnorm.betabinomial(elfe$group, elfe$raw)

# Without data points
plot(model.bb, age = elfe$group, score = elfe$raw, weights=NULL, points=FALSE)

## End(Not run)</pre>
```

plot.cnormBetaBinomial2

Plot cnormBetaBinomial Model with Data and Percentile Lines

Description

This function creates a visualization of a fitted cnormBetaBinomial model, including the original data points manifest percentiles and specified percentile lines.

Usage

```
## S3 method for class 'cnormBetaBinomial2' plot(x, ...)
```

Arguments

x A fitted model object of class "cnormBetaBinomial" or "cnormBetaBinomial2".

. . Additional arguments passed to the plot method.

- age A vector the age data.
- A vector of the score data.
- weights An optional numeric vector of weights for each observation.
- percentiles An optional vector with the percentiles to plot.
- points Logical indicating whether to plot the data points. Default is TRUE.

Value

A ggplot object.

```
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plotDensity(), plotDerivative(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(), plotRaw(), plotSubset()
```

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plot.cnormShash

Plot SinH-ArcSinH Model with Data and Percentile Lines

Description

Plot SinH-ArcSinH Model with Data and Percentile Lines

Usage

```
## S3 method for class 'cnormShash' plot(x, ...)
```

Arguments

x A fitted model object of class "cnormShash"

... Additional arguments including age, score, weights, percentiles, points

Value

A ggplot object

plotCnorm

General convenience plotting function

Description

General convenience plotting function

Usage

```
plotCnorm(x, y, ...)
```

Arguments

x a cnorm object

y the type of plot as a string, can be one of 'raw' (1), 'norm' (2), 'curves' (3), 'percentiles' (4), 'series' (5), 'subset' (6), or 'derivative' (7), either as a string or

the according index

... additional parameters for the specific plotting function

plotDensity 43

plotDensity Plot the density function per group by raw score	plotDensity	Plot the density function per group by raw score	
--	-------------	--	--

Description

This function plots density curves based on the regression model against the raw scores. It supports both traditional continuous norming models and beta-binomial models. The function allows for customization of the plot range and groups to be displayed.

Usage

```
plotDensity(
  model,
  minRaw = NULL,
  maxRaw = NULL,
  minNorm = NULL,
  maxNorm = NULL,
  group = NULL
)
```

Arguments

model	The model from the bestModel function, a cnorm object, a cnormBetaBinomial, a cnormBetaBinomial2 or cnormShash object.
minRaw	Lower bound of the raw score. If NULL, it's automatically determined based on the model type.
maxRaw	Upper bound of the raw score. If NULL, it's automatically determined based on the model type.
minNorm	Lower bound of the norm score. If NULL, it's automatically determined based on the model type.
maxNorm	Upper bound of the norm score. If NULL, it's automatically determined based on the model type.
group	Numeric vector specifying the age groups to plot. If NULL, groups are automatically selected.

Details

The function generates density curves for specified age groups, allowing for easy comparison of score distributions across different ages.

For beta-binomial models, the density is based on the probability mass function, while for traditional models, it uses a normal distribution based on the norm scores.

Value

A ggplot object representing the density functions.

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Note

Please check for inconsistent curves, especially those showing implausible shapes such as violations of biuniqueness in the cnorm models.

See Also

```
plotNormCurves, plotPercentiles
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(),
plotDerivative(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(),
plotRaw(), plotSubset()
```

Examples

```
## Not run:
# For traditional continuous norming model
result <- cnorm(raw = elfe$raw, group = elfe$group)
plotDensity(result, group = c(2, 4, 6))
# For beta-binomial model
bb_model <- cnorm.betabinomial(age = ppvt$age, score = ppvt$raw, n = 228)
plotDensity(bb_model)
## End(Not run)</pre>
```

plotDerivative

Plot first order derivative of regression model

Description

This function plots the scores obtained via the first order derivative of the regression model in dependence of the norm score.

Usage

```
plotDerivative(
  model,
  minAge = NULL,
  maxAge = NULL,
  minNorm = NULL,
  maxNorm = NULL,
  stepAge = NULL,
  stepNorm = NULL,
  order = 1
)
```

plotDerivative 45

Arguments

model	The model from the bestModel function, a cnorm object.
minAge	Minimum age to start checking. If NULL, it's automatically determined from the model.
maxAge	Maximum age for checking. If NULL, it's automatically determined from the model.
minNorm	Lower end of the norm score range. If NULL, it's automatically determined from the model.
maxNorm	Upper end of the norm score range. If NULL, it's automatically determined from the model.
stepAge	Stepping parameter for the age check, usually 1 or 0.1; lower values indicate higher precision.
stepNorm	Stepping parameter for norm scores.
order	Degree of the derivative (default = 1).

Details

The results indicate the progression of the norm scores within each age group. The regression-based modeling approach relies on the assumption of a linear progression of the norm scores. Negative scores in the first order derivative indicate a violation of this assumption. Scores near zero are typical for bottom and ceiling effects in the raw data.

The regression models usually converge within the range of the original values. In case of vertical and horizontal extrapolation, with increasing distance to the original data, the risk of assumption violation increases as well.

Value

A ggplot object representing the derivative of the regression function.

Note

This function is currently incompatible with reversed raw score scales ('descent' option).

See Also

```
checkConsistency, bestModel, derive
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(), plotDensity(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(), plotRaw(), plotSubset()
```

Examples

```
# For traditional continuous norming model
result <- cnorm(raw = elfe$raw, group = elfe$group)
plotDerivative(result, minAge=2, maxAge=5, stepAge=.2, minNorm=25, maxNorm=75, stepNorm=1)</pre>
```

plotNorm

plotNorm	Plot manifest and fitted norm scores	
----------	--------------------------------------	--

Description

This function plots the manifest norm score against the fitted norm score from the inverse regression model per group. This helps to inspect the precision of the modeling process. The scores should not deviate too far from the regression line. Applicable for Taylor polynomial models.

Usage

```
plotNorm(
  model,
  age = NULL,
  score = NULL,
  width = NULL,
  weights = NULL,
  group = FALSE,
  minNorm = NULL,
  maxNorm = NULL,
  type = 0
)
```

Arguments

model	The regression model, usually from the 'cnorm' or 'cnorm.betabinomial' function
age	In case of beta binomial model, please provide the age vector
score	In case of beta binomial model, please provide the score vector
width	In case of beta binomial model, please provide the width for the sliding window. If null, the function tries to determine a sensible setting.
weights	Vector or variable name in the dataset with weights for each individual case. If NULL, no weights are used.
group	On optional grouping variable, use empty string for no group, the variable name for Taylor polynomial models or a vector with the groups for beta binomial models
minNorm	lower bound of fitted norm scores
maxNorm	upper bound of fitted norm scores
type	Type of display: $0 = \text{plot}$ manifest against fitted values, $1 = \text{plot}$ manifest against difference values

Value

A ggplot object representing the norm scores plot.

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See Also

```
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(),
plotDensity(), plotDerivative(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(),
plotRaw(), plotSubset()
```

Examples

```
## Not run:
# Load example data set, compute model and plot results

# Taylor polynomial model
model <- cnorm(raw = elfe$raw, group = elfe$group)
plot(model, "norm")

# Beta binomial models; maximum number of items in elfe is n = 28
model.bb <- cnorm.betabinomial(elfe$group, elfe$raw, n = 28)
plotNorm(model.bb, age = elfe$group, score = elfe$raw)

## End(Not run)</pre>
```

plotNormCurves

Plot norm curves

Description

This function plots the norm curves based on the regression model. It supports both Taylor polynomial models and beta-binomial models.

Usage

```
plotNormCurves(
  model,
  normList = NULL,
  minAge = NULL,
  maxAge = NULL,
  step = 0.1,
  minRaw = NULL,
  maxRaw = NULL
)
```

Arguments

model The model from the bestModel function, a cnorm object, or a cnormBetaBinomial / cnormBetaBinomial2 object.

NormList Vector with norm scores to display. If NULL, default values are used.

minAge Age to start with checking. If NULL, it's automatically determined from the

model.

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maxAge	Upper end of the age check. If NULL, it's automatically determined from the model.
step	Stepping parameter for the age check, usually 1 or 0.1; lower scores indicate higher precision.
minRaw	Lower end of the raw score range, used for clipping implausible results. If NULL, it's automatically determined from the model.
maxRaw	Upper end of the raw score range, used for clipping implausible results. If NULL, it's automatically determined from the model.

Details

Please check the function for inconsistent curves: The different curves should not intersect. Violations of this assumption are a strong indication of violations of model assumptions in modeling the relationship between raw and norm scores.

Common reasons for inconsistencies include: 1. Vertical extrapolation: Choosing extreme norm scores (e.g., scores \leq -3 or \geq 3). 2. Horizontal extrapolation: Using the model scores outside the original dataset. 3. The data cannot be modeled with the current approach, or you need another power parameter (k) or R2 for the model.

Value

A ggplot object representing the norm curves.

See Also

```
checkConsistency, plotDerivative, plotPercentiles
```

```
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(), plotDensity(), plotDerivative(), plotNorm(), plotPercentileSeries(), plotPercentiles(), plotRaw(), plotSubset()
```

Examples

```
## Not run:
# For Taylor continuous norming model
m <- cnorm(raw = ppvt$raw, group = ppvt$group)
plotNormCurves(m, minAge=2, maxAge=5)

# For beta-binomial model
bb_model <- cnorm.betabinomial(age = ppvt$age, score = ppvt$raw, n = 228)
plotNormCurves(bb_model)
## End(Not run)</pre>
```

plotPercentiles 49

plotPercentiles Plot norm curves against actual percentiles

Description

The function plots the norm curves based on the regression model against the actual percentiles from the raw data. As in 'plotNormCurves', please check for inconsistent curves, especially intersections. Violations of this assumption are a strong indication for problems in modeling the relationship between raw and norm scores. In general, extrapolation (point 1 and 2) can carefully be done to a certain degree outside the original sample, but it should in general be handled with caution. The original percentiles are displayed as distinct points in the according color, the model based projection of percentiles are drawn as lines. Please note, that the estimation of the percentiles of the raw data is done with the quantile function with the default settings. In case, you get 'jagged' or disorganized percentile curve, try to reduce the 'k' and/or 't' parameter in modeling.

Usage

```
plotPercentiles(
  model,
  minRaw = NULL,
  maxRaw = NULL,
  minAge = NULL,
  maxAge = NULL,
  raw = NULL,
  group = NULL,
  percentiles = c(0.025, 0.1, 0.25, 0.5, 0.75, 0.9, 0.975),
  scale = NULL,
  title = NULL,
  subtitle = NULL,
  points = FALSE
)
```

Arguments

model	The Taylor polynomial regression model object from the cNORM
minRaw	Lower bound of the raw score (default = 0)
maxRaw	Upper bound of the raw score
minAge	Variable to restrict the lower bound of the plot to a specific age
maxAge	Variable to restrict the upper bound of the plot to a specific age
raw	The name of the raw variable
group	The name of the grouping variable; the distinct groups are automatically determined
percentiles	Vector with percentile scores, ranging from 0 to 1 (exclusive)

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scale	The norm scale, either 'T', 'IQ', 'z', 'percentile' or self defined with a double vector with the mean and standard deviation, f. e. c(10, 3) for Wechsler scale index points; if NULL, scale information from the data preparation is used (default)
title	custom title for plot
subtitle	custom title for plot
points	Logical indicating whether to plot the data points. Default is TRUE.

See Also

```
plotNormCurves,\,plotPercentileSeries
```

```
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(), plotDensity(), plotDerivative(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotRaw(), plotSubset()
```

Examples

```
# Load example data set, compute model and plot results
result <- cnorm(raw = elfe$raw, group = elfe$group)
plotPercentiles(result)</pre>
```

```
plotPercentileSeries Generates a series of plots with number curves by percentile for dif-
ferent models
```

Description

This functions makes use of 'plotPercentiles' to generate a series of plots with different number of predictors. It draws on the information provided by the model object to determine the bounds of the modeling (age and standard score range). It can be used as an additional model check to determine the best fitting model. Please have a look at the 'plotPercentiles' function for further information.

Usage

```
plotPercentileSeries(
   model,
   start = 1,
   end = NULL,
   group = NULL,
   percentiles = c(0.025, 0.1, 0.25, 0.5, 0.75, 0.9, 0.975),
   filename = NULL
)
```

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Arguments

model	The Taylor polynomial regression model object from the cNORM
start	Number of predictors to start with
end	Number of predictors to end with
group	The name of the grouping variable; the distinct groups are automatically determined
percentiles	Vector with percentile scores, ranging from 0 to 1 (exclusive)
filename	Prefix of the filename. If specified, the plots are saves as png files in the directory of the workspace, instead of displaying them

Value

the complete list of plots

See Also

```
plotPercentiles
```

```
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(), plotDensity(), plotDerivative(), plotNorm(), plotNormCurves(), plotPercentiles(), plotRaw(), plotSubset()
```

Examples

```
# Load example data set, compute model and plot results
result <- cnorm(raw = elfe$raw, group = elfe$group)
plotPercentileSeries(result, start=4, end=6)</pre>
```

plotRaw	Plot manifest and fitted raw scores	

Description

The function plots the raw data against the fitted scores from the regression model per group. This helps to inspect the precision of the modeling process. The scores should not deviate too far from regression line.

Usage

```
plotRaw(model, group = FALSE, raw = NULL, type = 0)
```

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Arguments

model The regression model from the 'cnorm' for	function
---	----------

group Should the fit be displayed by group?

raw Vector of the observed raw data

type Type of display: 0 = plot manifest against fitted values, 1 = plot manifest against

difference values

See Also

```
Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(), plotDensity(), plotDerivative(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(), plotSubset()
```

Examples

```
# Compute model with example dataset and plot results
result <- cnorm(raw = elfe$raw, group = elfe$group)
plotRaw(result)</pre>
```

plotSubset

Evaluate information criteria for regression model

Description

This function plots various information criteria and model fit statistics against the number of predictors or adjusted R-squared, depending on the type of plot selected. It helps in model selection by visualizing different aspects of model performance. Models, which did not pass the initial consistency check are depicted with an empty circle.

Usage

```
plotSubset(model, type = 0)
```

Arguments

model The regression model from the bestModel function or a cnorm object.

type Integer specifying the type of plot to generate:

- 0: Adjusted R2 by number of predictors (default)
- $\bullet\,$ 1: Log-transformed Mallow's Cp by adjusted R2
- 2: Bayesian Information Criterion (BIC) by adjusted R2
- 3: Root Mean Square Error (RMSE) by number of predictors
- 4: Residual Sum of Squares (RSS) by number of predictors
- 5: F-test statistic for consecutive models by number of predictors
- 6: p-value for model tests by number of predictors

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Details

The function generates different plots to help in model selection:

- For types 1 and 2 (Mallow's Cp and BIC), look for the "elbow" in the curve where the information criterion begins to drop. This often indicates a good balance between model fit and complexity. - For type 0 (Adjusted R2), higher values indicate better fit, but be cautious of overfitting with values approaching 1. - For types 3 and 4 (RMSE and RSS), lower values indicate better fit. - For type 5 (F-test), higher values suggest significant improvement with added predictors. - For type 6 (p-values), values below the significance level (typically 0.05) suggest significant improvement with added predictors.

Value

A ggplot object representing the selected information criterion plot.

Note

It's important to balance statistical measures with practical considerations and to visually inspect the model fit using functions like plotPercentiles.

See Also

```
bestModel, plotPercentiles, printSubset

Other plot: compare(), plot.cnorm(), plot.cnormBetaBinomial(), plot.cnormBetaBinomial2(), plotDensity(), plotDerivative(), plotNorm(), plotNormCurves(), plotPercentileSeries(), plotPercentiles(), plotRaw()
```

Examples

```
# Compute model with example data and plot information function
cnorm.model <- cnorm(raw = elfe$raw, group = elfe$group)
plotSubset(cnorm.model)

# Plot BIC against adjusted R-squared
plotSubset(cnorm.model, type = 2)

# Plot RMSE against number of predictors
plotSubset(cnorm.model, type = 3)</pre>
```

54 ppvt

Description

A dataset based on an unstratified sample of PPVT4 data (German adaption). The PPVT4 consists of blocks of items with 12 items each. Each item consists of 4 pictures. The test taker is given a word orally and he or she has to point out the picture matching the oral word. Bottom and ceiling blocks of items are determined according to age and performance. For instance, when a student knows less than 4 word from a block of 12 items, the testing stops. The sample is not identical with the norm sample and includes doublets of cases in order to align the sample size per age group. It is primarily intended for running the cNORM analyses with regard to modeling and stratification.

Usage

ppvt

Format

A data frame with 4542 rows and 6 variables:

age the chronological age of the child

sex the sex of the test taker, 1=male, 2=female

migration migration status of the family, 0=no, 1=yes

region factor specifying the region, the data were collected; grouped into south, north, east and west

raw the raw score of the student, spanning values from 0 to 228

group age group of the child, determined by the getGroups()-function with 12 equidistant age groups

A data frame with 5600 rows and 9 columns

Source

```
https://www.psychometrica.de/ppvt4.html
```

References

Lenhard, A., Lenhard, W., Segerer, R. & Suggate, S. (2015). Peabody Picture Vocabulary Test - Revision IV (Deutsche Adaption). Frankfurt a. M./Germany: Pearson Assessment.

Examples

```
# plot information function
plot(model.ppvt.group, "subset")

# check model consistency
checkConsistency(model.ppvt.group)

# plot percentiles
plot(model.ppvt.group, "percentiles")

## End(Not run)
```

predict.cnormBetaBinomial

Predict Norm Scores from Raw Scores

Description

This function calculates norm scores based on raw scores, age, and a fitted cnormBetaBinomial model.

Usage

```
## S3 method for class 'cnormBetaBinomial'
predict(object, ...)
```

Arguments

object

A fitted model object of class 'cnormBetaBinomial' or 'cnormBetaBinomial2'.

... Additional arguments passed to the prediction method:

- age A numeric vector of ages, same length as raw.
- score A numeric vector of raw scores.
- range The range of the norm scores in standard deviations. Default is 3. Thus, scores in the range of +/- 3 standard deviations are considered.

Details

The function first predicts the alpha and beta parameters of the beta-binomial distribution for each age using the provided model. It then calculates the cumulative probability for each raw score given these parameters. Finally, it converts these probabilities to the norm scale specified in the model.

Value

A numeric vector of norm scores.

```
Other predict: derivationTable(), getNormCurve(), normTable(), predict.cnormBetaBinomial2(), predict.cnormShash(), predictNorm(), predictRaw(), rawTable()
```

Examples

```
## Not run:
# Assuming you have a fitted model named 'bb_model':
model <- cnorm.betabinomial(ppvt$age, ppvt$raw)
raw <- c(100, 121, 97, 180)
ages <- c(7, 8, 9, 10)
norm_scores <- predict(model, ages, raw)
## End(Not run)</pre>
```

predict.cnormBetaBinomial2

Predict Norm Scores from Raw Scores

Description

This function calculates norm scores based on raw scores, age, and a fitted cnormBetaBinomial model.

Usage

```
## S3 method for class 'cnormBetaBinomial2'
predict(object, ...)
```

Arguments

object

A fitted model object of class 'cnormBetaBinomial' or 'cnormBetaBinomial2'.

.. Additional arguments passed to the prediction method:

- age A numeric vector of ages, same length as raw.
- score A numeric vector of raw scores.
- range The range of the norm scores in standard deviations. Default is 3. Thus, scores in the range of +/- 3 standard deviations are considered.

Details

The function first predicts the alpha and beta parameters of the beta-binomial distribution for each age using the provided model. It then calculates the cumulative probability for each raw score given these parameters. Finally, it converts these probabilities to the norm scale specified in the model.

Value

A numeric vector of norm scores.

```
Other predict: derivationTable(), getNormCurve(), normTable(), predict.cnormBetaBinomial(), predict.cnormShash(), predictNorm(), predictRaw(), rawTable()
```

predict.cnormShash 57

Examples

```
## Not run:
# Assuming you have a fitted model named 'bb_model':
model <- cnorm.betabinomial(ppvt$age, ppvt$raw)
raw <- c(100, 121, 97, 180)
ages <- c(7, 8, 9, 10)
norm_scores <- predict(model, ages, raw)
## End(Not run)</pre>
```

predict.cnormShash

Predict Norm Scores from Raw Scores

Description

This function calculates norm scores based on raw scores, age, and a fitted cnormShash model.

Usage

```
## S3 method for class 'cnormShash'
predict(object, ...)
```

Arguments

object

A fitted model object of class 'cnormShash'.

. . .

Additional arguments passed to the prediction method:

- age A numeric vector of ages, same length as score.
- score A numeric vector of raw scores.
- range The range of the norm scores in standard deviations. Default is 3. Thus, scores in the range of +/- 3 standard deviations are considered.

Details

The function predicts the SinH-ArcSinH (shash) distribution parameters (mu, sigma, epsilon, delta) for each age using the provided model. It then calculates the cumulative probability for each raw score given these parameters using the continuous shash distribution. Finally, it converts these probabilities to the norm scale specified in the model.

Value

A numeric vector of norm scores.

```
Other predict: derivationTable(), getNormCurve(), normTable(), predict.cnormBetaBinomial(), predict.cnormBetaBinomial2(), predictNorm(), predictRaw(), rawTable()
```

58 predictNorm

Examples

```
## Not run:
# Assuming you have a fitted model named 'shash_model':
model <- cnorm.shash(children$age, children$score)
raw_scores <- c(25.5, 30.2, 18.7, 45.3)
ages <- c(7, 8, 9, 10)
norm_scores <- predict(model, ages, raw_scores)
## End(Not run)</pre>
```

predictNorm

Retrieve norm value for raw score at a specific age

Description

This functions numerically determines the norm score for raw scores depending on the level of the explanatory variable A, e. g. norm scores for raw scores at given ages.

Usage

```
predictNorm(
  raw,
  A,
  model,
  minNorm = NULL,
  maxNorm = NULL,
  force = FALSE,
  silent = FALSE
)
```

Arguments

raw	The raw value, either single numeric or numeric vector
Α	the explanatory variable (e. g. age), either single numeric or numeric vector
model	The regression model or a cnorm object
minNorm	The lower bound of the norm score range
maxNorm	The upper bound of the norm score range
force	Try to resolve missing norm scores in case of inconsistent models
silent	set to TRUE to suppress messages

Value

The predicted norm score for a raw score, either single value or vector

predictRaw 59

See Also

Other predict: derivationTable(), getNormCurve(), normTable(), predict.cnormBetaBinomial(), predict.cnormBetaBinomial2(), predict.cnormShash(), predictRaw(), rawTable()

Examples

```
# Generate cnorm object from example data
cnorm.elfe <- cnorm(raw = elfe$raw, group = elfe$group)

# return norm value for raw value 21 for grade 2, month 9
specificNormValue <- predictNorm(raw = 21, A = 2.75, cnorm.elfe)

# predicted norm scores for the elfe dataset
# predictNorm(elfe$raw, elfe$group, cnorm.elfe)</pre>
```

predictRaw

Predict raw values

Description

Most elementary function to predict raw score based on Location (L, T score), Age (grouping variable) and the coefficients from a regression model.

Usage

```
predictRaw(norm, age, coefficients, minRaw = -Inf, maxRaw = Inf)
```

Arguments

norm The norm score, e. g. a specific T score or a vector of scores

age The age value or a vector of scores

coefficients The a cnorm object or the coefficients from the regression model

minRaw Minimum score for the results; can be used for clipping unrealistic outcomes,

usually set to the lower bound of the range of values of the test (default: 0)

maxRaw Maximum score for the results; can be used for clipping unrealistic outcomes

usually set to the upper bound of the range of values of the test

Value

the predicted raw score or a data frame of scores in case, lists of norm scores or age is used

```
Other predict: derivationTable(), getNormCurve(), normTable(), predict.cnormBetaBinomial(), predict.cnormBetaBinomial2(), predict.cnormShash(), predictNorm(), rawTable()
```

60 prepareData

Examples

```
# Prediction of single scores
model <- cnorm(raw = elfe$raw, group = elfe$group)
predictRaw(35, 3.5, model)</pre>
```

prepareData

Prepare data for modeling in one step (convenience method)

Description

This is a convenience method to either load the inbuilt sample dataset, or to provide a data frame with the variables "raw" (for the raw scores) and "group" The function ranks the data within groups, computes norm values, powers of the norm scores and interactions. Afterwards, you can use these preprocessed data to determine the best fitting model.

Usage

```
prepareData(
  data = NULL,
  group = "group",
  raw = "raw",
  age = "group",
  k = 4,
  t = NULL,
  width = NA,
  weights = NULL,
  scale = "T",
  descend = FALSE,
  silent = FALSE
)
```

Arguments

data	data.frame with a grouping variable named 'group' and a raw score variable named 'raw'.
group	grouping variable in the data, e. g. age groups, grades Setting group = FALSE deactivates modeling in dependence of age. Use this in case you do want conventional norm tables.
raw	the raw scores
age	the continuous explanatory variable; by default set to "group"
k	The power parameter, default = 4
t	the age power parameter (default NULL). If not set, cNORM automatically uses k. The age power parameter can be used to specify the k to produce rectangular matrices and specify the course of scores per independently from k

prepareData 61

width	if a width is provided, the function switches to rankBySlidingWindow to determine the observed raw scores, otherwise, ranking is done by group (default)
weights	Vector or variable name in the dataset with weights for each individual case. It can be used to compensate for moderate imbalances due to insufficient norm data stratification. Weights should be numerical and positive. Please use the 'computeWeights' function for this purpose.
scale	type of norm scale, either T (default), IQ , z or percentile (= no transformation); a double vector with the mean and standard deviation can as well, be provided f. e. $c(10, 3)$ for Wechsler scale index point
descend	ranking order (default descent = FALSE): inverses the ranking order with higher raw scores getting lower norm scores; relevant for example when norming error scores, where lower scores mean higher performance
silent	set to TRUE to suppress messages

Details

The functions rankBySlidingWindow, rankByGroup, bestModel, computePowers and prepareData are usually not called directly, but accessed through other functions like cnorm.

Value

data frame including the norm scores, powers and interactions of the norm score and grouping variable

See Also

```
Other prepare: computePowers(), rankByGroup(), rankBySlidingWindow()
```

Examples

```
# conducts ranking and computation of powers and interactions with the 'elfe' dataset
data.elfe <- prepareData(elfe)

# use vectors instead of data frame
data.elfe <- prepareData(raw=elfe$raw, group=elfe$group)

# variable names can be specified as well, here with the BMI data included in the package
## Not run:
data.bmi <- prepareData(CDC, group = "group", raw = "bmi", age = "age")

## End(Not run)

# modeling with only one group with the 'elfe' dataset as an example
# this results in conventional norming
data.elfe2 <- prepareData(data = elfe, group = FALSE)
m <- bestModel(data.elfe2)</pre>
```

62 print.cnorm

prettyPrint Format raw and norm tables The function takes a raw or norm table, condenses intervals at the bottom and top and round the numbers to meaningful interval.		
	prettyPrint	condenses intervals at the bottom and top and round the numbers to

Description

Format raw and norm tables The function takes a raw or norm table, condenses intervals at the bottom and top and round the numbers to meaningful interval.

Usage

```
prettyPrint(table)
```

Arguments

table

The table to format

Value

formatted table

print.cnorm

S3 method for printing model selection information

Description

After conducting the model fitting procedure on the data set, the best fitting model has to be chosen. The print function shows the R2 and other information on the different best fitting models with increasing number of predictors.

Usage

```
## S3 method for class 'cnorm'
print(x, ...)
```

Arguments

x The model from the 'bestModel' function or a cnorm object

... additional parameters

Value

A table with information criteria

print.cnormShash 63

See Also

```
Other model: bestModel(), checkConsistency(), cnorm.cv(), derive(), modelSummary(), printSubset(), rangeCheck(), regressionFunction(), summary.cnorm()
```

print.cnormShash

Print method for SinH-ArcSinH objects

Description

Print method for SinH-ArcSinH objects

Usage

```
## S3 method for class 'cnormShash'
print(x, ...)
```

Arguments

x A cnormShash object
... Additional arguments

printSubset

Print Model Selection Information

Description

Displays R^2 and other metrics for models with varying predictors, aiding in choosing the best-fitting model after model fitting.

Usage

```
printSubset(x, ...)
```

Arguments

x Model output from 'bestModel' or a cnorm object.

... Additional parameters.

Value

Table with model information criteria.

```
Other model: bestModel(), checkConsistency(), cnorm.cv(), derive(), modelSummary(), print.cnorm(), rangeCheck(), regressionFunction(), summary.cnorm()
```

rangeCheck

Examples

```
# Using cnorm object from sample data
result <- cnorm(raw = elfe$raw, group = elfe$group)
printSubset(result)</pre>
```

rangeCheck

Check for horizontal and vertical extrapolation

Description

Regression model only work in a specific range and extrapolation horizontally (outside the original range) or vertically (extreme norm scores) might lead to inconsistent results. The function generates a message, indicating extrapolation and the range of the original data.

Usage

```
rangeCheck(
  object,
  minAge = NULL,
  maxAge = NULL,
  minNorm = NULL,
  maxNorm = NULL,
  digits = 3,
  ...
)
```

Arguments

object	The regression model or a cnorm object
minAge	The lower age bound
maxAge	The upper age bound
minNorm	The lower norm value bound
maxNorm	The upper norm value bound
digits	The precision for rounding the norm and age data
	additional parameters

Value

the report

```
Other model: bestModel(), checkConsistency(), cnorm.cv(), derive(), modelSummary(), print.cnorm(), printSubset(), regressionFunction(), summary.cnorm()
```

rankByGroup 65

Examples

```
m <- cnorm(raw = elfe$raw, group = elfe$group)
rangeCheck(m)</pre>
```

rankByGroup

Determine the norm scores of the participants in each subsample

Description

This is the initial step, usually done in all kinds of test norming projects, after the scale is constructed and the norm sample is established. First, the data is grouped according to a grouping variable and afterwards, the percentile for each raw value is retrieved. The percentile can be used for the modeling procedure, but in case, the samples to not deviate too much from normality, T, IQ or z scores can be computed via a normal rank procedure based on the inverse cumulative normal distribution. In case of bindings, we use the medium rank and there are different methods for estimating the percentiles (default RankIt).

Usage

```
rankByGroup(
  data = NULL,
  group = "group",
  raw = "raw",
  weights = NULL,
  method = 4,
  scale = "T",
  descend = FALSE,
  descriptives = TRUE,
  na.rm = TRUE,
  silent = FALSE
)
```

Arguments

data	data.frame with norm sample data. If no data.frame is provided, the raw score and group vectors are directly used
group	name of the grouping variable (default 'group') or numeric vector, e. g. grade, setting group to FALSE cancels grouping (data is treated as one group)
raw	name of the raw value variable (default 'raw') or numeric vector
weights	Vector or variable name in the dataset with weights for each individual case. It can be used to compensate for moderate imbalances due to insufficient norm data stratification. Weights should be numerical and positive. Please use the 'computeWeights' function for this purpose.
method	Ranking method in case of bindings, please provide an index, choosing from the following methods: 1 = Blom (1958), 2 = Tukey (1949), 3 = Van der Warden (1952), 4 = Rankit (default), 5 = Levenbach (1953), 6 = Filliben (1975), 7 = Yu

& Huang (2001)

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scale	type of norm scale, either T (default), IQ, z or percentile (= no transformation); a double vector with the mean and standard deviation can as well, be provided f. e. c(10, 3) for Wechsler scale index points
descend	ranking order (default descent = FALSE): inverses the ranking order with higher raw scores getting lower norm scores; relevant for example when norming error scores, where lower scores mean higher performance
descriptives	If set to TRUE (default), information in n, mean, median and standard deviation per group is added to each observation
na.rm	remove values, where the percentiles could not be estimated, most likely happens in the context of weighting
silent	set to TRUE to suppress messages

Value

the dataset with the percentiles and norm scales per group

Remarks on using covariates

So far the inclusion of a binary covariate is experimental and far from optimized. The according variable name has to be specified in the ranking procedure and the modeling includes this in the further process. At the moment, during ranking the data are split into the according cells group x covariate, which leads to small sample sizes. Please take care to have enough cases in each combination. Additionally, covariates can lead to unstable modeling solutions. The question, if it is really reasonable to include covariates when norming a test is a decision beyond the pure data modeling. Please use with care or alternatively split the dataset into the two groups beforehand and model them separately.

The functions rankBySlidingWindow, rankByGroup, bestModel, computePowers and prepareData are usually not called directly, but accessed through other functions like cnorm.

See Also

```
rankBySlidingWindow, computePowers, computeWeights, weighted.rank
Other prepare: computePowers(), prepareData(), rankBySlidingWindow()
```

Examples

```
# Transformation with default parameters: RankIt and converting to T scores
data.elfe <- rankByGroup(elfe, group = "group") # using a data frame with vector names
data.elfe2 <- rankByGroup(raw=elfe$raw, group=elfe$group) # use vectors for raw score and group
# Transformation into Wechsler scores with Yu & Huang (2001) ranking procedure
data.elfe <- rankByGroup(raw = elfe$raw, group = elfe$group, method = 7, scale = c(10, 3))
# cNORM can as well be used for conventional norming, in case no group is given
d <- rankByGroup(raw = elfe$raw)
d <- computePowers(d)
m <- bestModel(d)
rawTable(0, m) # please use an arbitrary value for age when generating the tables</pre>
```

rankBySlidingWindow

Determine the norm scores of the participants by sliding window

Description

The function retrieves all individuals in the predefined age range (x +/- width/2) around each case and ranks that individual based on this individually drawn sample. This function can be directly used with a continuous age variable in order to avoid grouping. When collecting data on the basis of a continuous age variable, cases located far from the mean age of the group receive distorted percentiles when building discrete groups and generating percentiles with the traditional approach. The distortion increases with distance from the group mean and this effect can be avoided by the sliding window. Nonetheless, please ensure, that the optional grouping variable in fact represents the correct mean age of the respective age groups, as this variable is later on used for displaying the manifest data in the percentile plots.

Usage

```
rankBySlidingWindow(
  data = NULL,
  age = "age",
  raw = "raw",
  weights = NULL,
  width,
  method = 4,
  scale = "T",
  descend = FALSE,
  descriptives = TRUE,
  nGroup = 0,
  group = NA,
  na.rm = TRUE,
  silent = FALSE
)
```

Arguments

data	data.frame with norm sample data
age	the continuous age variable. Setting 'age' to FALSE inhibits computation of powers of age and the interactions
raw	name of the raw value variable (default 'raw')
weights	Vector or variable name in the dataset with weights for each individual case. It can be used to compensate for moderate imbalances due to insufficient norm data stratification. Weights should be numerical and positive. It can be resource intense when applied to the sliding window. Please use the 'computeWeights' function for this purpose.
width	the width of the sliding window

method	Ranking method in case of bindings, please provide an index, choosing from the following methods: 1 = Blom (1958), 2 = Tukey (1949), 3 = Van der Warden (1952), 4 = Rankit (default), 5 = Levenbach (1953), 6 = Filliben (1975), 7 = Yu & Huang (2001)
scale	type of norm scale, either T (default), IQ, z or percentile (= no transformation); a double vector with the mean and standard deviation can as well, be provided f. e. $c(10,3)$ for Wechsler scale index points
descend	ranking order (default descent = FALSE): inverses the ranking order with higher raw scores getting lower norm scores; relevant for example when norming error scores, where lower scores mean higher performance
descriptives	If set to TRUE (default), information in n, mean, median and standard deviation per group is added to each observation
nGroup	If set to a positive value, a grouping variable is created with the desired number of equi distant groups, named by the group mean age of each group. It creates the column 'group' in the data.frame and in case, there is already one with that name, overwrites it.
group	Optional parameter for providing the name of the grouping variable (if present; overwritten if ngroups is used)
na.rm	remove values, where the percentiles could not be estimated, most likely happens in the context of weighting
silent	set to TRUE to suppress messages

Details

In case of bindings, the function uses the medium rank and applies the algorithms already described in the rankByGroup function. At the upper and lower end of the data sample, the sliding stops and the sample is drawn from the interval min + width and max - width, respectively.

Value

the dataset with the individual percentiles and norm scores

Remarks on using covariates

So far the inclusion of a binary covariate is experimental and far from optimized. The according variable name has to be specified in the ranking procedure and the modeling includes this in the further process. At the moment, during ranking the data are split into the according degrees of the covariate and the ranking is done separately. This may lead to small sample sizes. Please take care to have enough cases in each combination. Additionally, covariates can lead to unstable modeling solutions. The question, if it is really reasonable to include covariates when norming a test is a decision beyond the pure data modeling. Please use with care or alternatively split the dataset into the two groups beforehand and model them separately.

The functions rankBySlidingWindow, rankByGroup, bestModel, computePowers and prepareData are usually not called directly, but accessed through other functions like cnorm.

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See Also

```
rankByGroup, computePowers, computeWeights, weighted.rank, weighted.quantile Other prepare: computePowers(), prepareData(), rankByGroup()
```

Examples

```
## Not run:
# Transformation using a sliding window
data.elfe2 <- rankBySlidingWindow(relfe, raw = "raw", age = "group", width = 0.5)
# Comparing this to the traditional approach should give us exactly the same
# values, since the sample dataset only has a grouping variable for age
data.elfe <- rankByGroup(elfe, group = "group")
mean(data.elfe$normValue - data.elfe2$normValue)
## End(Not run)</pre>
```

rawTable

Create a table with norm scores assigned to raw scores for a specific age based on the regression model

Description

This function is comparable to 'normTable', despite it reverses the assignment: A table with raw scores and the according norm scores for a specific age based on the regression model is generated. This way, the inverse function of the regression model is solved numerically with brute force. Please specify the range of raw values, you want to cover. With higher precision and smaller stepping, this function becomes computational intensive. In case a confidence coefficient (CI, default .9) and the reliability is specified, confidence intervals are computed for the true score estimates, including a correction for regression to the mean (Eid & Schmidt, 2012, p. 272).

Usage

```
rawTable(
   A,
   model,
   minRaw = NULL,
   maxRaw = NULL,
   minNorm = NULL,
   maxNorm = NULL,
   step = 1,
   monotonuous = TRUE,
   CI = 0.9,
   reliability = NULL,
   pretty = TRUE
)
```

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Arguments

Α	the age	either	single	value or	vector	with age	values
/ · ·	me age,	CITICI	5111510	varue or	VCCtOI	with age	varaco

model The regression model or a cnorm object
minRaw The lower bound of the raw score range
maxRaw The upper bound of the raw score range

minNorm Clipping parameter for the lower bound of norm scores (default 25)

maxNorm Clipping parameter for the upper bound of norm scores (default 25)

step Stepping parameter for the raw scores (default 1)

monotonuous corrects for decreasing norm scores in case of model inconsistencies (default)

CI confidence coefficient, ranging from 0 to 1, default .9

reliability coefficient, ranging between 0 to 1

pretty Format table by collapsing intervals and rounding to meaningful precision

Value

either data.frame with raw scores and the predicted norm scores in case of simple A value or a list of norm tables if vector of A values was provided

References

Eid, M. & Schmidt, K. (2012). Testtheorie und Testkonstruktion. Hogrefe.

See Also

normTable

```
Other predict: derivationTable(), getNormCurve(), normTable(), predict.cnormBetaBinomial(), predict.cnormBetaBinomial2(), predict.cnormShash(), predictNorm(), predictRaw()
```

Examples

```
# Generate cnorm object from example data
cnorm.elfe <- cnorm(raw = elfe$raw, group = elfe$group)
# generate a norm table for the raw value range from 0 to 28 for the time point month 7 of grade 3
table <- rawTable(3 + 7 / 12, cnorm.elfe, minRaw = 0, maxRaw = 28)
# generate several raw tables
table <- rawTable(c(2.5, 3.5, 4.5), cnorm.elfe, minRaw = 0, maxRaw = 28)
# additionally compute confidence intervals
table <- rawTable(c(2.5, 3.5, 4.5), cnorm.elfe, minRaw = 0, maxRaw = 28, CI = .9, reliability = .94)
# conventional norming, set age to arbitrary value
model <- cnorm(raw=elfe$raw)
rawTable(0, model)</pre>
```

regressionFunction 71

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Regression function

Description

The method builds the regression function for the regression model, including the beta weights. It can be used to predict the raw scores based on age and location.

Usage

```
regressionFunction(model, raw = NULL, digits = NULL)
```

Arguments

model The regression model from the bestModel function or a cnorm object

raw The name of the raw value variable (default 'raw')
digits Number of digits for formatting the coefficients

Value

The regression formula as a string

See Also

```
Other model: bestModel(), checkConsistency(), cnorm.cv(), derive(), modelSummary(), print.cnorm(), printSubset(), rangeCheck(), summary.cnorm()
```

Examples

```
result <- cnorm(raw = elfe$raw, group = elfe$group)
regressionFunction(result)</pre>
```

shash

Sinh-Arcsinh (shash) Distribution

Description

Density, distribution function, quantile function and random generation for the Sinh-Arcsinh distribution with location parameter mu, scale parameter sigma, skewness parameter epsilon, and tail weight parameter delta.

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Usage

```
dshash(x, mu = 0, sigma = 1, epsilon = 0, delta = 1, log = FALSE)
pshash(
  q,
 mu = 0,
 sigma = 1,
  epsilon = 0,
  delta = 1,
 lower.tail = TRUE,
  log.p = FALSE
)
qshash(
 p,
 mu = 0,
  sigma = 1,
  epsilon = 0,
 delta = 1,
  lower.tail = TRUE,
  log.p = FALSE
)
rshash(n, mu = 0, sigma = 1, epsilon = 0, delta = 1)
```

Arguments

x, q	vector of quantiles
mu	location parameter (default: 0)
sigma	scale parameter (must be > 0 , default: 1)
epsilon	skewness parameter (default: 0, symmetric distribution)
delta	tail weight parameter (must be > 0, default: 1 for normal-like tails)
log, log.p	logical; if TRUE, probabilities p are given as log(p)
lower.tail	logical; if TRUE (default), probabilities are $P[X \le x]$ otherwise, $P[X > x]$
p	vector of probabilities
n	number of observations. If $length(n) > 1$, the length is taken to be the number required.

Details

The Sinh-Arcsinh distribution (Jones & Pewsey, 2009) is defined by the transformation:

$$X = \mu + \sigma \cdot \sinh\left(\frac{\mathrm{asinh}(Z) - \epsilon}{\delta}\right)$$

where $Z \sim N(0,1)$ is a standard normal variable.

The four parameters control:

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- mu: Location (similar to mean)
- sigma: Scale (similar to standard deviation)
- epsilon: Skewness (epsilon = 0 gives symmetry)
- delta: Tail weight (delta = 1 gives normal-like tails, delta > 1 gives heavier tails, delta <
 1 gives lighter tails)

Value

dshash gives the density, pshash gives the distribution function, qshash gives the quantile function, and rshash generates random deviates.

The length of the result is determined by n for rshash, and is the maximum of the lengths of the numerical arguments for the other functions.

References

```
Jones, M. C., & Pewsey, A. (2009). Sinh-arcsinh distributions. Biometrika, 96(4), 761-780. doi:10.1093/biomet/asp053
```

See Also

Normal for the normal distribution.

Examples

```
# Generate random samples
x <- rshash(1000, mu = 0, sigma = 1, epsilon = 0.5, delta = 1.2)
# Density
plot(density(x))
curve(dshash(x, mu = 0, sigma = 1, epsilon = 0.5, delta = 1.2),
      add = TRUE, col = "red")
# Cumulative probability
pshash(0, mu = 0, sigma = 1, epsilon = 0.5, delta = 1.2)
qshash(c(0.025, 0.5, 0.975), mu = 0, sigma = 1, epsilon = 0.5, delta = 1.2)
# Compare with normal distribution (epsilon = 0, delta = 1)
par(mfrow = c(2, 2))
x_{vals} \leftarrow seq(-4, 4, length.out = 200)
plot(x_vals, dshash(x_vals), type = "l", main = "Symmetric (like normal)")
plot(x_vals, dshash(x_vals, epsilon = 1), type = "l", main = "Right skewed")
plot(x_vals, dshash(x_vals, delta = 2), type = "1", main = "Heavy tails")
plot(x_vals, dshash(x_vals, delta = 0.5), type = "1", main = "Light tails")
```

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simMean

Simulate mean per age

Description

Simulate mean per age

Usage

```
simMean(age)
```

Arguments

age

the age variable

Value

return predicted means

Examples

```
## Not run:
x <- simMean(a)
## End(Not run)</pre>
```

 $\verb|simSD|$

Simulate sd per age

Description

Simulate sd per age

Usage

```
simSD(age)
```

Arguments

age

the age variable

Value

return predicted sd

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Examples

```
## Not run:
x <- simSD(a)
## End(Not run)</pre>
```

simulateRasch

Simulate raw test scores based on Rasch model

Description

For testing purposes only: The function simulates raw test scores based on a virtual Rasch based test with n results per age group, an evenly distributed age variable, items.n test items with a simulated difficulty and standard deviation. The development trajectories over age group are modeled by a curve linear function of age, with at first fast progression, which slows down over age, and a slightly increasing standard deviation in order to model a scissor effects. The item difficulties can be accessed via \$theta and the raw data via \$data of the returned object.

Usage

```
simulateRasch(
  data = NULL,
  n = 100,
  minAge = 1,
  maxAge = 7,
  items.n = 21,
  items.m = 0,
  items.sd = 1,
  Theta = "random",
  width = 1
)
```

Arguments

data	data.frame from previous simulations for recomputation (overrides n, minAge, maxAge)
n	The sample size per age group
minAge	The minimum age (default 1)
maxAge	The maximum age (default 7)
items.n	The number of items of the test
items.m	The mean difficulty of the items
items.sd	The standard deviation of the item difficulty
Theta	irt scales difficulty parameters, either "random" for drawing a random sample, "even" for evenly distributed or a set of predefined values, which then overrides the item.n parameters

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width

The width of the window size for the continuous age per group; +- 1/2 width around group center on items.m and item.sd; if set to FALSE, the distribution is not drawn randomly but normally nonetheless

Value

a list containing the simulated data and thetas

data the data.frame with only age, group and rawsim the complete simulated data with item level resultstheta the difficulty of the items

Examples

standardize

Standardize a numeric vector

Description

This function standardizes a numeric vector by subtracting the mean and dividing by the standard deviation. The resulting vector will have a mean of 0 and a standard deviation of 1.

Usage

```
standardize(x)
```

Arguments

Χ

A numeric vector to be standardized.

Value

A numeric vector of the same length as x, containing the standardized values.

Examples

```
data <- c(1, 2, 3, 4, 5)
standardized_data <- standardize(data)
print(standardized_data)</pre>
```

standardizeRakingWeights

Function for standardizing raking weights Raking weights get divided by the smallest weight. Thereby, all weights become larger or equal to 1 without changing the ratio of the weights to each other.

Description

Function for standardizing raking weights Raking weights get divided by the smallest weight. Thereby, all weights become larger or equal to 1 without changing the ratio of the weights to each other.

Usage

```
standardizeRakingWeights(weights)
```

Arguments

weights

Raking weights computed by computeWeights()

Value

the standardized weights

subsample_lm

K-fold Resampled Coefficient Estimation for Linear Regression

Description

Performs k-fold resampling to estimate averaged coefficients for linear regression. The coefficients are averaged across k different subsets of the data to provide more stable estimates. For small samples (n < 100), returns a standard linear model instead.

Usage

```
subsample_lm(text, data, weights, k = 10)
```

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Arguments

data A data frame containing the variables in the model

weights Optional numeric vector of weights. If NULL, unweighted regression is per-

formed

k Integer specifying the number of resampling folds (default = 10)

Details

The function splits the data into k subsets, fits a linear model on k-1 subsets, and stores the coefficients. This process is repeated k times, and the final coefficients are averaged across all iterations to provide more stable estimates.

Value

An object of class 'lm' with averaged coefficients from k-fold resampling. For small samples, returns a standard lm object.

summary.cnorm	S3 method for printing the results and regression function of a cnorm
	model

Description

S3 method for printing the results and regression function of a cnorm model

Usage

```
## S3 method for class 'cnorm'
summary(object, ...)
```

Arguments

object A regression model or cnorm object additional parameters

Value

A report on the regression function, weights, R2 and RMSE

See Also

```
Other model: bestModel(), checkConsistency(), cnorm.cv(), derive(), modelSummary(), print.cnorm(), printSubset(), rangeCheck(), regressionFunction()
```

summary.cnormBetaBinomial

Summarize a Beta-Binomial Continuous Norming Model

Description

This function provides a summary of a fitted beta-binomial continuous norming model, including model fit statistics, convergence information, and parameter estimates.

Usage

```
## S3 method for class 'cnormBetaBinomial'
summary(object, ...)
```

Arguments

object

An object of class "cnormBetaBinomial" or "cnormBetaBinomial2", typically the result of a call to cnorm.betabinomial.

. . .

Additional arguments passed to the summary method:

- age An optional numeric vector of age values corresponding to the raw scores. If provided along with raw, additional fit statistics (R-squared, RMSE, bias) will be calculated.
- score An optional numeric vector of raw scores. Must be provided if age is given.
- weights An optional numeric vector of weights for each observation.

Details

The summary includes:

- Basic model information (type, number of observations, number of parameters)
- Model fit statistics (log-likelihood, AIC, BIC)
- R-squared, RMSE, and bias (if age and raw scores are provided) in comparison to manifest norm scores
- Convergence information
- Parameter estimates with standard errors, z-values, and p-values

Value

Invisibly returns a list containing detailed diagnostic information about the model. The function primarily produces printed output summarizing the model.

See Also

cnorm.betabinomial, diagnostics.betabinomial

Examples

```
## Not run:
model <- cnorm.betabinomial(ppvt$age, ppvt$raw, n = 228)
summary(model)

# Including R-squared, RMSE, and bias in the summary:
summary(model, age = ppvt$age, score = ppvt$raw)

## End(Not run)</pre>
```

summary.cnormBetaBinomial2

Summarize a Beta-Binomial Continuous Norming Model

Description

This function provides a summary of a fitted beta-binomial continuous norming model, including model fit statistics, convergence information, and parameter estimates.

Usage

```
## S3 method for class 'cnormBetaBinomial2'
summary(object, ...)
```

Arguments

object

An object of class "cnormBetaBinomial" or "cnormBetaBinomial2", typically the result of a call to cnorm.betabinomial.

. . .

Additional arguments passed to the summary method:

- age An optional numeric vector of age values corresponding to the raw scores. If provided along with raw, additional fit statistics (R-squared, RMSE, bias) will be calculated.
- score An optional numeric vector of raw scores. Must be provided if age is given.
- weights An optional numeric vector of weights for each observation.

Details

The summary includes:

- Basic model information (type, number of observations, number of parameters)
- Model fit statistics (log-likelihood, AIC, BIC)
- R-squared, RMSE, and bias (if age and raw scores are provided) in comparison to manifest norm scores
- Convergence information
- · Parameter estimates with standard errors, z-values, and p-values

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Value

Invisibly returns a list containing detailed diagnostic information about the model. The function primarily produces printed output summarizing the model.

See Also

```
cnorm.betabinomial, diagnostics.betabinomial
```

Examples

```
## Not run:
model <- cnorm.betabinomial(ppvt$age, ppvt$raw, n = 228)
summary(model)

# Including R-squared, RMSE, and bias in the summary:
summary(model, age = ppvt$age, raw = ppvt$raw)

## End(Not run)</pre>
```

summary.cnormShash

Summarize a SinH-ArcSinH Continuous Norming Model

Description

This function provides a summary of a fitted SinH-ArcSinH (shash) continuous norming model, including model fit statistics, convergence information, and parameter estimates.

Usage

```
## S3 method for class 'cnormShash'
summary(object, ...)
```

Arguments

object

An object of class "cnormShash", typically the result of a call to cnorm. shash.

. .

Additional arguments passed to the summary method:

- age An optional numeric vector of age values corresponding to the raw scores. If provided along with score, additional fit statistics (R-squared, RMSE, bias) will be calculated.
- score An optional numeric vector of raw scores. Must be provided if age is given.
- weights An optional numeric vector of weights for each observation.

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Details

The summary includes:

- Basic model information (polynomial degrees, delta parameter, number of observations)
- Model fit statistics (log-likelihood, AIC, BIC)
- R-squared, RMSE, and bias (if age and raw scores are provided)
- Convergence information
- Parameter estimates with standard errors, z-values, and p-values

Value

Invisibly returns a list containing detailed diagnostic information about the model. The function primarily produces printed output summarizing the model.

See Also

```
cnorm.shash, diagnostics.shash
```

Examples

```
## Not run:
model <- cnorm.shash(children$age, children$score)
summary(model)

# Including R-squared, RMSE, and bias in the summary:
summary(model, age = children$age, score = children$score)
## End(Not run)</pre>
```

taylorSwift

Swiftly compute Taylor regression models for distribution free continuous norming

Description

Conducts distribution free continuous norming and aims to find a fitting model. Raw data are modelled as a Taylor polynomial of powers of age and location and their interactions. In addition to the raw scores, either provide a numeric vector for the grouping information (group) for the ranking of the raw scores. You can adjust the grade of smoothing of the regression model by setting the k, t and terms parameter. In general, increasing k and t leads to a higher fit, while lower values lead to more smoothing. If both parameters are missing, taylorSwift uses k = 5 and t = 3 by default.

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Usage

```
taylorSwift(
 raw = NULL,
 group = NULL,
 age = NULL,
 width = NA,
 weights = NULL,
 scale = "T",
 method = 4,
 descend = FALSE,
 k = NULL
  t = NULL,
  terms = 0,
 R2 = NULL,
 plot = TRUE,
 extensive = TRUE,
 subsampling = TRUE
)
```

Arguments

raw	Numeric vector of raw scores
group	Numeric vector of grouping variable, e. g. grade. If no group or age variable is provided, conventional norming is applied
age	Numeric vector with chronological age, please additionally specify width of window
width	Size of the sliding window in case an age vector is used
weights	Vector or variable name in the dataset with weights for each individual case. It can be used to compensate for moderate imbalances due to insufficient norm data stratification. Weights should be numerical and positive.
scale	type of norm scale, either T (default), IQ, z or percentile (= no transformation); a double vector with the mean and standard deviation can as well, be provided f. e. $c(10,3)$ for Wechsler scale index points
method	Ranking method in case of bindings, please provide an index, choosing from the following methods: 1 = Blom (1958), 2 = Tukey (1949), 3 = Van der Warden (1952), 4 = Rankit (default), 5 = Levenbach (1953), 6 = Filliben (1975), 7 = Yu & Huang (2001)
descend	ranking order (default descent = FALSE): inverses the ranking order with higher raw scores getting lower norm scores; relevant for example when norming error scores, where lower scores mean higher performance
k	The power constant. Higher values result in more detailed approximations but have the danger of over-fit (max = 6). If not set, it uses t and if both parameters are NULL, k is set to 5 .
t	The age power parameter ($\max = 6$). If not set, it uses k and if both parameters are NULL, k is set to 3, since age trajectories are most often well captured by cubic polynomials.

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terms	Selection criterion for model building. The best fitting model with this number of terms is used
R2	Adjusted R square as a stopping criterion for the model building (default $R2 = 0.99$)
plot	Default TRUE; plots the regression model and prints report
extensive	If TRUE, screen models for consistency and - if possible, exclude inconsistent ones
subsampling	If TRUE (default), model coefficients are calculated using 10-folds and averaged across the folds. This produces more robust estimates with a slight increase in bias.

Value

cnorm object including the ranked raw data and the regression model

References

- 1. Gary, S. & Lenhard, W. (2021). In norming we trust. Diagnostica.
- 2. Gary, S., Lenhard, W. & Lenhard, A. (2021). Modelling Norm Scores with the cNORM Package in R. Psych, 3(3), 501-521. https://doi.org/10.3390/psych3030033
- 3. Lenhard, A., Lenhard, W., Suggate, S. & Segerer, R. (2016). A continuous solution to the norming problem. Assessment, Online first, 1-14. doi:10.1177/1073191116656437
- 4. Lenhard, A., Lenhard, W., Gary, S. (2018). Continuous Norming (cNORM). The Comprehensive R Network, Package cNORM, available: https://CRAN.R-project.org/package=cNORM
- 5. Lenhard, A., Lenhard, W., Gary, S. (2019). Continuous norming of psychometric tests: A simulation study of parametric and semi-parametric approaches. PLoS ONE, 14(9), e0222279. doi:10.1371/journal.pone.0222279
- Lenhard, W., & Lenhard, A. (2020). Improvement of Norm Score Quality via Regression-Based Continuous Norming. Educational and Psychological Measurement(Online First), 1-33. https://doi.org/10.1177/0013164420928457

See Also

rankByGroup, rankBySlidingWindow, computePowers, bestModel

Examples

```
## Not run:
# Using this function with the example dataset 'ppvt'
# You can use the 'getGroups()' function to set up grouping variable in case,
# you have a continuous age variable.
model <- taylorSwift(raw = ppvt$raw, group = ppvt$group)

# return norm tables including 90% confidence intervals for a
# test with a reliability of r = .85; table are set to mean of quartal
# in grade 3 (children completed 2 years of schooling)
normTable(c(5, 15), model, CI = .90, reliability = .95)</pre>
```

weighted.quantile 85

```
# ... or instead of raw scores for norm scores, the other way round
rawTable(c(8, 12), model, CI = .90, reliability = .95)
## End(Not run)
```

weighted.quantile

Weighted quantile estimator

Description

Computes weighted quantiles (code from Andrey Akinshin (2023) "Weighted quantile estimators" arXiv:2304.07265 [stat.ME] Code made available via the CC BY-NC-SA 4.0 license) on the basis of either the weighted Harrell-Davis quantile estimator or an adaption of the type 7 quantile estimator of the generic quantile function in the base package. Please provide a vector with raw values, the probabilities for the quantiles and an additional vector with the weight of each observation. In case the weight vector is NULL, a normal quantile estimation is done. The vectors may not include NAs and the weights should be positive non-zero values. Please draw on the computeWeights() function for retrieving weights in post stratification.

Usage

```
weighted.quantile(x, probs, weights = NULL, type = "Harrell-Davis")
```

Arguments

x A numerical vector

probs Numerical vector of quantiles

weights A numerical vector with weights; should have the same length as x

type Type of estimator, can either be "inflation", "Harrell-Davis" using a beta function

to approximate the weighted percentiles (Harrell & Davis, 1982) or "Type7" (default; Hyndman & Fan, 1996), an adaption of the generic quantile function in R, including weighting. The inflation procedure is essentially a numerical, non-parametric solution that gives the same results as Harrel-Davis. It requires less ressources with small datasets and always finds a solution (e. g. 1000 cases with weights between 1 and 10). If it becomes too resource intense, it switches to Harrell-Davis automatically. Harrel-Davis and Type7 code is based on the

work of Akinshin (2023).

Value

the weighted quantiles

References

- 1. Harrell, F.E. & Davis, C.E. (1982). A new distribution-free quantile estimator. Biometrika, 69(3), 635-640.
- 2. Hyndman, R. J. & Fan, Y. (1996). Sample quantiles in statistical packages, American Statistician 50, 361–365.
- 3. Akinshin, A. (2023). Weighted quantile estimators arXiv:2304.07265 [stat.ME]

See Also

weighted.quantile.inflation, weighted.quantile.harrell.davis, weighted.quantile.type7

weighted.quantile.harrell.davis

Weighted Harrell-Davis quantile estimator

Description

Computes weighted quantiles; code from Andrey Akinshin (2023) "Weighted quantile estimators" arXiv:2304.07265 [stat.ME] Code made available via the CC BY-NC-SA 4.0 license

Usage

weighted.quantile.harrell.davis(x, probs, weights = NULL)

Arguments

x A numerical vector

probs Numerical vector of quantiles

weights A numerical vector with weights; should have the same length as x. If no

weights are provided (NULL), it falls back to the base quantile function, type 7

Value

the quantiles

```
weighted.quantile.inflation
```

Weighted quantile estimator through case inflation

Description

Applies weighted ranking numerically by inflating cases according to weight. This function will be resource intensive, if inflated cases get too high and in this cases, it switches to the parametric Harrell-Davis estimator.

Usage

```
weighted.quantile.inflation(
    x,
    probs,
    weights = NULL,
    degree = 3,
    cutoff = 1e+07
)
```

Arguments

X	A numerical vector
probs	Numerical vector of quantiles
weights	A numerical vector with weights; should have the same length as x.
degree	power parameter for case inflation (default = 3, equaling factor 1000) If no weights are provided (NULL), it falls back to the base quantile function, type 7
cutoff	stop criterion for the sum of standardized weights to switch to Harrell-Davis,

default = 1000000

Value

the quantiles

```
weighted.quantile.type7
```

Weighted type7 quantile estimator

Description

Computes weighted quantiles; code from Andrey Akinshin (2023) "Weighted quantile estimators" arXiv:2304.07265 [stat.ME] Code made available via the CC BY-NC-SA 4.0 license

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Usage

```
weighted.quantile.type7(x, probs, weights = NULL)
```

Arguments

x A numerical vector

probs Numerical vector of quantiles

weights A numerical vector with weights; should have the same length as x. If no

weights are provided (NULL), it falls back to the base quantile function, type 7

Value

the quantiles

weighted.rank

Weighted rank estimation

Description

Conducts weighted ranking on the basis of sums of weights per unique raw score. Please provide a vector with raw values and an additional vector with the weight of each observation. In case the weight vector is NULL, a normal ranking is done. The vectors may not include NAs and the weights should be positive non-zero values.

Usage

```
weighted.rank(x, weights = NULL)
```

Arguments

x A numerical vector

weights A numerical vector with weights; should have the same length as x

Value

the weighted absolute ranks

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