

Package ‘geex’

October 13, 2022

Type Package

Title An API for M-Estimation

Version 1.1.1

Author Bradley Saul [aut, cre],
Brian Barkley [ctb]

Maintainer Bradley Saul <bradleysaul@gmail.com>

Description Provides a general, flexible framework for estimating parameters and empirical sandwich variance estimator from a set of unbiased estimating equations (i.e., M-estimation in the vein of Stefanski & Boos (2002) [doi:10.1198/000313002753631330](https://doi.org/10.1198/000313002753631330)). All examples from Stefanski & Boos (2002) are published in the corresponding Journal of Statistical Software paper “The Calculus of M-Estimation in R with geex” by Saul & Hudgens (2020) [doi:10.18637/jss.v092.i02](https://doi.org/10.18637/jss.v092.i02). Also provides an API to compute finite-sample variance corrections.

Depends R (>= 3.3)

Imports Matrix (>= 1.2-6), rootSolve (>= 1.6.6), numDeriv (>= 2014.2-1), lme4 (>= 1.1-12), methods (>= 3.3)

Suggests testthat, knitr, dplyr, moments, sandwich, inferference, xtable, AER, ICSNP, MASS, gee, saws, rmarkdown, geepack, covr, mvtnorm

URL <https://github.com/bsaul/geex>, <https://bsaul.github.io/geex/>

BugReports <https://github.com/bsaul/geex/issues>

License MIT + file LICENSE

LazyData TRUE

VignetteBuilder knitr

RoxygenNote 7.2.1

Encoding UTF-8

NeedsCompilation no

Repository CRAN

Date/Publication 2022-08-08 10:40:04 UTC

R topics documented:

geex-package	3
approx_control-class	4
basic_control-class	4
coef,geex-method	5
compute_sigma	5
correction	6
correct_by	7
correct_control-class	8
create_basis	8
create_GFUN	9
create_psiFUN_list	10
deriv_control-class	11
diagnose_roots	11
estimate_GFUN_roots	12
estimate_sandwich_matrices	13
estimating_function-class	14
fay_bias_correction	15
fay_df_correction	16
geex-class	17
geexex	17
geex_control-class	18
geex_summary-class	18
get_corrections	19
grab	20
grab_bread	20
grab_bread_list	21
grab_design_levels	22
grab_design_matrix	22
grab_ee_list	23
grab_estFUN	24
grab_fixed_formula	24
grab_GFUN	25
grab_meat	25
grab_meat_list	26
grab_psiFUN	27
grab_psiFUN_list	28
grab_response	29
grab_response_formula	30
m_estimate	30
m_estimation_basis-class	33
nobs,geex-method	34
roots	35
root_control-class	36
sandwich_components-class	36
setup_approx_control	36
setup_control	37

geex-package	3
--------------	---

setup_deriv_control	38
setup_root_control	38
show	39
summary,geex-method	40
vcov,geex-method	41
weights,geex-method	41

Index	43
--------------	-----------

geex-package	<i>geex: M-estimation API</i>
--------------	-------------------------------

Description

geex provides an extensible API for estimating parameters and their covariance from a set of estimating functions (M-estimation). M-estimation theory has a long history [see reference in the M-estimation bibliography: https://bsaul.github.io/geex/articles/articles/mestimation_bib.html. For an excellent introduction, see the primer by L.A. Stefanski and D.D. Boos, "The Calculus of M-estimation" (*The American Statistician* (2002), 56(1), 29-38) (<http://www.jstor.org/stable/3087324>).

Details

M-estimation encompasses a broad swath of statistical estimators and ideas including:

- the empirical "sandwich" variance estimator
- generalized estimating equations (GEE)
- many maximum likelihood estimators
- robust regression
- and many more

geex can implement all of these using a user-defined estimating function.

To learn more about geex, see the package vignettes: `browseVignettes(package = 'geex')`.

Goals

If you can specify a set of unbiased estimating equations, geex does the rest. The goals of geex are simply:

- To minimize the translational distance between a set of estimating functions and R code;
- To return numerically accurate point and covariance estimates from a set of unbiased estimating functions.

geex does not, by itself, necessarily aim to be fast nor precise. Such goals are left to the user to implement or confirm.

Author(s)

Maintainer: Bradley Saul <bradleysaul@gmail.com>

Other contributors:

- Brian Barkley [contributor]

References

Saul, Bradley C., and Michael G. Hudgens. (2020). "The Calculus of M-estimation in R with geex." Journal of Statistical Software 92(2), 1-15. doi: [10.18637/jss.v092.i02](https://doi.org/10.18637/jss.v092.i02).

See Also

Useful links:

- <https://github.com/bsaul/geex>
- <https://bsaul.github.io/geex/>
- Report bugs at <https://github.com/bsaul/geex/issues>

`approx_control-class` *approx_control S4 class*

Description

EXPERIMENTAL. See example 7 in `vignette("01_additional_examples", package = "geex")` for usage.

Slots

- .FUN a function which approximates an estFUN.
- .options a list of options passed to .FUN.

`basic_control-class` *basic_control S4 class*

Description

A general class for defining a function, and the options passed to the function

Slots

- .FUN a function
- .options a list of options passed to .FUN

See Also

[root_control-class](#), [deriv_control-class](#) [approx_control-class](#)

coef,geex-method	<i>Gets the parameter estimates from a geex object</i>
------------------	--------------------------------------------------------

Description

Gets the parameter estimates from a geex object

Usage

```
## S4 method for signature 'geex'
coef(object)

## S4 method for signature 'geex_summary'
coef(object)
```

Arguments

object a [geex](#) object

Examples

```
ex_eefUN <- function(data){
  function(theta){
    with(data,
      c(Y1 - theta[1],
        (Y1 - theta[1])^2 - theta[2] ))
  }
}

results <- m_estimate(
  estFUN = ex_eefUN,
  data  = geexex,
  root_control = setup_root_control(start = c(1,1)))

coef(results)
```

compute_sigma	<i>Compute empirical sandwich covariate estimator</i>
---------------	-------------------------------------------------------

Description

Computes $\Sigma = A^{-1}B(A^{-1})^T$ with provided A and B matrices.

Usage

```
compute_sigma(A, B, solver = solve)
```

Arguments

- A a matrix, generally the `.A` slot in a `sandwich_components` object created in `estimate_sandwich_matrices`
- B a matrix, generally the `.B` slot in a `sandwich_components` object created in `estimate_sandwich_matrices`
- solver the function used to compute the inverse of A, Defaults to `solve`

Value

```
the matrix Ainv %*% B %*% t(Ainv)
```

Examples

```
A <- diag(2, nrow = 2, ncol = 2)
B <- matrix(4, nrow = 2, ncol = 2)
compute_sigma(A = A, B = B)
```

correction*Creates a correct_control object***Description**

Creates a `correct_control` object

Usage

```
correction(FUN, ...)
```

Arguments

- FUN a correction to perform. `components` must be the first argument
- ... additional arguments passed to FUN

Value

a `correct_control` object

Examples

```
correction(FUN = fay_bias_correction, b = 0.75)
```

correct_by	<i>Correct sandwich components</i>
------------	------------------------------------

Description

Modifies the matrices in a `sandwich_components` object using the function and options in a `correct_control` object. The function `correction` is a utility for creating `correct_control` objects.

Usage

```
correct_by(.components, .correct_control)
```

Arguments

.components an object of class `sandwich_components`
.correct_control
 an object of class `correct_control`

Details

See the finite sample corrections vignette for further examples.

Value

the result of .FUN in .correct_control.

See Also

`fay_bias_correction` and `fay_df_correction` for corrections provided by geex

Examples

```
myee <- function(data){  
  function(theta){  
    c(data$Y1 - theta[1],  
      (data$Y1 - theta[1])^2 - theta[2])  
  }  
}  
mybasis <- create_basis(  
  estFUN = myee,  
  data   = geexex)  
mats <- estimate_sandwich_matrices(mybasis, .theta = c(5.04, 10.04))  
correct_by(mats,  
  .correct_control = correction(fay_bias_correction, b = .75))
```

`correct_control-class` *correct_control S4 class*

Description

`correct_control` S4 class

Slots

- .FUN a function which "corrects" a `sandwich_components` object. Usually a small-sample correction
- .options a list of options passed to .FUN.

`create_basis`

Creates an m_estimation_basis object

Description

Creates an `m_estimation_basis` object

Usage

```
create_basis(estFUN, data, units, outer_args, inner_args)
```

Arguments

- | | |
|-------------------------|--------------------------------------------------------------------------------------------------------------|
| <code>estFUN</code> | a function that takes in group-level data and returns a function that takes parameters as its first argument |
| <code>data</code> | a <code>data.frame</code> |
| <code>units</code> | an optional character string identifying the grouping variable in <code>data</code> |
| <code>outer_args</code> | a list of arguments passed to the outer (data) function of <code>estFUN</code> . (optional) |
| <code>inner_args</code> | a list of arguments passed to the inner (theta) function of <code>estFUN</code> . (optional) |

Details

Either `data` or `split_data` must be provided

Value

a `m_estimation_basis`

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}
mybasis <- create_basis(
  estFUN = myee,
  data   = geexex)
```

create_GFUN

Creates a function that sums over psi functions

Description

From a list of $\psi(O_i, \theta)$ for $i = 1, \dots, m$, creates $G_m = \sum_i \psi(O_i, \theta)$, called GFUN. Here, $\psi(O_i, \theta)$ is the *inner* part of an estFUN, in that the data is fixed and G_m is a function of θ .

Usage

```
create_GFUN(object, ...)
## S4 method for signature 'm_estimation_basis'
create_GFUN(object)
```

Arguments

object	an object of class <code>m_estimation_basis</code>
...	additional arguments passed to other methods

Value

a function

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}
mybasis <- create_basis(
  estFUN = myee,
  data   = geexex)
f <- grab_GFUN(create_GFUN(mybasis))
```

```
# Evaluate GFUN at mean and variance: should be close to zero
n <- nrow(geexex)
f(c(mean(geexex$Y1), var(geexex$Y1) * (n - 1)/n))
```

create_psiFUN_list *Creates list of psi functions*

Description

Creates the estimating function ($\psi(O_i, \theta)$) for each unit. That is, this function evaluates the outer function in `estFUN` for each independent unit and returns the inner function in `estFUN`.

Usage

```
create_psiFUN_list(object, ...)
## S4 method for signature 'm_estimation_basis'
create_psiFUN_list(object)
```

Arguments

object	an object of class <code>m_estimation_basis</code>
...	additional arguments passed to other methods

Value

the object with the `.psiFUN_list` slot populated.

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}
mybasis <- create_basis(
  estFUN = myee,
  data   = geexex)
psi_list <- grab_psiFUN_list(create_psiFUN_list(mybasis))

# A list of functions
head(psi_list)
```

deriv_control-class *deriv_control S4 class*

Description

deriv_control S4 class

Slots

- .FUN a function which computes a numerical derivation. This functions first argument must the function on which the derivative is being compute. Defaults to [jacobian](#).
- .options a list of options passed to .FUN. Defaults to list(method = 'Richardson')

diagnose_roots *Diagnose roots of estimating equations*

Description

Computes the value of

$$G_m = \sum_i \psi(O_i, \hat{\theta})$$

, i.e., the estimating equations at theta. Used to verify that $G_m = 0$ (or close to 0).

Usage

```
diagnose_roots(GFUN, theta)
```

Arguments

- | | |
|-------|--------------------------------------------------------------------|
| GFUN | a function of theta |
| theta | parameter estimates to use in evaluating the estimating equations. |

Value

a numeric vector

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

mest <- m_estimate(
```

```

estFUN = myee,
data   = geexex,
root_control = setup_root_control(start = c(1, 1)))

f <- grab_GFUN(mest@basis)
# Should be close to zero
diagnose_roots(GFUN = f, theta = roots(mest))

```

estimate_GFUN_roots *Estimate roots for a set of estimating equations*

Description

Using the rootFUN specified by the user (defaults to [multiroot](#)), this function estimates the roots of the equations:

$$G_m = \sum_i \psi(O_i, \hat{\theta}) = 0$$

Usage

```
estimate_GFUN_roots(.basis)
```

Arguments

.basis	an object of class m_estimation_basis
--------	-------------------------------------------------------

Details

This is primilary an internal function used within [m_estimate](#), but it is exported for use in debugging and development.

For an example of how to use a different rootFUN, see the root solver vignette, `vignette('geex_root_solvers', package = 'geex')`.

Value

the output of the rootFUN function

Examples

```

myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

# Start with a basic basis
mybasis <- create_basis(
  estFUN = myee,

```

```

data    = geexex)

# Add a control for the root solver
mycontrol <- new('geex_control', .root = setup_root_control(start = c(1, 1)))
mybasis@.control <- mycontrol

# Now estimate roots of GFUN
roots <- estimate_GFUN_roots(mybasis)
roots

```

estimate_sandwich_matrices

Estimate component matrices of the empirical sandwich covariance estimator

Description

For a given set of estimating equations computes the 'meat' (B_m in Stefanski and Boos notation) and 'bread' (A_m in Stefanski and Boos notation) matrices necessary to compute the covariance matrix.

Usage

```
estimate_sandwich_matrices(.basis, .theta)
```

Arguments

- | | |
|--------|-------------------------------------------------------------|
| .basis | basis an object of class m_estimation_basis |
| .theta | vector of parameter estimates (i.e. estimated roots) |

Details

For a set of estimating equations ($\sum_i \psi(O_i, \theta) = 0$), this function computes:

$$A_i = \partial\psi(O_i, \theta)/\partial\theta$$

$$A = \sum_i A_i$$

$$B_i = \psi(O_i, \theta)\psi(O_i, \theta)^T$$

$$B = \sum_i B_i$$

where all of the above are evaluated at $\hat{\theta}$. The partial derivatives in A_i numerically approximated by the function defined in [deriv_control](#).

Note that $A = \sum_i A_i$ and not $\sum_i A_i/m$, and the same for B .

Value

a [sandwich_components](#) object

References

Stefanski, L. A., & Boos, D. D. (2002). The calculus of m-estimation. *The American Statistician*, 56(1), 29-38.

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

# Start with a basic basis
mybasis <- create_basis(
  estFUN = myee,
  data   = geexex)

# Now estimate sandwich matrices
estimate_sandwich_matrices(
  mybasis, c(mean(geexex$Y1), var(geexex$Y1)))
```

estimating_function-class
estimating_function S4 class

Description

estimating_function S4 class

Slots

- .estFUN the estimating function.
- .outer_args a named list of arguments passed to the outer function of .estFUN. Should *not* include the data argument.
- .inner_args a named list of arguments passed to the inner function of .estFUN. Should *not* include the theta argument.

fay_bias_correction *Correct sandwich variance estimator by Fay's bias correction*

Description

Computes the bias corrected sandwich covariance matrix described in Fay and Graubard (2001). See `vignette("05_finite_sample_corrections", package = "geex")` for further information.

Usage

```
fay_bias_correction(components, b = 0.75)
```

Arguments

components	an object of class <code>sandwich_components</code>
b	a numeric value < 1. Defaults to 0.75 as in Fay.

Value

a corrected covariance matrix

References

Fay, M. P., & Graubard, B. I. (2001). Small-Sample adjustments for Wald-type tests using sandwich estimators. *Biometrics*, 57(4), 1198-1206

Examples

```
# This example demonstrates usage of the corrections, not a meaningful application
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

results <- m_estimate(
  estFUN = myee,
  data = geexex,
  root_control = setup_root_control(start = c(1,1)),
  corrections = list(
    bias_correction_.1 = correction(fay_bias_correction, b = .1),
    bias_correction_.3 = correction(fay_bias_correction, b = .3))
  )

get_corrections(results)
```

fay_df_correction	<i>Correct sandwich variance inference by Fay's degrees of freedom correction</i>
-------------------	-----------------------------------------------------------------------------------

Description

Computes the degrees of freedom correction described in Fay and Graubard (2001). See `vignette("05_finite_sample_correction", package = "geex")` for further information.

Usage

```
fay_df_correction(components, b = 0.75, L, version)
```

Arguments

components	an object of class <code>sandwich_components</code>
b	a numeric value < 1. Defaults to 0.75 as in Fay.
L	a k x p matrix where p is the dimension of theta
version	either 1 or 2, corresponding to hat(d) or tilde(d), respectively

Value

a scalar corresponding to the estimated degrees of freedom

References

Fay, M. P., & Graubard, B. I. (2001). Small-Sample adjustments for Wald-type tests using sandwich estimators. *Biometrics*, 57(4), 1198-1206

Examples

```
# This example demonstrates usage of the corrections, not a meaningful application
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

results <- m_estimate(
  estFUN = myee,
  data = geexex,
  root_control = setup_root_control(start = c(1,1)),
  corrections = list(
    df_correction1 = correction(fay_df_correction,
      b = .75, L = c(0, 1), version = 1 ),
    df_correction2 = correction(fay_df_correction,
```

```

    b = .75, L = c(0, 1), version = 2 ))
)
get_corrections(results)

```

geex-class

*geex S4 class***Description**

geex S4 class

Slots

call the `m_estimate` call
 basis a `m_estimation_basis` object
 rootFUN_results the results of call to the root finding algorithm function
 sandwich_components a `sandwich_components` object
 GFUN the function of which the roots are computed.
 corrections a list of correction performed on sandwich_components
 estimates a numeric vector of parameter estimates
 vcov the empirical sandwich variance matrix

geexex

*Dataset used to illustrate Stefanski and Boos examples.***Description**

The data used to illustrate examples 1-9 of Stefanski and Boos (2002).

Format

a dataset with 9 variables and 100 observations

- Y1 `rnorm(mean = 5, sd = 4)`
- Y2 `rnorm(mean = 2, sd = 1)`
- X1 `rgamma(shape = 5)`
- Y3 $2 + 3*X1 + 1*rnorm(0, 1)$
- W1 $X1 + 0.25 * rnorm(0, 1)$
- Z1 $2 + 1.5*X1 + 1*rnorm(0, 1)$
- X2 0 for first 50 observation, 1 for rest
- Y4 $0.1 + 0.1*X1 + 0.5*X2 + rnorm(0, 1)$
- Y5 `rbinom(prob = plogis(0.1 + 0.1*X1 + 0.5*X2))`

References

Stefanski, L. A., & Boos, D. D. (2002). The calculus of m-estimation. *The American Statistician*, 56(1), 29-38.

geex_control-class *geex_control S4 class*

Description

An object which control all the `basic_control` objects necessary to perform M-estimation

Slots

- .approx a `approx_control` object
- .root a `root_control` object
- .deriv a `deriv_control` object

geex_summary-class *geex summary object*

Description

geex summary object

Slots

- estFUN a estimating-function
- outer_args the list arguments passed to the `m_estimate` call
- inner_args the list arguments passed to the `m_estimate` call
- data the `data.frame` passed to the `m_estimate` call
- weights the weights passed to the `m_estimate` call
- nobs the number of observational units used to compute the M-estimator
- units the name of the variable identifying the observational units
- corrections a list of correction performed on `sandwich_components`
- estimates a numeric vector of parameter estimates
- vcov the empirical sandwich variance matrix

get_corrections *Gets the corrections from a geex object*

Description

Gets the corrections from a geex object

Usage

```
get_corrections(object, ...)

## S4 method for signature 'geex'
get_corrections(object)

## S4 method for signature 'geex_summary'
get_corrections(object)
```

Arguments

object	a geex object
...	arguments passed to other methods

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

results <- m_estimate(
  estFUN = myee,
  data = geexex,
  root_control = setup_root_control(start = c(1,1)),
  corrections = list(
    bias_correction_.1 = correction(fay_bias_correction, b = .1),
    bias_correction_.3 = correction(fay_bias_correction, b = .3))
)
get_corrections(results)
```

<code>grab</code>	<i>Grab something from an object</i>
-------------------	--------------------------------------

Description

Grab something from an object

Usage

```
grab(from, what, ...)
```

Arguments

<code>from</code>	an object
<code>what</code>	what to grab one of 'response', 'design_matrix', 'response_formula', 'fixed_formula', 'eeFUN'
<code>...</code>	additional arguments passed to <code>grab_**</code> function

Value

the value returns depends on the argument `what`.

See Also

[grab_response](#), [grab_design_matrix](#), [grab_response_formula](#), [grab_fixed_formula](#), [grab_design_levels](#)

<code>grab_bread</code>	<i>Grabs the .A (bread matrix) slot</i>
-------------------------	-----------------------------------------

Description

Grabs the .A (bread matrix) slot

Usage

```
grab_bread(object)
```

```
## S4 method for signature 'sandwich_components'
grab_bread(object)
```

Arguments

<code>object</code>	a sandwich_components object
---------------------	----------------------------------------------

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

results <- m_estimate(
  estFUN = myee,
  data = geexex,
  root_control = setup_root_control(start = c(1,1)))

grab_bread(results@sandwich_components)
```

grab_bread_list *Gets the .A_i (list of bread matrices) slot*

Description

Gets the .A_i (list of bread matrices) slot

Usage

```
grab_bread_list(object)

## S4 method for signature 'sandwich_components'
grab_bread_list(object)
```

Arguments

object a [sandwich_components](#) object

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

results <- m_estimate(
  estFUN = myee,
  data = geexex,
  root_control = setup_root_control(start = c(1,1)))

head(grab_bread_list(results@sandwich_components))
```

`grab_design_levels` *Grab a list of the levels of factor variables in a model.*

Description

Useful when splitting data later, used with `grab_design_matrix` or especially when calling `grab_psiFUN` from within an eeFun.

Usage

```
grab_design_levels(model)
```

Arguments

model	a model object such as <code>lm</code> , <code>glm</code> , <code>merMod</code>
-------	---------------------------------------------------------------------------------

Value

A named list of character vectors that provides the entire set of levels that each factor predictor in `model` will take on. This is hopefully identical to what the `xlev` argument to `link[stats]{model.frame}` desires. When `model` has no factors as predictors, then an empty list is returned.

Examples

```
## Not run:
geex:::grab_design_matrix(
  data = data,
  rhs_formula = geex:::grab_fixed_formula(model),
  xlev = geex:::grab_design_levels(model)
)
## Below is helpful within an eeFun.
geex:::grab_psiFUN(
  data = data,## Especially when this is a subset of the data
  rhs_formula = geex:::grab_fixed_formula(model),
  xlev = geex:::grab_design_levels(model)
)
## End(Not run)
```

`grab_design_matrix` *Grab a matrix of fixed effects from a model object*

Description

Grab a matrix of fixed effects from a model object

Usage

```
grab_design_matrix(data, rhs_formula, ...)
```

Arguments

- | | |
|-------------|---------------------------------------------------------|
| data | the data from which to extract the matrix |
| rhs_formula | the right hand side of a model formula |
| ... | Can be used to pass xlev to model.frame |

Value

a [model.matrix](#)

Examples

```
# Create a "desigm" matrix for the first ten rows of iris data
fit <- lm(Sepal.Width ~ Petal.Width, data = iris)
grab_design_matrix(
  data = iris[1:10, ],
  grab_fixed_formula(fit))
```

grab_ee_list *Gets the .ee_i (observed estimating function) slot*

Description

Gets the .ee_i (observed estimating function) slot

Usage

```
grab_ee_list(object)
```

Arguments

- | | |
|--------|----------------------------------------------|
| object | a sandwich_components object |
|--------|----------------------------------------------|

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

results <- m_estimate(
  estFUN = myee,
  data = geexex,
```

```
root_control = setup_root_control(start = c(1,1))

grab_ee_list(results@sandwich_components)
```

grab_estFUN*Grab estimating functions from a model object***Description**

Grab estimating functions from a model object

Usage

```
grab_estFUN(object)

## S4 method for signature 'estimating_function'
grab_estFUN(object)
```

Arguments

object	a estimating_function object
---------------	-------------------------------------

grab_fixed_formula*Grab the RHS formula from a model object***Description**

Grab the RHS formula from a model object

Usage

```
grab_fixed_formula(model)
```

Arguments

model	a model object such as lm , glm , merMod
--------------	---------------------------------------------------------------

Value

the right-hand side of a model's **formula** object

Examples

```
fit <- lm(Sepal.Width ~ Petal.Width, data = iris)
grab_fixed_formula(fit)
```

grab_GFUN*Gets the .psi_list slot in a m_estimation_basis*

Description

Gets the .psi_list slot in a m_estimation_basis

Usage

```
grab_GFUN(object)

## S4 method for signature 'm_estimation_basis'
grab_GFUN(object)

## S4 method for signature 'geex'
grab_GFUN(object)
```

Arguments

object a [m_estimation_basis](#) object

grab_meat*Gets the .B (meat matrix) slot*

Description

Gets the .B (meat matrix) slot

Usage

```
grab_meat(object)

## S4 method for signature 'sandwich_components'
grab_meat(object)
```

Arguments

object a [sandwich_components](#) object

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

results <- m_estimate(
  estFUN = myee,
  data = geexex,
  root_control = setup_root_control(start = c(1,1)))

grab_meat_list(results@sandwich_components)
```

grab_meat_list *Gets the .B_i (list of bread matrices) slot*

Description

Gets the .B_i (list of bread matrices) slot

Usage

```
grab_meat_list(object)

## S4 method for signature 'sandwich_components'
grab_meat_list(object)

## S4 method for signature 'sandwich_components'
grab_ee_list(object)
```

Arguments

object a [sandwich_components](#) object

Examples

```
myee <- function(data){
  function(theta){
    c(data$Y1 - theta[1],
      (data$Y1 - theta[1])^2 - theta[2])
  }
}

results <- m_estimate(
  estFUN = myee,
  data = geexex,
  root_control = setup_root_control(start = c(1,1)))
```

```
head(grab_meat_list(results@sandwich_components))
```

grab_psiFUN

Grab estimating functions from a model object

Description

Grab estimating functions from a model object

Usage

```
grab_psiFUN(object, ...)

## S3 method for class 'glm'
grab_psiFUN(object, data, ...)

## S3 method for class 'geeglm'
grab_psiFUN(object, data, ...)

## S3 method for class 'merMod'
grab_psiFUN(object, data, numderiv_opts = NULL, ...)
```

Arguments

object	the object from which to extract psiFUN
...	additonal arguments passed to other methods
data	the data to use for the estimating function
numderiv_opts	a list of arguments passed to numDeriv::grad

Value

a function corresponding to the estimating equations of a model

Methods (by class)

- `grab_psiFUN(glm)`: Create estimating equation function from a `glm` object
- `grab_psiFUN(geeglm)`: Create estimating equation function from a `geeglm` object
- `grab_psiFUN(merMod)`: Create estimating equation function from a `merMod` object

Examples

```

## Not run:
library(geepack)
library(lme4)
data('ohio')

glmfit <- glm(resp ~ age, data = ohio,
                family = binomial(link = "logit"))
geefit <- geeglm(resp ~ age, data = ohio, id = id,
                  family = binomial(link = "logit"))
glmmfit <- glmer(resp ~ age + (1|id), data = ohio,
                  family = binomial(link = "logit"))
example_ee <- function(data, model){
  f <- grab_psiFUN(model, data)
  function(theta){
    f(theta)
  }
}

m_estimate(
  estFUN = example_ee,
  data = ohio,
  compute_roots = FALSE,
  units = 'id',
  roots = coef(glmfit),
  outer_args = list(model = glmfit))
m_estimate(
  estFUN = example_ee,
  data = ohio,
  compute_roots = FALSE,
  units = 'id',
  roots = coef(geefit),
  outer_args = list(model = geefit))
m_estimate(
  estFUN = example_ee,
  data = ohio,
  compute_roots = FALSE,
  units = 'id',
  roots = unlist(getME(glmmfit, c('beta', 'theta'))),
  outer_args = list(model = glmmfit))

## End(Not run)

```

grab_psiFUN_list *Gets the .psi_list slot in a m_estimation_basis*

Description

Gets the .psi_list slot in a m_estimation_basis

Usage

```
grab_psiFUN_list(object)

## S4 method for signature 'm_estimation_basis'
grab_psiFUN_list(object)

## S4 method for signature 'geex'
grab_psiFUN_list(object)
```

Arguments

object a [m_estimation_basis](#) object

grab_response *Grab a vector of responses from a model object*

Description

Grab a vector of responses from a model object

Usage

```
grab_response(data, formula)
```

Arguments

data data.frame from which to extract the vector of responses
formula model formula

Value

a [model.response](#)

Examples

```
# Grab vector of responses for the first ten rows of iris data
fit <- lm(Sepal.Width ~ Petal.Width, data = iris)
grab_response(
  data = iris[1:10, ],
  formula(fit))
```

`grab_response_formula` *Grab the LHS formula from a model object*

Description

Grab the LHS formula from a model object

Usage

```
grab_response_formula(model)
```

Arguments

model	a model object such as <code>lm</code> , <code>glm</code> , <code>merMod</code>
-------	---------------------------------------------------------------------------------

Value

the left-hand side of a model's `formula` object

Examples

```
fit <- lm(Sepal.Width ~ Petal.Width, data = iris)
grab_response_formula(fit)
```

`m_estimate`

Estimate parameters and their covariance from a set of estimating equations

Description

M-estimation theory provides a framework for asymptotic properties of estimators that are solutions to estimating equations. Many R packages implement specific applications of estimating equations. **geex** aims to be provide a more general framework that any modelling method can use to compute point and variance estimates for parameters that are solutions to estimating equations of the form:

$$\sum_i \psi(O_i, \hat{\theta}) = 0$$

Usage

```
m_estimate(
  estFUN,
  data,
  units = character(0),
  weights = numeric(0),
  outer_args = list(),
```

```

    inner_args = list(),
    roots = NULL,
    compute_roots = TRUE,
    compute_vcov = TRUE,
    Asolver = solve,
    corrections,
    deriv_control,
    root_control,
    approx_control
)

```

Arguments

estFUN	a function that takes in group-level data and returns a function that takes parameters as its first argument
data	a data.frame
units	an optional character string identifying the grouping variable in data
weights	an optional vector of weights. See details.
outer_args	a list of arguments passed to the outer (data) function of estFUN. (optional)
inner_args	a list of arguments passed to the inner (theta) function of estFUN. (optional)
roots	a vector of parameter estimates must be provided if compute_roots = FALSE
compute_roots	whether or not to find the roots of the estimating equations. Defaults to TRUE.
compute_vcov	whether or not to compute the variance-covariance matrix. Defaults to TRUE.
Asolver	a function passed to compute_sigma used to compute the inverse of the "bread" matrix. Defaults to <code>solve</code> .
corrections	an optional list of small sample corrections where each list element is a <code>correct_control</code> object which contains two elements: <code>correctFUN</code> and <code>correctFUN_options</code> . The function <code>correction</code> constructs <code>correct_control</code> objects. See details for more information.
deriv_control	a <code>deriv_control</code> object
root_control	a <code>root_control</code> object
approx_control	a <code>approx_control</code> object

Details

The basic idea of **geex** is for the analyst to provide at least two items:

- data
- estFUN: (the ψ function), a function that takes unit-level data and returns a function in terms of parameters (θ)

With the estFUN, **geex** computes the roots of the estimating equations and/or the empirical sandwich variance estimator.

The root finding algorithm defaults to `multiroot` to estimate roots though the solver algorithm can be specified in the rootFUN argument. Starting values for `multiroot` are passed via the

`root_control` argument. See `vignette("v03_root_solvers", package = "geex")` for information on customizing the root solver function.

To compute only the covariance matrix, set `compute_roots = FALSE` and pass estimates of θ via the `roots` argument.

M-estimation is often used for clustered data, and a variable by which to split the `data.frame` into independent units is specified by the `units` argument. This argument defaults to `NULL`, in which case the number of units equals the number of rows in the `data.frame`.

For information on the finite-sample corrections, refer to the finite sample correction API vignette: `vignette("v05_finite_sample_corrections", package = "geex")`

Value

a `geex` object

Writing an estFUN

Description: An `estFUN` is a function representing ψ . `geex` works by breaking ψ into two parts:

- the "outer" part of the `estFUN` which manipulates `data` and `outer_args` and returns an
- "inner" function of `theta` and `inner_args`. Internally, this "inner" function is called `psiFUN`.

In pseudo-code this looks like:

```
function(data, <><outer_args>>){
  O <- manipulate(data, <><outer_args>>)
  function(theta, <><inner_args>>){
    map(O, to = theta, and = <><inner_args>>)
  }
}
```

See the examples below or the package vignettes to see an `estFUN` in action.

Importantly, the `data` used in an `estFUN` is *unit* level data, which may be single rows in a `data.frame` or block of rows for clustered data.

Additional arguments: Additional arguments may be passed to both the inner and outer function of the `estFUN`. Elements in an `outer_args` list are passed to the outer function; any elements of the `inner_args` list are passed to the inner function. For an example, see the finite sample correction vignette [`vignette("v05_finite_sample_corrections", package = "geex")`].

Setting up root_control

To estimate roots of the estimating functions, `geex` uses the `rootSolve multiroot` function by default, which requires starting values. The `root_control` argument expects a `root_control` object, which the utility function `setup_root_control` aids in creating. For example, `setup_root_control(start = 4)` creates a `root_control` setting the starting value to 4. In general, the dimension of `start` must be the same as `theta` in the inner `estFUN`.

Using weights

In some situations, use of weights can massively speed computations. Refer to `vignette("v04_weights", package = "geex")` for an example.

References

Stefanski, L. A., & Boos, D. D. (2002). The calculus of M-estimation. *The American Statistician*, 56(1), 29-38.

Examples

```
# Estimate the mean and variance of Y1 in the geexex dataset
ex_eefUN <- function(data){
  function(theta){
    with(data,
      c(Y1 - theta[1],
        (Y1 - theta[1])^2 - theta[2] ))
  }
}

m_estimate(
  estFUN = ex_eefUN,
  data  = geexex,
  root_control = setup_root_control(start = c(1,1)))

# compare to the mean() and variance() functions
mean(geexex$Y1)
n <- nrow(geexex)
var(geexex$Y1) * (n - 1)/n

# A simple linear model for regressing X1 and X2 on Y4
lm_eefun <- function(data){
  X <- cbind(1, data$X1, data$X2)
  Y <- data$Y4
  function(theta){
    t(X) %*% (Y - X %*% theta)
  }
}

m_estimate(
  estFUN = lm_eefun,
  data  = geexex,
  root_control = setup_root_control(start = c(0, 0, 0)))

# Compare to lm() results
summary(lm(Y4 ~ X1 + X2, data = geexex))
```

m_estimation_basis-class

m_estimation_basis S4 class

Description

m_estimation_basis S4 class

Slots

- .data the analysis data.frame
- .units an (optional) character string identifying the variable in .data which splits the data into independent units
- .weights a numeric vector of weights used in weighting the estimating functions
- .psiFUN_list a list of psiFUNs created by `create_psiFUN_list`
- .GFUN a function created by `create_GFUN`
- .control a `geex_control` object

nobs,geex-method	<i>Extract the number observations</i>
------------------	----------------------------------------

Description

Extract the number observations

Usage

```
## S4 method for signature 'geex'
nobs(object)

## S4 method for signature 'geex_summary'
nobs(object)
```

Arguments

object a `geex` object

Examples

```
library(geepack)
data('ohio')

glmfit <- glm(resp ~ age, data = ohio,
                family = binomial(link = "logit"))
example_ee <- function(data, model){
  f <- grab_psiFUN(model, data)
  function(theta){
    f(theta)
  }
}
z <- m_estimate(
  estFUN = example_ee,
  data = ohio,
  compute_roots = FALSE,
  units = 'id',
  roots = coef(glmfit),
```

```
outer_args = list(model = glmfit)  
nobs(z)
```

roots*Gets the parameter estimates matrix from a geex object*

Description

Gets the parameter estimates matrix from a geex object

Usage

```
roots(object, ...)  
  
## S4 method for signature 'geex'  
roots(object)  
  
## S4 method for signature 'geex_summary'  
roots(object)
```

Arguments

object	a geex object
...	arguments passed to other methods

Examples

```
ex_eefUN <- function(data){  
  function(theta){  
    with(data,  
      c(Y1 - theta[1],  
       (Y1 - theta[1])^2 - theta[2] ))  
  }}  
  
results <- m_estimate(  
  estFUN = ex_eefUN,  
  data = geexex,  
  root_control = setup_root_control(start = c(1,1)))  
  
roots(results)
```

`root_control-class` *root_control S4 class*

Description

`root_control` S4 class

Slots

- .FUN a root finding function whose first argument must be named f.
- .options a list of options passed to .FUN.
- .object_name a character string identifying the object containing the roots in the output of .FUN.

`sandwich_components-class` *sandwich_components S4 class*

Description

`sandwich_components` S4 class

Slots

- .A the "bread" matrix
- .A_i a list of "bread" matrices per unit
- .B the "meat" matrix
- .B_i a list of "meat" matrices per unit
- .ee_i a list of observed estimating function values per unit

`setup_approx_control` *Setup an approx_control object*

Description

Setup an approx_control object

Usage

`setup_approx_control(FUN, ...)`

Arguments

FUN	a function
...	arguments passed to FUN

Value

a [approx_control](#) object

Examples

```
# For usage, see example 7 in  
vignette("01_additional_examples", package = "geex")
```

setup_control *Setup a basic_control object*

Description

Setup a basic_control object

Usage

```
setup_control(type, FUN, ...)
```

Arguments

type	one of c("deriv", "approx", "root")
FUN	a function
...	arguments passed to FUN

Value

a [basic_control](#) object

See Also

[setup_root_control](#), [setup_deriv_control](#), [setup_approx_control](#)

`setup_deriv_control` *Setup a deriv_control object*

Description

Setup a deriv_control object

Usage

```
setup_deriv_control(FUN, ...)
```

Arguments

<code>FUN</code>	a function
<code>...</code>	arguments passed to FUN

Value

a `deriv_control` object

Examples

```
setup_deriv_control() # default
setup_deriv_control(method = "simple") # will speed up computations
```

`setup_root_control` *Setup a root_control object*

Description

Setup a root_control object

Usage

```
setup_root_control(FUN, roots_name, ...)
```

Arguments

<code>FUN</code>	a function
<code>roots_name</code>	a character string identifying the object containing the arguments passed to FUN
<code>...</code>	

Value

a `root_control` object

Examples

```
# Setup the default
setup_root_control(start = c(3, 5, 6))

# Also setup the default
setup_root_control(FUN = rootSolve::multiroot,
                   start = c(3, 5, 6))

# Or use uniroot()
setup_root_control(FUN = stats::uniroot,
                   interval = c(0, 1))
```

show

Show (print) the S4 geex classes

Description

`m_estimation_basis`, or `geex` object

Usage

```
show(object)

## S4 method for signature 'sandwich_components'
show(object)

## S4 method for signature 'm_estimation_basis'
show(object)

## S4 method for signature 'geex'
show(object)

## S4 method for signature 'geex_summary'
show(object)
```

Arguments

`object` the object to print

 summary.geex-method *Object Summaries*

Description

Object Summaries

Usage

```
## S4 method for signature 'geex'
summary(object, keep_data = TRUE, keep_args = TRUE)
```

Arguments

object	a geex object
keep_data	keep the original data or not
keep_args	keep the outer_args and inner_args passed to estFUN or not

Examples

```
library(geepack)
data('ohio')
glmfit <- glm(resp ~ age, data = ohio,
                 family = binomial(link = "logit"))
example_ee <- function(data, model){
  f <- grab_psiFUN(model, data)
  function(theta){
    f(theta)
  }
}
z <- m_estimate(
  estFUN = example_ee,
  data = ohio,
  compute_roots = FALSE,
  units = 'id',
  roots = coef(glmfit),
  outer_args = list(model = glmfit))

object.size(z)
object.size(summary(z))
object.size(summary(z, keep_data = FALSE))
object.size(summary(z, keep_data = FALSE, keep_args = FALSE))
```

vcov,geex-method	<i>Gets the variance-covariance matrix from a geex object</i>
------------------	---------------------------------------------------------------

Description

Gets the variance-covariance matrix from a geex object

Usage

```
## S4 method for signature 'geex'
vcov(object)

## S4 method for signature 'geex_summary'
vcov(object)
```

Arguments

object a [geex](#) object

Examples

```
ex_eefUN <- function(data){
  function(theta){
    with(data,
      c(Y1 - theta[1],
        (Y1 - theta[1])^2 - theta[2] ))
  }
}

results <- m_estimate(
  estFUN = ex_eefUN,
  data = geexex,
  root_control = setup_root_control(start = c(1,1)))

vcov(results)
```

weights,geex-method	<i>Extract Model weights</i>
---------------------	------------------------------

Description

Extract Model weights

Usage

```
## S4 method for signature 'geex'
weights(object)

## S4 method for signature 'geex_summary'
weights(object)
```

Arguments

object a [geex](#) object

Index

* datasets

geexex, 17

approx_control, 18, 31, 37

approx_control-class, 4

basic_control, 18, 37

basic_control-class, 4

coef, geex, geex-method

(coef, geex-method), 5

coef, geex-method, 5

coef, geex_summary-method

(coef, geex-method), 5

compute_sigma, 5

correct_by, 7

correct_control, 6, 7, 31

correct_control-class, 8

correction, 6, 7, 31

create_basis, 8

create_GFUN, 9, 34

create_GFUN, m_estimation_basis, m_estimation_basis-method

(create_GFUN), 9

create_GFUN, m_estimation_basis-method

(create_GFUN), 9

create_psiFUN_list, 10, 34

create_psiFUN_list, m_estimation_basis, m_estimation_basis-method

(create_psiFUN_list), 10

create_psiFUN_list, m_estimation_basis-method

(create_psiFUN_list), 10

deriv_control, 13, 18, 31, 38

deriv_control-class, 11

diagnose_roots, 11

estimate_GFUN_roots, 12

estimate_sandwich_matrices, 6, 13

estimating_function, 24

estimating_function-class, 14

fay_bias_correction, 7, 15

fay_df_correction, 7, 16

formula, 24, 30

geex, 5, 19, 32, 34, 35, 39–42

geex (geex-package), 3

geex-class, 17

geex-package, 3

geex_control, 34

geex_control-class, 18

geex_summary-class, 18

geexex, 17

get_corrections, 19

get_corrections, geex-method

(get_corrections), 19

get_corrections, geex_summary-method

(get_corrections), 19

get_corrections, m_estimation_basis, m_estimation_basis-method

(get_corrections), 19

grab, 20

grab_bread, 20

grab_bread, sandwich_components, sandwich_components-method

(grab_bread), 20

grab_bread, sandwich_components-method

(grab_bread), 20

grab_bread_list, 21

grab_bread_list, sandwich_components, sandwich_components-method

(grab_bread_list), 21

grab_bread_list, sandwich_components-method

(grab_bread_list), 21

grab_design_levels, 20, 22

grab_design_matrix, 20, 22, 22

grab_ee_list, 23

grab_ee_list, sandwich_components-method

(grab_meat_list), 26

grab_estFUN, 24

grab_estFUN, estimating_function, estimating_function-method

(grab_estFUN), 24

grab_estFUN, estimating_function-method

(grab_estFUN), 24

grab_fixed_formula, 20, 24

grab_GFUN, 25
 grab_GFUN, geex, geex-method (grab_GFUN), 25
 grab_GFUN, geex-method (grab_GFUN), 25
 grab_GFUN, m_estimation_basis, m_estimation_basis-method (grab_GFUN), 25
 grab_GFUN, m_estimation_basis-method (grab_GFUN), 25
 grab_meat, 25
 grab_meat, sandwich_components, sandwich_components-method (grab_meat), 25
 grab_meat, sandwich_components-method (grab_meat), 25
 grab_meat_list, 26
 grab_meat_list, sandwich_components, sandwich_components-method (grab_meat_list), 26
 grab_meat_list, sandwich_components-method (grab_meat_list), 26
 grab_psiFUN, 22, 27
 grab_psiFUN_list, 28
 grab_psiFUN_list, geex, geex-method (grab_psiFUN_list), 28
 grab_psiFUN_list, geex-method (grab_psiFUN_list), 28
 grab_psiFUN_list, m_estimation_basis, m_estimation_basis-method (grab_psiFUN_list), 28
 grab_psiFUN_list, m_estimation_basis-method (grab_psiFUN_list), 28
 grab_response, 20, 29
 grab_response_formula, 20, 30

 jacobian, 11

 m_estimate, 12, 30
 m_estimation_basis, 8–10, 12, 13, 17, 25, 29, 39
 m_estimation_basis-class, 33
 model.frame, 23
 model.matrix, 23
 model.response, 29
 multiroot, 12, 31, 32

 nobs, geex, geex-method (nobs, geex-method), 34
 nobs, geex-method, 34
 nobs, geex_summary, geex_summary-method (nobs, geex-method), 34
 nobs, geex_summary-method (nobs, geex-method), 34

root_control, 18, 31, 32, 38
 root_control-class, 36
 roots, 35
 roots, geex, geex-method (roots), 35
 roots, geex-method (roots), 35
 roots, geex_summary-method (roots), 35

 sandwich_components, 6–8, 14–17, 20, 21, 23, 25, 26
 sandwich_components-class, 36
 setup_approx_control, 36, 37
 setup_control, 37
 setup_deriv_control, 37, 38
 setup_root_control, 32, 37, 38
 show, 39
 show, sandwich_components-method (show), 39
 show, geex-method (show), 39
 show, geex_summary, geex_summary-method (show), 39
 show, geex_summary-method (show), 39
 show, m_estimation_basis, m_estimation_basis-method (show), 39
 show, m_estimation_basis-method (show), 39
 show, sandwich_components, sandwich_components-method (show), 39
 show, sandwich_components-method (show), 39
 solve, 6, 31
 summary, geex-method, 40

vcov, geex, geex-method (vcov, geex-method), 41
 vcov, geex-method, 41
 vcov, geex_summary, geex_summary-method (vcov, geex-method), 41
 vcov, geex_summary-method (vcov, geex-method), 41

 weights, geex, geex-method (weights, geex-method), 41
 weights, geex-method, 41
 weights, geex_summary, geex_summary-method (weights, geex-method), 41
 weights, geex_summary-method (weights, geex-method), 41