Package 'dsem'

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Description Applies dynamic structural equation models to time-series data with generic and simplified specification for simultaneous and lagged effects. Methods are described in Thorson et al. (2024) ``Dynamic structural equation models synthesize ecosystem dynamics

constrained by ecological mechanisms."

License GPL-3

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as_fitted_DAG

Description

Convert dsem to phylopath output

Usage

```
as_fitted_DAG(
   fit,
   lag = 0,
   what = c("Estimate", "Std_Error", "p_value"),
   direction = 1
)
```

Arguments

fit	Output from dsem
lag	which lag to output
what	whether to output estimates what="Estimate", standard errors what="Std_Error" or p-values what="Std_Error"
direction	whether to include one-sided arrows direction=1, or both one- and two-sided arrows direction=c(1,2)

Value

Convert output to format supplied by est_DAG

```
as_sem
```

Convert dsem to sem output

Description

Convert output from package dsem to sem

Usage

as_sem(object, lag = 0)

Arguments

object	Output from dsem
lag	what lag to extract and visualize

Value

Convert output to format supplied by sem

bering_sea Bering Sea marine ecosystem

Description

Data used to demonstrate and test ecosystem synthesis

Usage

data(bering_sea)

cAIC

Calculate conditional AIC

Description

Calculates the conditional Akaike Information criterion (cAIC).

Usage

cAIC(object, what = c("cAIC", "EDF"))

Arguments

object	Output from dsem
what	Whether to return the cAIC or the effective degrees of freedom (EDF) for each
	group of random effects.

Details

cAIC is designed to optimize the expected out-of-sample predictive performance for new data that share the same random effects as the in-sample (fitted) data, e.g., spatial interpolation. In this sense, it should be a fast approximation to optimizing the model structure based on k-fold crossvalidation. By contrast, AIC calculates the marginal Akaike Information Criterion, which is designed to optimize expected predictive performance for new data that have new random effects, e.g., extrapolation, or inference about generative parameters.

cAIC also calculates as a byproduct the effective degrees of freedom, i.e., the number of fixed effects that would have an equivalent impact on model flexibility as a given random effect.

Both cAIC and EDF are calculated using Eq. 6 of Zheng Cadigan Thorson 2024.

Note that, for models that include profiled fixed effects, these profiles are turned off.

Value

Either the cAIC, or the effective degrees of freedom (EDF) by group of random effects

References

Deriving the general approximation to cAIC used here

Zheng, N., Cadigan, N., & Thorson, J. T. (2024). A note on numerical evaluation of conditional Akaike information for nonlinear mixed-effects models (arXiv:2411.14185). arXiv. doi:10.48550/arXiv.2411.14185

The utility of EDF to diagnose hierarchical model behavior

Thorson, J. T. (2024). Measuring complexity for hierarchical models using effective degrees of freedom. Ecology, 105(7), e4327 doi:10.1002/ecy.4327

classify_variables Classify variables path

Description

classify_variables is copied from sem:::classifyVariables

Usage

```
classify_variables(model)
```

Arguments

model SEM model

Details

Copied from package 'sem' under licence GPL (>= 2) with permission from John Fox

Value

Tagged-list defining exogenous and endogenous variables

convert_equations Convert equations notation

Description

Converts equations to arrow-and-lag notation expected by dsem

Usage

convert_equations(equations)

Arguments

equations Specification for time-series structural equation model structure including lagged or simultaneous effects. See Details section in convert_equations for more description

Details

The function modifies code copied from package 'sem' under licence GPL (≥ 2) with permission from John Fox.

For specifyEquations, each input line is either a regression equation or the specification of a variance or covariance. Regression equations are of the form y = par1*x1 + par2*x2 + ... + park*xk where y and the xs are variables in the model (either observed or latent), and the pars are parameters. If a parameter is given as a numeric value (e.g., 1) then it is treated as fixed. Note that no error variable is included in the equation; error variances are specified via either the covs argument, via V(y) = par (see immediately below), or are added automatically to the model when, as by default, endog.variances=TRUE. A regression equation may be split over more than one input by breaking at a +, so that + is either the last non-blank character on a line or the first non-blank character on the subsequent line.

Variances are specified in the form V(var) = par and covariances in the form C(var1, var2) = par, where the vars are variables (observed or unobserved) in the model. The symbols V and C may be in either lower- or upper-case. If par is a numeric value (e.g., 1) then it is treated as fixed. In conformity with the RAM model, a variance or covariance for an endogenous variable in the model is an error variance or covariance.

To set a start value for a free parameter, enclose the numeric start value in parentheses after the parameter name, as parameter(value).

dsem

Description

Fits a dynamic structural equation model

Usage

```
dsem(
    sem,
    tsdata,
    family = rep("fixed", ncol(tsdata)),
    estimate_delta0 = FALSE,
    prior_negloglike = NULL,
    control = dsem_control(),
    covs = colnames(tsdata)
)
```

Arguments

sem	Specification for time-series structural equation model structure including lagged or simultaneous effects. See Details section in make_dsem_ram for more description	
tsdata	time-series data, as outputted using ts, with NA for missing values.	
family	Character-vector listing the distribution used for each column of tsdata, where each element must be fixed (for no measurement error), normal for normal measurement error using an identity link, gamma for a gamma measurement er- ror using a fixed CV and log-link, bernoulli for a Bernoulli measurement error using a logit-link, or poisson for a Poisson measurement error using a log-link. family="fixed" is default behavior and assumes that a given variable is mea- sured exactly. Other options correspond to different specifications of measure- ment error.	
estimate_delta0		
	Boolean indicating whether to estimate deviations from equilibrium in initial year as fixed effects, or alternatively to assume that dynamics start at some stochastic draw away from the stationary distribution	
prior_negloglik	e	
	A user-provided function that takes as input the vector of fixed effects out\$obj\$par returns the negative log-prior probability. For example prior_negloglike = function(obj) -1 * dnorm(obj\$par[1], mean=0, sd=0.1, log=TRUE) spec- ifies a normal prior probability for the for the first fixed effect with mean of zero and logsd of 0.1. NOTE: this implementation does not work well with tmbstan and is highly experimental. If using priors, considering using dsemRTMB instead. The option in dsem is mainly intended to validate its use in dsemRTMB. Note that the user must load RTMB using library(RTMB) prior to running the model.	

control	Output from dsem_control, used to define user settings, and see documentation for that function for details.
covs	optional: a character vector of one or more elements, with each element giving a string of variable names, separated by commas. Variances and covariances among all variables in each such string are added to the model. Warning: $covs="x1, x2"$ and $covs=c("x1", "x2")$ are not equivalent: $covs="x1, x2"$ specifies the variance of x1, the variance of x2, and their covariance, while $covs=c("x1", "x2")$ specifies the variance of x1 and the variance of x2 but not their covariance. These same covariances can be added manually via argument 'sem', but using argument 'covs' might save time for models with many variables.

Details

A DSEM involves (at a minimum):

Time series a matrix **X** where column \mathbf{x}_c for variable c is a time-series;

Path diagram a user-supplied specification for the path coefficients, which define the precision (inverse covariance) **Q** for a matrix of state-variables and see make_dsem_ram for more details on the math involved.

The model also estimates the time-series mean μ_c for each variable. The mean and precision matrix therefore define a Gaussian Markov random field for X:

$$\operatorname{vec}(\mathbf{X}) \sim \operatorname{MVN}(\operatorname{vec}(\mathbf{I}_{\mathbf{T}} \otimes \mu), \mathbf{Q}^{-1})$$

Users can the specify a distribution for measurement errors (or assume that variables are measured without error) using argument family. This defines the link-function $g_c(.)$ and distribution $f_c(.)$ for each time-series c:

$$y_{t,c} \sim f_c(g_c^{-1}(x_{t,c}), \theta_c)$$

dsem then estimates all specified coefficients, time-series means μ_c , and distribution measurement errors θ_c via maximizing a log-marginal likelihood, while also estimating state-variables $x_{t,c}$. summary.dsem then assembles estimates and standard errors in an easy-to-read format. Standard errors for fixed effects (path coefficients, exogenoux variance parameters, and measurement error parameters) are estimated from the matrix of second derivatives of the log-marginal likelihod, and standard errors for random effects (i.e., missing or state-space variables) are estimated from a generalization of this method (see sdreport for details).

Any column \mathbf{x}_c of tsdata that includes only NA values represents a latent variable, and all others are called manifest variables. The identifiability criteria for latent variables can be complicated. To explain, we ignore lagged effects (only simultaneous paths) and classify three types of latent variables:

factor latent variables: any latent variable F that includes paths out from it to manifest variables, but has no paths from manifest variables into F is a factor variable. These are identifable by fixing their SD (i.e., at one), and using a trimmed Cholesky parameterization (i.e., each successive factor includes fewer paths to manifest variables). See the DFA vignette for an example. Factor latent variables can be used to represent residual covariance while also estimating the source of that covariance explicitly

- intermediate latent variables: Any latent variable Y that includes paths in from some manifest variables X and some paths out to manifest variables Z is an intermediate latent variable. In general, the at least one path in or out must be fixed a priori (e.g., at one) to identify the scale of the intermediate LV. These intermediate latent variables can represent ecological concepts that serve as intermediate link between different manifest variables
- **composite latent variables:** Any latent variable **C** that includes paths in from some manifest variables **X** and no paths out to manifest variables is a composite latent variable. In general, you must fix all paths to composite variables a priori, and must also fix the SD a priori (e.g., at zero). These composite variables allow DSEM to estimate a response with standard errors that integrates across multiple manifest variables

As stated, these criteria do not involve paths from one to another latent variable. These are also possible, but involve more complicated identifiability criteria.

Value

An object (list) of class 'dsem'. Elements include:

obj TMB object from MakeADFun

ram RAM parsed by make_dsem_ram

model SEM structure parsed by make_dsem_ram as intermediate description of model linkages

tmb_inputs The list of inputs passed to MakeADFun

opt The output from nlminb

sdrep The output from sdreport

interal Objects useful for package function, i.e., all arguments passed during the call

run_time Total time to run model

References

Introducing the package, its features, and comparison with other software (to cite when using dsem):

Thorson, J. T., Andrews, A., Essington, T., Large, S. (2024). Dynamic structural equation models synthesize ecosystem dynamics constrained by ecological mechanisms. Methods in Ecology and Evolution. doi:10.1111/2041210X.14289

Examples

```
# Define model
sem = "
    # Link, lag, param_name
    cprofits -> consumption, 0, a1
    cprofits -> consumption, 1, a2
    pwage -> consumption, 0, a3
    gwage -> consumption, 0, a3
    cprofits -> invest, 0, b1
    cprofits -> invest, 1, b2
    capital -> invest, 0, b3
    gnp -> pwage, 0, c2
```

```
gnp -> pwage, 1, c3
  time -> pwage, 0, c1
,,
# Load data
data(KleinI, package="AER")
TS = ts(data.frame(KleinI, "time"=time(KleinI) - 1931))
tsdata = TS[,c("time","gnp","pwage","cprofits",'consumption',
               "gwage", "invest", "capital")]
# Fit model
fit = dsem( sem=sem,
            tsdata = tsdata,
            estimate_delta0 = TRUE,
            control = dsem_control(quiet=TRUE) )
summary( fit )
plot( fit )
plot( fit, edge_label="value" )
```

dsemRTMB

Fit dynamic structural equation model

Description

Fits a dynamic structural equation model

Usage

```
dsemRTMB(
    sem,
    tsdata,
    family = rep("fixed", ncol(tsdata)),
    estimate_delta0 = FALSE,
    log_prior = function(p) 0,
    control = dsem_control(),
    covs = colnames(tsdata)
)
```

Arguments

sem	Specification for time-series structural equation model structure including lagged or simultaneous effects. See Details section in make_dsem_ram for more de- scription	
tsdata	time-series data, as outputted using ts, with NA for missing values.	
family	Character-vector listing the distribution used for each column of tsdata, where	
	each element must be fixed (for no measurement error), normal for normal	

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	measurement error using an identity link, gamma for a gamma measurement er- ror using a fixed CV and log-link, bernoulli for a Bernoulli measurement error using a logit-link, or poisson for a Poisson measurement error using a log-link. family="fixed" is default behavior and assumes that a given variable is mea- sured exactly. Other options correspond to different specifications of measure- ment error.	
estimate_delta0		
	Boolean indicating whether to estimate deviations from equilibrium in initial year as fixed effects, or alternatively to assume that dynamics start at some stochastic draw away from the stationary distribution	
log_prior	A user-provided function that takes as input the list of parameters out\$obj\$env\$parList() where out is the output from dsemRTMB(), and returns the log-prior probabil- ity. For example log_prior = function(p) dnorm(p\$beta_z[1], mean=0, sd=0.1, log=TRUE) specifies a normal prior probability for the first path coefficient with mean of zero and sd of 0.1. Note that the user must load RTMB using library(RTMB) prior to running the model.	
control	Output from dsem_control, used to define user settings, and see documentation	

covs optional: a character vector of one or more elements, with each element giving a string of variable names, separated by commas. Variances and covariances among all variables in each such string are added to the model. Warning: covs="x1, x2" and covs=c("x1", "x2") are not equivalent: covs="x1, x2" specifies the variance of x1, the variance of x2, and their covariance, while covs=c("x1", "x2") specifies the variance of x1 and the variance of x2 but not their covariance. These same covariances can be added manually via argument 'sem', but using argument 'covs' might save time for models with many variables.

Details

dsemRTMB is interchangeable with dsem, but uses RTMB instead of TMB for estimation. Both are provided for comparison and real-world comparison. See ?dsem for more details

Value

An object (list) of class 'dsem', fitted using RTMB

for that function for details.

Examples

```
# Define model
sem = "
    # Link, lag, param_name
    cprofits -> consumption, 0, a1
    cprofits -> consumption, 1, a2
    pwage -> consumption, 0, a3
    gwage -> consumption, 0, a3
    cprofits -> invest, 0, b1
    cprofits -> invest, 1, b2
    capital -> invest, 0, b3
```

dsem_control

Detailed control for dsem structure

Description

Define a list of control parameters. Note that the format of this input is likely to change more rapidly than that of dsem

Usage

```
dsem_control(
  nlminb_loops = 1,
  newton_loops = 1,
  trace = 0,
  eval.max = 1000,
  iter.max = 1000,
  getsd = TRUE,
  quiet = FALSE,
  run_model = TRUE,
  gmrf_parameterization = c("separable", "projection"),
  constant_variance = c("conditional", "marginal", "diagonal"),
  use_REML = TRUE,
  profile = NULL,
  parameters = NULL,
 map = NULL,
  getJointPrecision = FALSE,
  extra_convergence_checks = TRUE,
  lower = -Inf,
  upper = Inf
)
```

dsem_control

Arguments

0	
nlminb_loops	Integer number of times to call nlminb.
newton_loops	Integer number of Newton steps to do after running nlminb.
trace	Parameter values are printed every 'trace' iteration for the outer optimizer. Passed to 'control' in nlminb.
eval.max	Maximum number of evaluations of the objective function allowed. Passed to 'control' in nlminb.
iter.max	Maximum number of iterations allowed. Passed to 'control' in nlminb.
getsd	Boolean indicating whether to call sdreport
quiet	Boolean indicating whether to run model printing messages to terminal or not;
run_model	Boolean indicating whether to estimate parameters (the default), or instead to return the model inputs and compiled TMB object without running;
gmrf_parameter	ization
	Parameterization to use for the Gaussian Markov random field, where the default 'separable' constructs a precision matrix that must be full rank, and the alterna- tive 'projection' constructs a full-rank and IID precision for variables over time, and then projects this using the inverse-cholesky of the precision, where this projection can be rank-deficient.
constant_varia	nce
	Whether to specify a constant conditional variance $\Gamma\Gamma^t$ using the default constant_variance="condition which results in a changing marginal variance along the specified causal graph when lagged paths are present. Alternatively, the user can specify a constant marginal variance using constant_variance="diagonal" or constant_variance="marginal", such that Γ and $I - P$ are rescaled to achieve this constraint. All options are equivalent when the model includes no lags (only simultaneous effects) and no covariances (no two-headed arrows). "diagonal" and "marginal" are equivalent when the model includes no covariances. Given some exogenous covariance, constant_variance = "diagonal" preserves the conditional correlation and has changing conditional variance, while constant_variance = "marginal" has changing conditional correlation along the causal graph.
use_REML	Boolean indicating whether to treat non-variance fixed effects as random, ei- ther to motigate bias in estimated variance parameters or improve efficiency for parameter estimation given correlated fixed and random effects
profile	Parameters to profile out of the likelihood (this subset will be appended to random with Laplace approximation disabled).
parameters	list of fixed and random effects, e.g., as constructed by dsem and then modified by hand (only helpful for advanced users to change starting values or restart at intended values)
map	list of fixed and mirrored parameters, constructed by dsem by default but avail- able to override this default and then pass to MakeADFun
getJointPrecis	
	whether to get the joint precision matrix. Passed to sdreport.
extra_converge	nce_checks Boolean indicating whether to run extra checks on model convergence.

list_parameters

lower	vectors of lower bounds, replicated to be as long as start and passed to nlminb. If unspecified, all parameters are assumed to be unconstrained.
upper	vectors of upper bounds, replicated to be as long as start and passed to nlminb. If unspecified, all parameters are assumed to be unconstrained.

Value

An S3 object of class "dsem_control" that specifies detailed model settings, allowing user specification while also specifying default values

isle_royale

Isle Royale wolf and moose

Description

Data used to demonstrate and test cross-lagged (vector autoregressive) models

Usage

data(isle_royale)

Details

Data extracted from file "Data_wolves_moose_Isle_Royale_June2019.csv" available at https://www.isleroyalewolf.org and obtained 2023-06-23. Reproduced with permission from John Vucetich, and generated by the Wolves and Moose of Isle Royale project.

References

Vucetich, JA and Peterson RO. 2012. The population biology of Isle Royale wolves and moose: an overview. https://www.isleroyalewolf.org

list_parameters List fixed and random effects

Description

list_parameters lists all fixed and random effects

Usage

list_parameters(Obj, verbose = TRUE)

Arguments

Obj	Compiled TMB object
verbose	Boolean, whether to print messages to terminal

logLik.dsem

Value

Tagged-list of fixed and random effects, returned invisibly and printed to screen

logLik.dsem Marginal log-likelihood

Description

Extract the (marginal) log-likelihood of a dsem model

Usage

S3 method for class 'dsem'
logLik(object, ...)

Arguments

object	Output from dsem
	Not used

Value

object of class logLik with attributes

val	log-likelihood
df	number of parameters

Returns an object of class logLik. This has attributes "df" (degrees of freedom) giving the number of (estimated) fixed effects in the model, abd "val" (value) giving the marginal log-likelihood. This class then allows AIC to work as expected.

loo_residuals Calculate leave-one-out residuals

Description

Calculates quantile residuals using the predictive distribution from a jacknife (i.e., leave-one-out predictive distribution)

Usage

```
loo_residuals(
   object,
   nsim = 100,
   what = c("quantiles", "samples", "loo"),
   track_progress = TRUE,
   ...
)
```

Arguments

object	Output from dsem
nsim	Number of simulations to use if family!="fixed" for some variable, such that simulation residuals are required.
what	whether to return quantile residuals, or samples from the leave-one-out predic- tive distribution of data, or a table of leave-one-out predictions and standard errors for the latent state
track_progress	whether to track runtimes on terminal
	Not used

Details

Conditional quantile residuals cannot be calculated when using family = "fixed", because statevariables are fixed at available measurements and hence the conditional distribution is a Dirac delta function. One alternative is to use leave-one-out residuals, where we calculate the predictive distribution for each state value when dropping the associated observation, and then either use that as the predictive distribution, or sample from that predictive distribution and then calculate a standard quantile distribution for a given non-fixed family. This appraoch is followed here. It is currently only implemented when all variables follow family = "fixed", but could be generalized to a mix of families upon request.

Value

A matrix of residuals, with same order and dimensions as argument tsdata that was passed to dsem.

make_dfa	Make text for dynamic factor analysis	
----------	---------------------------------------	--

Description

Make the text string for a dynamic factor analysis expressed using arrow-and-lag notation for DSEM.

Usage

```
make_dfa(variables, n_factors, factor_names = paste0("F", seq_len(n_factors)))
```

Arguments

variables	Character string of variables (i.e., column names of tsdata).
n_factors	Number of factors.
factor_names	Optional character-vector of factor names, which must match NA columns in tsdata.

Value

A text string to be passed to dsem

make_dsem_ram

Description

make_dsem_ram converts SEM arrow notation to ram describing SEM parameters

Usage

```
make_dsem_ram(
  sem,
  times,
  variables,
  covs = variables,
  quiet = FALSE,
  remove_na = TRUE
)
```

Arguments

sem	Specification for time-series structural equation model structure including lagged or simultaneous effects. See Details section in make_dsem_ram for more de- scription	
times	A character vector listing the set of times in order	
variables	A character vector listing the set of variables	
COVS	A character vector listing variables for which to estimate a standard deviation	
quiet	Boolean indicating whether to print messages to terminal	
remove_na	Boolean indicating whether to remove NA values from RAM (default) or not. remove_NA=FALSE might be useful for exploration and diagnostics for advanced users	

Details

RAM specification using arrow-and-lag notation

Each line of the RAM specification for make_dsem_ram consists of four (unquoted) entries, separated by commas:

1. Arrow specification: This is a simple formula, of the form A -> B or, equivalently, B <- A for a regression coefficient (i.e., a single-headed or directional arrow); A <-> A for a variance or A <-> B for a covariance (i.e., a double-headed or bidirectional arrow). Here, A and B are variable names in the model. If a name does not correspond to an observed variable, then it is assumed to be a latent variable. Spaces can appear freely in an arrow specification, and there can be any number of hyphens in the arrows, including zero: Thus, e.g., A->B, A --> B, and A>B are all legitimate and equivalent.

- 2. Lag (using positive values): An integer specifying whether the linkage is simultaneous (lag=0) or lagged (e.g., X -> Y, 1, XtoY indicates that X in time T affects Y in time T+1), where only one-headed arrows can be lagged. Using positive values to indicate lags then matches the notational convention used in package dynlm.
- **3. Parameter name:** The name of the regression coefficient, variance, or covariance specified by the arrow. Assigning the same name to two or more arrows results in an equality constraint. Specifying the parameter name as NA produces a fixed parameter.
- **4. Value:** start value for a free parameter or value of a fixed parameter. If given as NA (or simply omitted), the model is provide a default starting value.

Lines may end in a comment following #. The function extends code copied from package 'sem' under licence GPL (>= 2) with permission from John Fox.

Simultaneous autoregressive process for simultaneous and lagged effects

This text then specifies linkages in a multivariate time-series model for variables **X** with dimensions $T \times C$ for T times and C variables. make_dsem_ram then parses this text to build a path matrix **P** with dimensions $TC \times TC$, where element ρ_{k_2,k_1} represents the impact of x_{t_1,c_1} on x_{t_2,c_2} , where $k_1 = Tc_1 + t_1$ and $k_2 = Tc_2 + t_2$. This path matrix defines a simultaneous equation

$$\operatorname{vec}(\mathbf{X}) = \mathbf{P}\operatorname{vec}(\mathbf{X}) + \operatorname{vec}(\mathbf{\Delta})$$

where Δ is a matrix of exogenous errors with covariance $\mathbf{V} = \Gamma \Gamma^t$, where Γ is the Cholesky of exogenous covariance. This simultaneous autoregressive (SAR) process then results in \mathbf{X} having covariance:

$$\operatorname{Cov}(\mathbf{X}) = (\mathbf{I} - \mathbf{P})^{-1} \mathbf{\Gamma} \mathbf{\Gamma}^{t} ((\mathbf{I} - \mathbf{P})^{-1})^{t}$$

Usefully, computing the inverse-covariance (precision) matrix $\mathbf{Q} = \mathbf{V}^{-1}$ does not require inverting $(\mathbf{I} - \mathbf{P})$:

$$\mathbf{Q} = (\mathbf{\Gamma}^{-1}(\mathbf{I} - \mathbf{P}))^t \mathbf{\Gamma}^{-1}(\mathbf{I} - \mathbf{P})$$

Example: univariate first-order autoregressive model

This simultaneous autoregressive (SAR) process across variables and times allows the user to specify both simutanous effects (effects among variables within year T) and lagged effects (effects among variables among years T). As one example, consider a univariate and first-order autoregressive process where T = 4. with independent errors. This is specified by passing sem = "X -> X, 1, rho \n X <-> X, 0, sigma" to make_dsem_ram. This is then parsed to a RAM:

heads	to	from	paarameter	start
1	2	1	1	<na></na>
1	3	2	1	<na></na>
1	4	3	1	<na></na>
2	1	1	2	<na></na>
2	2	2	2	<na></na>
2	3	3	2	<na></na>
2	4	4	2	<na></na>

Rows of this RAM where heads=1 are then interpreted to construct the path matrix **P**, where column "from" in the RAM indicates column number in the matrix, column "to" in the RAM indicates row number in the matrix:

$$\mathbf{P} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ \rho & 0 & 0 & 0 \\ 0 & \rho & 0 & 0 \\ 0 & 0 & \rho & 0 \end{bmatrix}$$

While rows where heads=2 are interpreted to construct the Cholesky of exogenous covariance Γ and column "parameter" in the RAM associates each nonzero element of those two matrices with an element of a vector of estimated parameters:

$$\mathbf{\Gamma} = \begin{bmatrix} \sigma & 0 & 0 & 0 \\ 0 & \sigma & 0 & 0 \\ 0 & 0 & \sigma & 0 \\ 0 & 0 & 0 & \sigma \end{bmatrix}$$

with two estimated parameters $\beta = (\rho, \sigma)$. This then results in covariance:

$$\operatorname{Cov}(\mathbf{X}) = \sigma^{2} \begin{bmatrix} 1 & \rho^{1} & \rho^{2} & \rho^{3} \\ \rho^{1} & 1 + \rho^{2} & \rho^{1}(1 + \rho^{2}) & \rho^{2}(1 + \rho^{2}) \\ \rho^{2} & \rho^{1}(1 + \rho^{2}) & 1 + \rho^{2} + \rho^{4} & \rho^{1}(1 + \rho^{2} + \rho^{4}) \\ \rho^{3} & \rho^{2}(1 + \rho^{2}) & \rho^{1}(1 + \rho^{2} + \rho^{4}) & 1 + \rho^{2} + \rho^{4} + \rho^{6} \end{bmatrix}$$

Which converges on the stationary covariance for an AR1 process for times t >> 1:

$$\operatorname{Cov}(\mathbf{X}) = \frac{\sigma^2}{1+\rho^2} \begin{bmatrix} 1 & \rho^1 & \rho^2 & \rho^3 \\ \rho^1 & 1 & \rho^1 & \rho^2 \\ \rho^2 & \rho^1 & 1 & \rho^1 \\ \rho^3 & \rho^2 & \rho^1 & 1 \end{bmatrix}$$

except having a lower pointwise variance for the initial times, which arises as a "boundary effect".

Similarly, the arrow-and-lag notation can be used to specify a SAR representing a conventional structural equation model (SEM), cross-lagged (a.k.a. vector autoregressive) models (VAR), dy-namic factor analysis (DFA), or many other time-series models.

Value

A reticular action module (RAM) describing dependencies

Examples

```
# Univariate AR1
sem = "
    X -> X, 1, rho
    X <-> X, 0, sigma
"
make_dsem_ram( sem=sem, variables="X", times=1:4 )
```

```
# Univariate AR2
sem = "
  X -> X, 1, rho1
  X -> X, 2, rho2
 X <-> X, 0, sigma
,,
make_dsem_ram( sem=sem, variables="X", times=1:4 )
# Bivariate VAR
sem = "
  X -> X, 1, XtoX
 X -> Y, 1, XtoY
  Y -> X, 1, YtoX
  Y -> Y, 1, YtoY
 X <-> X, 0, sdX
 Y <-> Y, 0, sdY
make_dsem_ram( sem=sem, variables=c("X","Y"), times=1:4 )
# Dynamic factor analysis with one factor and two manifest variables
# (specifies a random-walk for the factor, and miniscule residual SD)
sem = "
  factor -> X, 0, loadings1
  factor -> Y, 0, loadings2
  factor -> factor, 1, NA, 1
  X <-> X, 0, NA, 0.01
                             # Fix at negligible value
  Y <-> Y, 0, NA, 0.01
                             # Fix at negligible value
make_dsem_ram( sem=sem, variables=c("X","Y","factor"), times=1:4 )
# ARIMA(1,1,0)
sem = "
  factor -> factor, 1, rho1 # AR1 component
  X -> X, 1, NA, 1
                            # Integrated component
  factor -> X, 0, NA, 1
                            # Fix at negligible value
  X <-> X, 0, NA, 0.01
,,
make_dsem_ram( sem=sem, variables=c("X","factor"), times=1:4 )
# ARIMA(0,0,1)
sem = "
  factor -> X, 0, NA, 1
  factor -> X, 1, rho1
                        # MA1 component
 X <-> X, 0, NA, 0.01
                        # Fix at negligible value
make_dsem_ram( sem=sem, variables=c("X","factor"), times=1:4 )
```

make_matrices Make path matrices

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parse_path

Description

Constructs path matrices for dynamic structural equation model (DSEM) using a vector of parameters and specification of the DSEM

Usage

make_matrices(beta_p, model, times, variables)

Arguments

beta_p	vector parameters.	
model matrix or data.frame with the following columns, and one row per one-he or two-headed arrow in the dynamic structural model:		
	direction whether a path coefficient is one-headed (1) or two-headed (2)	
	lag whether the lag associated with a given coefficient	
start starting value, used when parameter=0		
	parameter The parameter number from beta_p associated with a given path	
	first The variable at the tail of a given path	
	second The variable at the head of a given path	
times	integer-vector of times to use when defining matrices	
variables	character-vector listing variables	

Details

When length(times) is T and length(variables) is J, make_matrices returns matrices of dimension $TJ \times TJ$ representing paths among $vec(\mathbf{X})$ where matrix \mathbf{X} has dimension $T \times J$ and vec stacks columns into a single long vector

Value

A named list of matrices including:

P_kk The matrix of interactions, i.e., one-headed arrows

G_kk The matrix of exogenous covariance, i.e., two-headed arrows

parse_path Parse path

Description

parse_path is copied from sem::parse.path

Usage

parse_path(path)

Arguments

path

Details

Copied from package 'sem' under licence GPL (>= 2) with permission from John Fox

Value

Tagged-list defining variables and direction for a specified path coefficient

plot.dsem Simulate dsem

text to parse

Description

Plot from a fitted dsem model

Usage

```
## S3 method for class 'dsem'
plot(
    x,
    y,
    edge_label = c("name", "value", "value_and_stars"),
    digits = 2,
    style = c("igraph", "ggraph"),
    ...
)
```

Arguments

х	Output from dsem
У	Not used
edge_label	Whether to plot parameter names, estimated values, or estimated values along with stars indicating significance at 0.05, 0.01, or 0.001 levels (based on two-sided Wald tests)
digits	integer indicating the number of decimal places to be used
style	Whether to make a graph using igraph or ggraph
	arguments passed to plot.igraph

Details

This function coerces output from a graph and then plots the graph.

predict.dsem

Value

Invisibly returns the output from graph_from_data_frame which was passed to plot.igraph for plotting.

predict.dsem predictions using dsem

Description

Predict variables given new (counterfactual) values of data, or for future or past times

Usage

```
## S3 method for class 'dsem'
predict(object, newdata = NULL, type = c("link", "response"), ...)
```

Arguments

object	Output from dsem
newdata	optionally, a data frame in which to look for variables with which to predict. If omitted, the fitted data are used to create predictions. If desiring predictions after the fitted data, the user must append rows with NAs for those future times. Sim- ilarly, if desiring predictions given counterfactual values for time-series data, then those individual observations can be edited while keeping other observa- tions at their original fitted values.
type	the type of prediction required. The default is on the scale of the linear predic- tors; the alternative "response" is on the scale of the response variable. Thus for a Poisson-distributed variable the default predictions are of log-intensity and type = "response" gives the predicted intensity.
	Not used

Value

A matrix of predicted values with dimensions and order corresponding to argument newdata is provided, or tsdata if not. Predictions are provided on either link or response scale, and are generated by re-optimizing random effects condition on MLE for fixed effects, given those new data.

print.dsem

Description

Prints output from fitted dsem model

Usage

S3 method for class 'dsem'
print(x, ...)

Arguments

х	Output from dsem
	Not used

Value

No return value, called to provide clean terminal output when calling fitted object in terminal.

read_model

Make a RAM (Reticular Action Model)

Description

read_model converts SEM arrow notation to model describing SEM parameters

Usage

```
read_model(sem, times, variables, covs = NULL, quiet = FALSE)
```

Arguments

sem	Specification for time-series structural equation model structure including lagged or simultaneous effects. See Details section in make_dsem_ram for more de- scription
times	A character vector listing the set of times in order
variables	A character vector listing the set of variables
COVS	A character vector listing variables for which to estimate a standard deviation
quiet	Boolean indicating whether to print messages to terminal

Details

See make_dsem_ram for details

residuals.dsem Calculate residuals

Description

Calculate deviance or response residuals for dsem

Usage

```
## S3 method for class 'dsem'
residuals(object, type = c("deviance", "response"), ...)
```

Arguments

object	Output from dsem
type	which type of residuals to compute (only option is "deviance" or "response" for now)
	Not used

Value

A matrix of residuals, with same order and dimensions as argument tsdata that was passed to dsem.

sea_otter

Sea otter trophic cascade

Description

Data used to demonstrate and test trophic cascades options

Usage

data(sea_otter)

simulate.dsem Simulate dsem

Description

Simulate from a fitted dsem model

Usage

```
## S3 method for class 'dsem'
simulate(
   object,
   nsim = 1,
   seed = NULL,
   variance = c("none", "random", "both"),
   resimulate_gmrf = FALSE,
   fill_missing = FALSE,
   ...
)
```

Arguments

object	Output from dsem
nsim	number of simulated data sets
seed	random seed
variance	whether to ignore uncertainty in fixed and random effects, include estimation uncertainty in random effects, or include estimation uncertainty in both fixed and random effects
resimulate_gmrf	
	whether to resimulate the GMRF based on estimated or simulated random effects (determined by argument variance)
fill_missing	whether to fill in simulate all data (including values that are missing in the orig- inal data set)
	Not used

Details

This function conducts a parametric bootstrap, i.e., simulates new data conditional upon estimated values for fixed and random effects. The user can optionally simulate new random effects conditional upon their estimated covariance, or simulate new fixed and random effects conditional upon their imprecision.

Note that simulate will have no effect on states x_tj for which there is a measurement and when those measurements are fitted using family="fixed", unless resimulate_gmrf=TRUE. In this latter case, the GMRF is resimulated given estimated path coefficients

Value

Simulated data, either from obj\$simulate where obj is the compiled TMB object, first simulating a new GMRF and then calling obj\$simulate.

stepwise_selection Simulate dsem

Description

Plot from a fitted dsem model

Usage

```
stepwise_selection(
  model_options,
  model_shared,
  options_initial = c(),
  quiet = FALSE,
   criterion = AIC,
   ...
)
```

Arguments

model_options	character-vector containing sem elements that could be included or dropped depending upon their parsimony
model_shared	character-vector containing sem elements that must be included regardless of parsimony
options_initial	
	character-vector containing some (possible empty) subset of model_options, where stepwise selection begins with that set of model options included.
quiet	whether to avoid displaying progress to terminal
criterion	function that computes the information criterion to be minimized, typically using AIC. However, users can instead supply a function that computes CIC using test_dsep and desired settings, presumably including a set.seed if missing data are being imputed
	arguments passed to dsem, other than sem e.g., tsdata, family etc.

Details

This function conducts stepwise (i.e., forwards and backwards) model selection using marginal AIC, while forcing some model elements to be included and selecting among others.

Value

An object (list) that includes:

model the string with the selected SEM model

record a list showing the AIC and whether each model_options is included or not

Examples

```
# Simulate x -> y -> z
set.seed(101)
x = rnorm(100)
y = 0.5 * x + rnorm(100)
z = 1*y + rnorm(100)
tsdata = ts(data.frame(x=x, y=y, z=z))
# define candidates
model_options = c(
  "y -> z, 0, y_to_z",
  "x -> z, 0, x_to_z"
)
# define paths that are required
model_shared = "
 x -> y, 0, x_to_y
,,
# Do selection
step = stepwise_selection(
  model_options = model_options,
  model_shared = model_shared,
  tsdata = tsdata,
  quiet = TRUE
)
# Check selected model
cat(step$model)
```

summary.dsem summarize dsem

Description

summarize parameters from a fitted dynamic structural equation model

Usage

```
## S3 method for class 'dsem'
summary(object, ...)
```

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summary.dsem

Arguments

object	Output from dsem
	Not used

Details

A DSEM is specified using "arrow and lag" notation, which specifies the set of path coefficients and exogenous variance parameters to be estimated. Function dsem then estimates the maximum likelihood value for those coefficients and parameters by maximizing the log-marginal likelihood. Standard errors for parameters are calculated from the matrix of second derivatives of this log-marginal likelihood (the "Hessian matrix").

However, many users will want to associate individual parameters and standard errors with the path coefficients that were specified using the "arrow and lag" notation. This task is complicated in models where some path coefficients or variance parameters are specified to share a single value a priori, or were assigned a name of NA and hence assumed to have a fixed value a priori (such that these coefficients or parameters have an assigned value but no standard error). The summary function therefore compiles the MLE for coefficients (including duplicating values for any path coefficients that assigned the same value) and standard error estimates, and outputs those in a table that associates them with the user-supplied path and parameter names. It also outputs the z-score and a p-value arising from a two-sided Wald test (i.e. comparing the estimate divided by standard error against a standard normal distribution).

Value

Returns a data.frame summarizing estimated path coefficients, containing columns:

path The parsed path coefficient
lag The lag, where e.g. 1 means the predictor in time t effects the response in time t+1
name Parameter name
start Start value if supplied, and NA otherwise
parameter Parameter number
first Variable in path treated as predictor
second Variable in path treated as response
direction Whether the path is one-headed or two-headed
Estimate Maximum likelihood estimate
Std_Error Estimated standard error from the Hessian matrix
z_value Estimate divided by Std_Error
p_value P-value associated with z_value using a two-sided Wald test

test_dsep

Description

Calculate the p-value for a test of d-separation (Experimental)

Usage

```
test_dsep(
  object,
  n_time = NULL,
  n_burnin = NULL,
  what = c("pvalue", "CIC", "all"),
  test = c("wald", "lr"),
  seed = 123456,
  order = NULL,
  impute_data = c("by_test", "single", "none")
)
```

Arguments

object	object from dsem
n_time	how many times to include when defining the set of conditional independence relationships. If missing, this value is taken from the maximum lag that's in- cluded in the model plus one.
n_burnin	how many times to include prior to $seq_len(n_time)$ when identifying the conditioning set that must be included when defining conditional independence relationships.
what	whether to just get the p-value, an information criterion based on the condi- tional independence test, or a named list with these two and other intermediate calculations (used for diagnosing test behavior)
test	whether to test each conditional-independence relationship using a (univariate) wald test or a (multivariate) likelihood ratio test. The likelihood-ratio test might be more accurate given estimation covariance and also faster (does not require standard errors), but also is not used by phylopath and therefore less supported by previous d-dsep testing applications.
seed	random number seed used when simulating imputed data, so that results are reproducible.
order	an optional character vector providing the order for variables to be tested when defining the directed acyclic graph for use in d-sep testing
impute_data	whether to independently impute missing data for each conditional indepen- dence test, or to use imputed values from the original fit. The data are imputed separately for each conditional independence test, so that they are uncorrelated as expected when combining them using Fisher's method. Preliminary testing suggests that using imputed data improves test performance

test_dsep

Details

A user-specified SEM implies a set of conditional independence relationships among variables, which can be fitted individually, extracting the slope and associated p-value, and then combining these p-values to define a model-wide (omnibus) p-value for the hypothesis that a given data set arises from the specified model. This test is modified from package:phylopath. However it is unclear exactly how to define the set of conditional-independence assumptions in a model with temporal autocorrelation, and the test was not developed for uses when data are missing. At the time of writing, the function is hightly experimental.

Note that the method is not currently designed to deal with two-headed arrows among variables (i.e., exogenous covariance).

Value

A p-value representing the weight of evidence that the data arises from the specified model, where a low p-value indicates significant evidence for rejecting this hypothesis.

References

Shipley, B. (2000). A new inferential test for path models based on directed acyclic graphs. Structural Equation Modeling, 7(2), 206-218. doi:10.1207/S15328007SEM0702_4

Examples

```
# Simulate data set
set.seed(101)
a = rnorm(100)
b = 0.5 * a + rnorm(100)
c = 1*a + rnorm(100)
d = 1*b - 0.5*c + rnorm(100)
tsdata = ts(data.frame(a=a, b=b, c=c, d=d))
# fit wrong model
wrong = dsem(
  tsdata = tsdata,
  sem = "
   a -> d, 0, a_to_d
   b -> d, 0, b_to_d
   c -> d, 0, c_to_d
)
test_dsep( wrong )
# fit right model
right = dsem(
  tsdata = tsdata,
  sem = "
   a -> b, 0, a_to_b
   a -> c, 0, a_to_c
   b -> d, 0, b_to_d
   c -> d, 0, c_to_d
```

```
)
test_dsep( right )
```

TMBAIC

Calculate marginal AIC for a fitted model

Description

TMBAIC calculates AIC for a given model fit

Usage

TMBAIC(opt, k = 2, n = Inf)

Arguments

opt	the output from nlminb or optim
k	the penalty on additional fixed effects (default=2, for AIC)
n	the sample size, for use in AICc calculation (default=Inf, for which AICc=AIC)

Value

AIC, where a parsimonious model has a AIC relative to other candidate models

|--|

Description

Calculate a data frame of total effects, representing the estimated effect of every variable on every other variable and any time-lag from 0 (simultaneous effects) to a user-specified maximum lag.

Usage

```
total_effect(object, n_lags = 4)
```

Arguments

object	Output from dsem
n_lags	Number of lags over which to calculate total effects

Details

Total effects are taken from the Leontief matrix $(\mathbf{I} - \mathbf{P})^{-1}$, where \mathbf{P} is the path matrix across variables and times. This calculates the effect of a pulse perturbation at lag=0 for a given variable (from) upon any other variable (to) either in the same time (lag=0), or subsequent times (lag >= 1).

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vcov.dsem

Value

A data frame listing the time-lag (lag), variable that is undergoing some exogenous change (from), and the variable being impacted (to), along with the total effect (total_effect) including direct and indirect pathways, and the partial "direct" effect (direct_effect)

Examples

```
# Define linear model with slope of 0.5
sem = "
  # from, to, lag, name, starting_value
  x -> y, 0, slope, 0.5
..
# Build DSEM with specified value for path coefficients
mod = dsem(
  sem = sem,
  tsdata = ts(data.frame(x=rep(0,20),y=rep(0,20))),
  control = dsem_control( run_model = FALSE )
)
# Show that total effect of X on Y is 0.5 but does not propagate over time
total_effect(mod, n_lags = 2)
# Define linear model with slope of 0.5 and autocorrelated response
sem = "
  x -> y, 0, slope, 0.5
  y -> y, 1, ar_y, 0.8
mod = dsem(
  sem = sem,
  tsdata = ts(data.frame(x=rep(0,20),y=rep(0,20))),
  control = dsem_control( run_model = FALSE )
)
# Show that total effect of X on Y is 0.5 with decay of 0.8 for each time
total_effect(mod, n_lags = 4)
```

vcov.dsem

Extract Variance-Covariance Matrix

Description

extract the covariance of fixed effects, or both fixed and random effects.

Usage

```
## S3 method for class 'dsem'
vcov(object, which = c("fixed", "random", "both"), ...)
```

vcov.dsem

Arguments

object	output from dsem
which	whether to extract the covariance among fixed effects, random effects, or both
	ignored, for method compatibility

Value

A square matrix containing the estimated covariances among the parameter estimates in the model. The dimensions dependend upon the argument which, to determine whether fixed, random effects, or both are outputted.

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