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Maintainer Shangkun Wang <shangkunwang01@gmail.com>

Description Construct various types of space-filling designs, including Latin hypercube designs, clustering-based designs, maximin designs, maximum projection designs, and uniform designs (Joseph 2016 <doi:10.1080/08982112.2015.1100447>). It also offers the option to optimize designs based on user-defined criteria. This work is supported by U.S. National Science Foundation grant DMS-2310637.

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Author Shangkun Wang [aut, cre], Roshan Joseph [aut]

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SFDesign-package Space-Filling designs

Description

This pacakge offers a comprehensive suite of functions to construct various types of space-filling designs, including Latin hypercube designs, clustering-based designs, maximum projection designs, and uniform designs (Joseph 2016). It also offers the option to optimize designs based on user-defined criteria.

Author(s)

Shangkun Wang, V. Roshan Joseph

Maintainer: Shangkun Wang <shangkunwang01@gmail.com>

References

Wang, Shangkun, Xie, Weijun and V. Roshan Joseph. SFDesign: An R package for Space-Filling Designs.

Joseph, V. R. (2016). Space-filling designs for computer experiments: A review. Quality Engineering, 28(1), 28-35. cluster.error Clustering error

Description

This function computes the clustering error.

Usage

```
cluster.error(design, X = NULL, alpha = 1)
```

Arguments

design	a design matrix.
х	candidate points in $[0,1]^p. \ {\rm If} \ {\rm X}$ is not provided, Sobol points are generated as candidate points.
alpha	power of the Euclidean distance.

Details

cluster.error computes the clustering error. The clustering error for a design $D = [x_1, \ldots, x_n]^T$ is defined as $\frac{1}{N} \sum_{i=1}^n \sum_{x \in V_i} ||x - x_i||^{\alpha}$, where V_i is the Voronoi cell of each design point x_i for $i = 1, \ldots, n$, N is the size of X. When $\alpha = 2$, we obtain K-means and when $\alpha = 1$, we obtain K-medians.

Value

clustering error of the design.

```
n = 20
p = 3
D = randomLHD(n, p)
cluster.error(D)
```

clustering.design Designs generated by clustering algorithms

Description

This function is for producing designs by minimizing the clustering error.

Usage

```
clustering.design(
   n,
   p,
   X = NULL,
   D.ini = NULL,
   multi.start = 1,
   alpha = 1,
   Lloyd.iter.max = 100,
   cen.iter.max = 10,
   Lloyd.tol = 1e-04,
   cen.tol = 1e-04
)
```

Arguments

n	design size.
р	design dimension.
Х	candidate points in $[0,1]^p$. If X is not provided, Sobol points is generated as cluster points.
D.ini	initial design points. If D.ini is not provided, Sobol points are generated as initial design.
multi.start	number of starting designs (cluster centers).
alpha	power of the Euclidean distance.
Lloyd.iter.max	maximum number of iterations for the Lloyd algorithm.
cen.iter.max	maximum number of iterations for the center calculation for each cluster.
Lloyd.tol	minimum relative change for the Lloyd algorithm to continue.
cen.tol	minimum relative change for the center calculation algorithm to continue.

Details

clustering.design produces a design by clustering algorithms. It minimize the clustering error (see cluster.error) by Lloyd's algorithm. When $\alpha > 2$, accelerated gradient descent is used to find the center for each cluster (Mak, S. and Joseph, V. R. 2018). When $\alpha \le 2$: Weizfeld algorithm is used to find the center for each cluster. Let $x_i^{(0)} = x_i$ denote the initial position of the *i*th center and and let S_i represent the points within its Voronoi cell. The center is then updated as: $x_i^{(k+1)} = \left(\sum_{s \in S_i} \frac{s}{\|s - x_i^{(k)}\|_2^{2-\alpha}}\right) / \left(\sum_{s \in S_i} \frac{1}{\|s - x_i^{(k)}\|_2^{2-\alpha}}\right) \quad \text{for } k = 0, 1, \ldots$

continuous.optim

Value

design	final design points.
cluster	cluster assignment for each cluster points.
cluster.error	final cluster error.

References

Mak, S. and Joseph, V. R. (2018), "Minimax and minimax projection designs using clustering," Journal of Computational and Graphical Statistics, 27, 166–178.

Examples

```
n = 20
p = 3
X = spacefillr::generate_sobol_set(1e5*p, p)
D = clustering.design(n, p, X)
```

continuous.optim Continuous optimization of a design

Description

This function does continuous optimization of an existing design based on a specified criterion. It has an option to run simulated annealing after the continuous optimization.

Usage

```
continuous.optim(
  D.ini,
  objective,
  gradient = NULL,
  iteration = 10,
  sa = FALSE,
  sa.objective = NULL
)
```

D.ini	initial design matrix.
objective	the criterion to minimize for the design. It can also return gradient information at the same time in a list with elements "objective" and "gradient".
gradient	the gradient of the objective with respect to the design.
iteration	number iterations for LBFGS.
sa	whether to use simulated annealing. If the final criterion is different from the objective function specified above, simulated annealing can be useful. Use this option only when the design size and dimension are not large.
sa.objective	the criterion to minimize for the simulated annealing.

continuous.optim optimizes an existing design based on a specified criterion. It is a wrapper for the L-BFGS-B function from the nloptr packakge (Johnson 2008) and/or GenSA function in GenSA package (Xiang, Gubian, Suomela and Hoeng 2013).

Value

the optimized design.

References

Johnson, S. G. (2008), The NLopt nonlinear-optimization package, available at https://github.com/stevengj/nlopt. Xiang Y, Gubian S, Suomela B, Hoeng (2013). "Generalized Simulated Annealing for Efficient Global Optimization: the GenSA Package for R". The R Journal Volume 5/1, June 2013.

```
# Below is an example showing how to create functions needed to generate MaxPro design manually by
# continuous.optim without using the maxpro.optim function in the package.
compute.distance.matrix <- function(A){</pre>
   log_prod_metric = function(x, y) 2 * sum(log(abs(x-y)))
   return (c(proxy::dist(A, log_prod_metric)))
}
optim.obj = function(x){
  D = matrix(x, nrow=n, ncol=p)
  d = exp(compute.distance.matrix(D))
  d_matrix = matrix(0, n, n)
  d_matrix[lower.tri(d_matrix)] = d
  d_matrix = d_matrix + t(d_matrix)
  fn = sum(1/d)
  lfn = log(fn)
  I = diag(n)
  diag(d_matrix) = rep(1,n)
  A = B = D
  for(j in 1:p)
  {
   A = t(outer(D[,j], D[,j], "-"))
   diag(A) = rep(1, n)
   B[, j] = diag((1/A - I) %*% (1/d_matrix - I))
  }
  grad = 2 * B / fn
  return(list("objective"=lfn, "gradient"=grad))
}
n = 20
p = 3
D.ini = maxproLHD(n, p)$design
D = continuous.optim(D.ini, optim.obj)
```

 ${\tt customLHD}$

Description

This function generates a LHD by minimizing a user-specified design criterion.

Usage

```
customLHD(
  compute.distance.matrix,
 compute.criterion,
 update.distance.matrix,
 n,
 р,
  design = NULL,
 max.sa.iter = 1e+06,
  temp = 0,
  decay = 0.95,
  no.update.iter.max = 400,
  num.passes = 10,
 max.det.iter = 1e+06,
 method = "full",
  scaled = TRUE
)
```

compute.distance.matrix			
	a function to calculate pairwise distance		
compute.criteri	on		
	a function to calculate the criterion based on the pairwise distance		
update.distance	.matrix		
	a function to update the distance matrix after swapping one column of two design points		
n	design size.		
р	design dimension.		
design	an initial LHD. If design=NULL, a random LHD is generated.		
max.sa.iter	maximum number of swapping involved in the simulated annealing (SA) algorithm.		
temp	initial temperature of the simulated annealing algorithm. If temp=0, it will be automatically determined.		
decay	the temperature decay rate of simulated annealing.		

no.update.iter.max				
	the maximum number of iterations where there is no update to the global optimum before SA stops.			
num.passes	the maximum number of passes of the whole design matrix if deterministic swapping is used.			
max.det.iter	maximum number of swapping involved in the deterministic swapping algorithm.			
method	choice of "deterministic", "sa", or "full". See details for the description of each choice.			
scaled	whether the design is scaled to unit hypercube. If scaled=FALSE, the design is represented by integer numbers from 1 to design size. Leave it as TRUE when no initial design is provided.			

customLHD generates a LHD by minimizing a user-specified design criterion.

- If method='sa', then a simulated annealing algorithm is used to optimize the LHD. To custom the optimization process, you can change the default values for max.sa.iter, temp, decay, no.update.iter.max. In this optimization step, two design points are randomly chosen and their coordinate along one dimension are swaped. If the new design improves the criterion, then it is accepted; otherwise, it is accepted with some probability.
- If method='deterministic', then a deterministic swap algorithm is used to optimize the LHD. To custom the optimization process, you can change the default values for num.passes, max.det.iter. In this optimization step, we swap the coordinates of all pairs of design points (start with design point 1 with design point 2, then 1 with 3, ... 1 with n, then 2 with 3 until n-1 with n). Only accept the change if the swap leads to an improvement.
- If method='full', then optimization goes through the above two stages.

Value

design	optimized LHD.
total.iter	total number of swaps in the optimization.
criterion	optimized criterion.
crit.hist	criterion history during the optimization process.

```
# Below is an example showing how to create functions needed to generate
# MaxPro LHD manually by customLHD without using the maxproLHD function in
# the package.
compute.distance.matrix <- function(A){
    s = 2
    log_prod_metric = function(x, y) s * sum(log(abs(x-y)))
    return (c(proxy::dist(A, log_prod_metric)))
}
compute.criterion <- function(n, p, d) {
    s = 2
```

```
dim <- as.integer(n * (n - 1) / 2)
 # Find the minimum distance
 Dmin < -min(d)
 # Compute the exponential summation
 avgdist <- sum(exp(Dmin - d))</pre>
 # Apply the logarithmic transformation and scaling
 avgdist <- log(avgdist) - Dmin</pre>
 avgdist <- exp((avgdist - log(dim)) * (p * s) ^ (-1))</pre>
 return(avgdist)
}
update.distance.matrix <- function(A, col, selrow1, selrow2, d) {</pre>
 s = 2
 n = nrow(A)
 # transform from c++ idx to r idx
 selrow1 = selrow1 + 1
 selrow2 = selrow2 + 1
 col = col + 1
 # A is the updated matrix
 row1 <- min(selrow1, selrow2)</pre>
 row2 <- max(selrow1, selrow2)</pre>
 compute_position <- function(row, h, n) {</pre>
   n*(h-1) - h*(h-1)/2 + row-h
 }
 # Update for rows less than row1
 if (row1 > 1) {
    for (h in 1:(row1-1)) {
      position1 <- compute_position(row1, h, n)</pre>
      position2 <- compute_position(row2, h, n)</pre>
      d[position1] <- d[position1] + s * log(abs(A[row1, col] - A[h, col])) -</pre>
          s * log(abs(A[row2, col] - A[h, col]))
      d[position2] <- d[position2] + s * log(abs(A[row2, col] - A[h, col])) -</pre>
          s * log(abs(A[row1, col] - A[h, col]))
    }
 }
 # Update for rows between row1 and row2
 if ((row2-row1) > 1){
    for (h in (row1+1):(row2-1)) {
      position1 <- compute_position(h, row1, n)</pre>
      position2 <- compute_position(row2, h, n)</pre>
      d[position1] <- d[position1] + s * log(abs(A[row1, col] - A[h, col])) -</pre>
          s * log(abs(A[row2, col] - A[h, col]))
      d[position2] <- d[position2] + s * log(abs(A[row2, col] - A[h, col])) -</pre>
          s * log(abs(A[row1, col] - A[h, col]))
   }
 }
 # Update for rows greater than row2
 if (row2 < n) {
    for (h in (row2+1):n) {
```

```
position1 <- compute_position(h, row1, n)</pre>
      position2 <- compute_position(h, row2, n)</pre>
      d[position1] <- d[position1] + s * log(abs(A[row1, col] - A[h, col])) -</pre>
          s * log(abs(A[row2, col] - A[h, col]))
      d[position2] <- d[position2] + s * log(abs(A[row2, col] - A[h, col])) -</pre>
          s * log(abs(A[row1, col] - A[h, col]))
    }
  }
  return (d)
}
n = 6
p = 2
# Find an appropriate initial temperature
crit1 = 1 / (n-1)
crit2 = (1 / ((n-1)^(p-1) * (n-2))) ^ (1/p)
delta = crit2 - crit1
temp = - delta / log(0.99)
result_custom = customLHD(compute.distance.matrix,
function(d) compute.criterion(n, p, d),
update.distance.matrix, n, p, temp = temp)
```

full.factorial Full factorial design

Description

This function generates a full factorial design.

Usage

```
full.factorial(p, level)
```

Arguments

р	design dimension.
level	an integer specifying the number of levels.

Details

full.factorial generates a p dimensional full factorial design.

Value

a full factorial design matrix (scaled to [0, 1])

maximin.augment

Examples

p = 3 level = 3 D = full.factorial(p, level)

maximin.augment	Augment a design by adding new design points that minimize the re-
	ciprocal distance criterion greedily

Description

This function augments a design by adding new design points one-at-a-time that minimize the reciprocal distance criterion.

Usage

```
maximin.augment(n, p, D.ini, candidate = NULL, r = 2 * p)
```

Arguments

n	the size of the final design.
р	design dimension.
D.ini	initial design.
candidate	candidate points to choose from. The default candidates are Sobol points of size 100n.
r	the power parameter in the maximin.crit. By default it is set as 2p.

Details

maximin.augment augments a design by adding new design points that minimize the reciprocal distance criterion (see maximin.crit) greedily. In each iteration, the new design points is selected as the one from the candidate points that has the smallest sum of reciprocal distance to the existing design, that is, $\boldsymbol{x}_{k+1} = \arg \min_{\boldsymbol{x}} \sum_{i=1}^{k} \frac{1}{\|\boldsymbol{x} - \boldsymbol{x}_i\|^{r}}$.

Value

the augmented design.

```
n.ini = 10
n = 20
p = 3
D.ini = maximinLHD(n.ini, p)$design
D = maximin.augment(n, p, D.ini)
```

maximin.crit

Description

This function calculates the maximin distance or the average reciprocal distance of a design.

Usage

```
maximin.crit(design, r = 2 * ncol(design), surrogate = FALSE)
```

Arguments

design	the design matrix.
r	the power used in the reciprocal distance objective function. The default value is set as twice the dimension of the design.
surrogate	whether to return the surrogate average reciprocal distance objective function or the maximin distance. If setting surrogate=TRUE, then the average reciprocal distance is returned.

Details

maximin.crit calculates the maximin distance or the average reciprocal distance of a design. The maximin distance for a design $D = [x_1, \ldots, x_n]^T$ is defined as $\phi_{Mm} = \min_{i \neq j} ||x_i - x_j||_2$. In optimization, the average reciprocal distance is usually used (Morris and Mitchell, 1995):

$$\phi_{\text{rec}} = \left(\frac{2}{n(n-1)} \sum_{i \neq j} \frac{1}{\|\boldsymbol{x}_i - \boldsymbol{x}_j\|_2^r}\right)^{1/r}$$

The r is a power parameter and when it is large enough, the reciprocal distance is similar to the exact maximin distance.

Value

the maximin distance or reciprocal distance of the design.

References

Morris, M. D. and Mitchell, T. J. (1995), "Exploratory designs for computational experiments," Journal of statistical planning and inference, 43, 381–402.

```
n = 20
p = 3
D = randomLHD(n, p)
maximin.crit(D)
```

maximin.optim

Description

This function optimizes a design by continuous optimization based on reciprocal distance criterion. A simulated annealing step can be enabled in the end to directly optimize the maximin distance criterion.

Usage

```
maximin.optim(D.ini, iteration = 10, sa = FALSE, find.best.ini = FALSE)
```

Arguments

D.ini	the initial design.
iteration	number iterations for L-BFGS-B algorithm.
sa	whether to use simulated annealing in the end. If sa=TRUE, continuous opti- mization is first used to optimize the reciprocal distance criterion and then SA is performed to optimize the maximin criterion.
find.best.ini	whether to generate other initial designs. If find.best.ini=TRUE, it will first find the closest full factorial design in terms of size to D.ini. If the size of the full factorial design is larger than D.ini, design points will be removed by the maximin.remove function. If the the size of the full factorial design is smaller than D.ini, then we will augment the design by maximin.augment. In this case, we have two different candidate set to choose from: one is a full factorial design with level+1 and another is Sobol points. All initial designs are optimized and the best is returned.

Details

maximin.optim optimizes a design by L-BFGS-B algorithm (Liu and Nocedal 1989) based on the reciprocal distance criterion. A simulated annealing step can be enabled in the end to directly optimize the maximin distance criterion. Optimization detail can be found in continuous.optim. We also provide the option to try other initial designs generated internally besides the D.ini provided by the user (see argument find.best.ini).

Value

design	the optimized design.
D.ini	initial designs. If find.best.ini=TRUE, a list will be returned containing all the
	initial designs considered.

References

Liu, D. C., & Nocedal, J. (1989). On the limited memory BFGS method for large scale optimization. Mathematical programming, 45(1), 503-528.

Examples

```
n = 20
p = 3
D = maximinLHD(n, p)$design
D = maximin.optim(D, sa=FALSE)$design
# D = maximin.optim(D, sa=TRUE)$design # Let sa=TRUE only when the n and p is not large.
```

maximin.remove	Sequentially remove design points from a design while maintaining
	low reciprocal distance criterion as possible

Description

This function sequentially removes design points one-at-a-time from a design while maintaining low reciprocal distance criterion as possible.

Usage

```
maximin.remove(D, n.remove, r = 2 * p)
```

Arguments

D	the design matrix.
n.remove	number of design points to remove.
r	the power parameter in the maximin.crit. By default it is set as 2p.

Details

maximin.remove sequentially removes design points from a design in a greedy way while maintaining low reciprocal distance criterion (see maximin.crit) as possible. In each iteration, the design point with the largest sum of reciprocal distances with the other design points is removed, that is, $k^* = \arg \max_k \sum_{i \neq k} \frac{1}{\|\boldsymbol{x}_k - \boldsymbol{x}_i\|^r}$.

Value

the updated design.

Examples

```
n = 20
p = 3
n.remove = 5
D = maximinLHD(n, p)$design
D = maximin.remove(D, n.remove)
```

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maximinLHD

Description

This function generates a LHD with large maximin distance.

Usage

```
maximinLHD(
    n,
    p,
    design = NULL,
    power = 2 * p,
    max.sa.iter = 1e+06,
    temp = 0,
    decay = 0.95,
    no.update.iter.max = 100,
    num.passes = 10,
    max.det.iter = 1e+06,
    method = "full",
    scaled = TRUE
)
```

n	design size.	
р	design dimension.	
design	an initial LHD. If design=NULL, a random LHD is generated.	
power	the power used in the maximin objective function.	
max.sa.iter	maximum number of swapping involved in the simulated annealing (SA) algorithm.	
temp	initial temperature of the simulated annealing algorithm. If temp=0, it will be automatically determined.	
decay	the temperature decay rate of simulated annealing.	
no.update.iter.max		
	the maximum number of iterations where there is no update to the global optimum before SA stops.	
num.passes	the maximum number of passes of the whole design matrix if deterministic swapping is used.	
max.det.iter	maximum number of swapping involved in the deterministic swapping algorithm.	
method	choice of "deterministic", "sa", or "full". If the method="full", the design is first optimized by SA and then deterministic swapping.	

scaled	whether the design is scaled to unit hypercube. If scaled=FALSE, the design is
	represented by integer numbers from 1 to design size. Leave it as TRUE when
	no initial design is provided.

maximinLHD generates a LHD or optimize an existing LHD to achieve large maximin distance by optimizing the reciprocal distance (see maximin.crit). The optimization details can be found in customLHD.

Value

design	final design points.
total.iter	total number of swaps in the optimization.
criterion	final optimized criterion.
crit.hist	criterion history during the optimization process.

Examples

```
# We show three different ways to use this function.
n = 20
p = 3
D.random = randomLHD(n, p)
# optimize over a random LHD by SA
D = maximinLHD(n, p, D.random, method='sa')
# optimize over a random LHD by deterministic swapping
D = maximinLHD(n, p, D.random, method='deterministic')
# Directly generate an optimized LHD for maximin criterion which goes
# through the above two optimization stages.
D = maximinLHD(n, p)
```

maxpro.crit

Maximum projection (MaxPro) criterion

Description

This function calculates the MaxPro criterion of a design.

Usage

maxpro.crit(design, delta = 0)

design	the design matrix.
delta	a small value added to the denominator of the maximum projection criterion. By default it is set as zero.

maxpro.optim

Details

maxpro.crit calculates the MaxPro criterion of a design. The MaxPro criterion for a design $D = [x_1, \ldots, x_n]^T$ is defined as

$$\left\{\frac{1}{\binom{n}{2}}\sum_{i=1}^{n-1}\sum_{j=i+1}^{n}\frac{1}{\prod_{l=1}^{p}(x_{il}-x_{jl})^{2}+\delta}\right\}^{1/p},$$

where p is the dimension of the design (Joseph, V. R., Gul, E., & Ba, S. 2015).

Value

the MaxPro criterion of the design.

References

Joseph, V. R., Gul, E., & Ba, S. (2015). Maximum projection designs for computer experiments. Biometrika, 102(2), 371-380.

Examples

```
n = 20
p = 3
D = randomLHD(n, p)
maxpro.crit(D)
```

maxpro.optim	$O_{1111111}/e$ u $uesign$	based on the maximum	
maxp: ereperm	optimize a debigit		projection criterion

Description

This function optimizes a design by continuous optimization based on maximum projection criterion (Joseph, V. R., Gul, E., & Ba, S. 2015).

Usage

```
maxpro.optim(D.ini, iteration = 10)
```

Arguments

D.ini	the initial design.
iteration	number iterations for L-BFGS-B.

Details

maxpro.optim optimizes a design by L-BFGS-B algorithm (Liu and Nocedal 1989) based on the maximum projection criterion maxpro.crit.

Value

design	optimized design.
D.ini	initial design.

References

Liu, D. C., & Nocedal, J. (1989). On the limited memory BFGS method for large scale optimization. Mathematical programming, 45(1), 503-528.

Joseph, V. R., Gul, E., & Ba, S. (2015). Maximum projection designs for computer experiments. Biometrika, 102(2), 371-380.

Examples

n = 20 p = 3 D = maxproLHD(n, p)\$design D = maxpro.optim(D)\$design

maxpro.remove	Sequentially remove design points from a design while maintaining
	low maximum projection criterion as possible

Description

This function sequentially removes design points one-at-a-time from a design while maintaining low maximum projection criterion as possible.

Usage

```
maxpro.remove(D, n.remove, delta = 0)
```

Arguments

D	design
n.remove	number of design points to remove
delta	a small value added to the denominator of the maximum projection criterion. By default it is set as zero.

Details

maxpro.remove sequentially removes design points from a design while maintaining low maximum projection criterion (see maxpro.crit) as possible. The maximum projection criterion is modified to include a small delta term:

$$\phi_{\text{maxpro}}(\boldsymbol{D}_n) = \left\{ \frac{1}{\binom{n}{2}} \sum_{i=1}^{n-1} \sum_{j=i+1}^n \frac{1}{\prod_{l=1}^p (x_{il} - x_{jl})^2 + \delta} \right\}^{1/p}.$$

maxproLHD

The index of the point to remove is $k^* = \arg \min_k \sum_{i \neq k} \frac{1}{\prod_{l=1}^p (x_{il} - x_{kl})^2 + \delta}$.

Value

the updated design.

Examples

```
n = 20
p = 3
n.remove = 5
D = maxproLHD(n, p)$design
D = maxpro.remove(D, n.remove)
```

maxproLHD

Generate a MaxPro Latin-hypercube design

Description

This function generates a MaxPro Latin-hypercube design.

Usage

```
maxproLHD(
   n,
   p,
   design = NULL,
   max.sa.iter = 1e+06,
   temp = 0,
   decay = 0.95,
   no.update.iter.max = 400,
   num.passes = 10,
   max.det.iter = 1e+06,
   method = "full",
   scaled = TRUE
)
```

n	design size.
р	design dimension.
design	an initial LHD. If design=NULL, a random LHD is generated.
max.sa.iter	maximum number of swapping involved in the simulated annealing (SA) algorithm.
temp	initial temperature of the simulated annealing algorithm. If temp=0, it will be automatically determined.

decay	the temperature decay rate of simulated annealing.
no.update.iter	max
	the maximum number of iterations where there is no update to the global opti- mum before SA stops.
num.passes	the maximum number of passes of the whole design matrix if deterministic swapping is used.
max.det.iter	maximum number of swapping involved in the deterministic swapping algorithm.
method	choice of "deterministic", "sa", or "full". If the method="full", the design is first optimized by SA and then deterministic swapping.
scaled	whether the design is scaled to unit hypercube. If scaled=FALSE, the design is represented by integer numbers from 1 to design size. Leave it as TRUE when no initial design is provided.

maxproLHD generates a MaxPro Latin-hypercube design (Joseph, V. R., Gul, E., & Ba, S. 2015). The major difference with the MaxPro packages is that we have a deterministic swap algorithm, which can be enabled by setting method="deterministic" or method="full". For optimization details, see the detail section in customLHD.

Value

design	final design points.
total.iter	total number of swaps in the optimization.
criterion	final optimized criterion.
crit.hist	criterion history during the optimization process.

References

Joseph, V. R., Gul, E., & Ba, S. (2015). Maximum projection designs for computer experiments. Biometrika, 102(2), 371-380.

Examples

n = 20p = 3D = maxproLHD(n, p) randomLHD

Description

This function generates a random Latin hypercube design.

Usage

randomLHD(n, p)

Arguments

n	design size.
р	design dimension

Details

randomLHD generates a random Latin hypercube design.

Value

a random Latin hypercube design.

Examples

n = 20 p = 3D = randomLHD(n, p)

uniform.crit Uniform criterion

Description

This function calculates the wrap-around discrepancy of a design.

Usage

```
uniform.crit(design)
```

Arguments

design a design matrix.

uniform.crit calculates the wrap-around discrepancy of a design. The wrap-around discrepancy for a design $D = [x_1, \ldots, x_n]^T$ is defined as (Hickernell, 1998):

$$\phi_{wa} = -\left(\frac{4}{3}\right)^p + \frac{1}{n^2} \sum_{i,j=1}^n \prod_{k=1}^p \left[\frac{3}{2} - |x_{ik} - x_{jk}|(1 - |x_{ik} - x_{jk}|)\right].$$

Value

wrap-around discrepancy of the design

References

Hickernell, F. (1998), "A generalized discrepancy and quadrature error bound," Mathematics of computation, 67, 299–322.

Examples

n = 20 p = 3 D = randomLHD(n, p) uniform.crit(D)

uniform.discrete	Generate a uniform design for discrete factors with different number
	of levels

Description

This function generates a uniform design for discrete factors with different number of levels.

Usage

```
uniform.discrete(
    t,
    p,
    levels,
    design = NULL,
    max.sa.iter = 1e+06,
    temp = 0,
    decay = 0.95,
    no.update.iter.max = 400,
    num.passes = 10,
    max.det.iter = 1e+06,
    method = "full",
    scaled = TRUE
)
```

uniform.discrete

Arguments

t	multiple of the least common multiple of the levels.	
р	design dimension.	
levels	a vector of the number of levels for each dimension.	
design	an initial design. If design=NULL, a random design is generated.	
max.sa.iter	maximum number of swapping involved in the simulated annealing (SA) algorithm.	
temp	initial temperature of the simulated annealing algorithm. If temp=0, it will be automatically determined.	
decay	the temperature decay rate of simulated annealing.	
no.update.iter.max		
	the maximum number of iterations where there is no update to the global opti- mum before SA stops.	
num.passes	the maximum number of passes of the whole design matrix if deterministic swapping is used.	
<pre>max.det.iter</pre>	maximum number of swapping involved in the deterministic swapping algorithm.	
method	choice of "deterministic", "sa", or "full". If the method="full", the design is first optimized by SA and then deterministic swapping.	
scaled	whether the design is scaled to unit hypercube. If scaled=FALSE, the design is represented by integer numbers from 1 to design size. Leave it as TRUE when no initial design is provided.	

Details

uniform.discrete generates a uniform design of discrete factors with different number of levels by minimizing the wrap-around discrepancy criterion (see uniform.crit).

Value

design	final design points.
design.int	design transformed to integer numbers for each dimenion
total.iter	total number of swaps in the optimization.
criterion	final optimized criterion.
crit.hist	criterion history during the optimization process.

```
p = 5
levels = c(3, 4, 6, 2, 3)
t = 1
D = uniform.discrete(t, p, levels)
```

uniform.optim

Description

This function optimizes a design through continuous optimization of the wrap-around discrepancy.

Usage

```
uniform.optim(D.ini, iteration = 10)
```

Arguments

D.ini	the initial design.
iteration	number iterations for LBFGS.

Details

uniform.optim optimizes a design through continuous optimization of the wrap-around discrepancy (see uniform.crit) by L-BFGS-B algorithm (Liu and Nocedal 1989).

Value

design	optimized design.
D.ini	initial design.

References

Liu, D. C., & Nocedal, J. (1989). On the limited memory BFGS method for large scale optimization. Mathematical programming, 45(1), 503-528.

Examples

n = 20 p = 3 D = uniformLHD(n, p)\$design D = uniform.optim(D)\$design uniformLHD

Description

This function generates a uniform LHD by minimizing the wrap-around discrepancy.

Usage

```
uniformLHD(
   n,
   p,
   design = NULL,
   max.sa.iter = 1e+06,
   temp = 0,
   decay = 0.95,
   no.update.iter.max = 400,
   num.passes = 10,
   max.det.iter = 1e+06,
   method = "full",
   scaled = TRUE
)
```

n	design size.	
р	design dimension.	
design	an initial LHD. If design=NULL, a random LHD is generated.	
max.sa.iter	maximum number of swapping involved in the simulated annealing (SA) algorithm.	
temp	initial temperature of the simulated annealing algorithm. If temp=0, it will be automatically determined.	
decay	the temperature decay rate of simulated annealing.	
no.update.iter.max		
	the maximum number of iterations where there is no update to the global opti- mum before SA stops.	
num.passes	the maximum number of passes of the whole design matrix if deterministic swapping is used.	
<pre>max.det.iter</pre>	maximum number of swapping involved in the deterministic swapping algorithm.	
method	choice of "deterministic", "sa", or "full". If the method="full", the design is first optimized by SA and then deterministic swapping.	
scaled	whether the design is scaled to unit hypercube. If scaled=FALSE, the design is represented by integer numbers from 1 to design size. Leave it as TRUE when no initial design is provided.	

uniformLHD generates a uniform LHD minimizing wrap-around discrepancy (see uniform.crit). The optimization details can be found in customLHD.

Value

design	final design points.
total.iter	total number of swaps in the optimization.
criterion	final optimized criterion.
crit.hist	criterion history during the optimization process.

Examples

n = 20 p = 3D = uniformLHD(n, p)

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