Package 'DepthProc'

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Title Statistical Depth Functions for Multivariate Analysis

Description Data depth concept offers a variety of powerful and user friendly tools for robust exploration and inference for multivariate data. The offered techniques may be successfully used in cases of lack of our knowledge on parametric models generating data due to their nature. The package consist of among others implementations of several data depth techniques involving multivariate quantile-quantile plots, multivariate scatter estimators, multivariate Wilcoxon tests and robust regressions.

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Depends R (>= 3.0.0), ggplot2, Rcpp (>= 0.11.2), rrcov, methods, MASS, np

Imports lattice, sm, geometry, colorspace, zoo, grDevices

Suggests mvtnorm, rgl, sn, robustbase, dplyr, RcppArmadillo, xts, covr, testthat, fda, lintr, roxygen2, pkgbuild

LinkingTo Rcpp, RcppArmadillo

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https://github.com/zzawadz/DepthProc

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NeedsCompilation yes

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Description

Add fitted line to a plot. This is overloaded function for robust regression methods from package depthproc.

Usage

```
## S4 method for signature 'RobReg'
abline(
    a = NULL,
    b = NULL,
    h = NULL,
    v = NULL,
    reg = NULL,
    coef = NULL,
    untf = FALSE,
    ...
)
```

```
a an object of class RobReg
b not used.
h not supported.
v not supported.
```

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```
reg not supported.

coef not supported.

untf not supported.

. . . Arguments to be passed to methods, such as graphical parameters (see par).
```

as.matrix

as.matrix method for DepthCurveList.

Description

Create a matrix from DepthCurve and DepthCurveList.

Usage

```
as.matrix(x, ...)
## S4 method for signature 'DepthCurveList'
as.matrix(x)
```

Arguments

x an object of class that inherits from DepthCurveList (ScaleCurveList or AsymmetryCurveList).

... other arguments passed to standard as.matrix function.

asymmetryCurve

Asymmetry curve based on depths

Description

Produces an asymmetry curve estimated from given data.

Usage

```
asymmetryCurve(
    x,
    y = NULL,
    alpha = seq(0, 1, 0.01),
    movingmedian = FALSE,
    name = "X",
    name_y = "Y",
    depth_params = list(method = "Projection")
)
```

asymmetryCurve 5

Arguments

X	The data as a matrix or data frame. If it is a matrix or data frame, then each row
	is viewed as one multivariate observation.

y Additional matrix of multivariate data.

alpha An ordered vector containing indices of central regins used for asymmetry curve

calculation.

movingmedian Logical. For default FALSE only one depth median is used to compute asym-

metry norm. If TRUE — for every central area, a new depth median will be used

— this approach needs much more time.

name Name of set X — used in plot legend name_y Name of set Y — used in plot legend

depth_params list of parameters for function depth (method, threads, ndir, la, lb, pdim, mean,

cov, exact).

method Character string which determines the depth function used. The method can be

"Projection" (the default), "Mahalanobis", "Euclidean", "Tukey" or "LP". For

details see depth.

Details

For sample depth function $D(x,Z^n)$, $x\in R^d$, $d\geq 2$, $Z^n=\{z_1,...,z_n\}\subset R^d$, $D_\alpha(Z^n)$ denoting α —central region, we can define the asymmetry curve $AC(\alpha)=\big(\alpha,\big\|c^{-1}(\{\bar z-med|D_\alpha(Z^n)\})\big\|\big)\subset R^2$, for $\alpha\in[0,1]$ being nonparametric scale and asymmetry functional correspondingly, where c—denotes constant, $\bar z$ —denotes mean vector, denotes multivariate median induced by depth function and vol—denotes a volume.

Asymmetry curve takes uses function convhulln from package geometry for computing a volume of convex hull containing central region.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

References

Serfling R. J. Multivariate Symmetry and Asymmetry, *Encyclopedia of Statistical Science*, S Kotz, C.B. Read, N. Balakrishnan, B. Vidakovic (eds), 2nd, ed., John Wiley.

Liu, R.Y., Parelius, J.M. and Singh, K. (1999), Multivariate analysis by data depth: Descriptive statistics, graphics and inference (with discussion), *Ann. Statist.*, **27**, 783–858.

Chaudhuri, P. (1996), On a Geometric Notion of Quantiles for Multivariate Data, *Journal of the American Statistical Association*, 862–872.

Dyckerhoff, R. (2004), Data Depths Satisfying the Projection Property, *Allgemeines Statistisches Archiv.*, **88**, 163–190.

See Also

scaleCurve, depth

6 BinnDepth2d-class

Examples

```
# EXAMPLE 1
library(sn)
xi < -c(0, 0)
alpha <- c(2, -5)
Omega <- diag(2) * 5
n <- 500
X <- mvrnorm(n, xi, Omega) # normal distribution
Y <- rmst(n, xi, Omega, alpha, nu = 1)
asymmetryCurve(X, Y, name = "NORM", name_y = "S_T(2, -5, 10)")
# EXAMPLE 2
data(under5.mort)
data(inf.mort)
data(maesles.imm)
data1990 <- cbind(under5.mort[, 1], inf.mort[, 1], maesles.imm[, 1])</pre>
data2011 <- cbind(under5.mort[, 22], inf.mort[, 22], maesles.imm[, 22])</pre>
as1990 <- asymmetryCurve(data1990, name = "scale curve 1990")</pre>
as2011 <- asymmetryCurve(data2011, name = "scale curve 2011")
figure <- getPlot(combineDepthCurves(as1990, as2011)) +</pre>
  ggtitle("Scale curves")
figure
```

 $Asymmetry Curve-class \quad \textit{Asymmetry Curve and Asymmetry Curve-List}$

Description

AsymmetryCurve is a class that stores results of asymmetryCurve function.

Details

The mechanism of creating plots with multiple curves is shown in DepthCurve-class (same mechanism is applied for ScaleCurve).

BinnDepth2d-class BinnDepth2d

Description

Class that stores result of function binningDepth2D(...)

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Slots

```
freq Matrix with number of elements in certain bin.
mid_x Middle values on x-axis.
mid_y Middle values on y-axis.
breaks_x Boundaries of bins.
breaks_y Boundaries of bins.
input_data Binned data.
max_depth_x Point with maximum depth on x-axis.
max_depth_y Point with maximum depth on y-axis.
```

binningDepth2D

2d Binning

Description

A robust method of decreasing a sample size and therefore a complexity of a statistical procedure. The method may be used within a kernel density or a predictive distribution estimation.

Usage

```
binningDepth2D(
    x,
    binmethod = "LocDepth",
    nbins = 8,
    k = 1,
    remove_borders = FALSE,
    depth_params = list(method = "LP")
)
```

X	bivariate matrix containing data. Each row is viewed as one two-dimensional observation.
binmethod	A method for calculation center and dispersion measures. "LocDepth" uses location-scale depth, MAD uses median and MAD in each dimension.
nbins	number of bins in each dimension
k	responsible for tightness of bins.
remove_borders	Logical, include or not marginal bins
depth_params	other arguments passed to depthMedian

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Details

Let us recall, that binning is a popular method of decreasing a sample size. To bin a window of n points $W_{i,n} = \{X_{i-n+1}, ..., X_i\}$ to a grid $X'_1, ..., X'_m$ we simply assign each sample point X_i to the nearest grid point X'_j . When binning is completed, each grid point X'_j has an associated number c_i , which is the sum of all the points that have been assigned to X'_j . This procedure replaces the data $W_{i,n} = \{X_{i-n+1}, ..., X_i\}$ with the smaller set $W'_{j,m} = \{X'_{j-m+1}, ..., X'_j\}$. Although simple binning can speed up the computation, it is criticized for a lack of precise approximate control over the accuracy of the approximation. Robust binning however stresses properties of the majority of the data and decreases the computational complexity of the DSA at the same time.

For a 1D window $W_{i,n}$, let $Z_{i,n-k}$ denote a 2D window created basing on $W_{i,n}$ and consisted of n-k pairs of observations and the k lagged observations $Z_{i,n-k} = \{(X_{i-n-k}, X_{i-n+1})\}$, $1 \le i \le n-k$. Robust 2D binning of the $Z_{i,n-p}$ is a very useful technique in a context of robust estimation of the predictive distribution of a time series (see *Kosiorowski:2013b*).

Assume we analyze a data stream $\{X_t\}$ using a moving window of a fixed length n, i.e., $W_{i,n}$ and the derivative window $Z_{i,n-1}$. In a first step we calculate the weighted sample L^p depth for $W_{i,n}$. Next we choose equally spaced grid of points $l_1,...,l_m$ in this way that $[l_1,l_m]\times[l_1,l_m]$ covers fraction of the β central points of $Z_{i,n-1}$ w.r.t. the calculated L^p depth, i.e., it covers $R^\beta(Z_{i,n-1})$ for certain prefixed threshold $\beta\in(0,1)$. For both X_t and X_{t-1} we perform a simple binning using following bins: $(-\infty,l_1),\ (l_1,l_2),\ ...,\ (l_m,\infty)$. For robust binning we reject "border" classes and further use only midpoints and binned frequencies for classes $(l_1,l_2),\ (l_2,l_3),\ ...,\ (l_{m-1},l_m)$.

Value

freq: a matrix containing the binned frequencies

mid_x: mid points for x mid_y: mid points for y breaks_x: breaks for x breaks_y: breaks for y

input_data: max_depth_x and max_depth_y:

Author(s)

Daniel Kosiorowski and Zygmunt Zawadzki from Cracow University of Economics.

References

Hall, P., Wand, M. P. (1996) On the Accuracy of Binned Kernel Density Estimators, Journal of Multivariate Analysis archive, Volume 56 Issue 2, 165–184

Holmstrom, L. (2000) The Accuracy and the Computational Complexity of a Multivariate Binned Kernel Density Estimator, Journal of Multivariate Analysis, Volume 72, Issue 2, 264–309, doi: 10.1006/jmva.1999.1863. (https://www.sciencedirect.com/science/article/pii/S0047259X99918638)

See Also

depth

combineDepthCurves 9

Examples

```
# EXAMPLE 1
Sigma1 <- matrix(c(10, 3, 3, 2), 2, 2)
X1 \leftarrow mvrnorm(n = 8500, mu = c(0, 0), Sigma1)
Sigma2 <- matrix(c(10, 0, 0, 2), 2, 2)
X2 \leftarrow mvrnorm(n = 1500, mu = c(-10, 6), Sigma2)
BALLOT <- rbind(X1, X2)</pre>
train <- sample(1:10000, 500)
data <- BALLOT[train, ]</pre>
plot(data)
b1 <- binningDepth2D(data, remove_borders = FALSE, nbins = 12, k = 1)
b2 <- binningDepth2D(data, nbins = 12, k = 1, remove_borders = TRUE)
plot(b1)
plot(b2)
# EXAMPLE 2
data(under5.mort)
data(maesles.imm)
data2011 <- cbind(under5.mort[, 22], maesles.imm[, 22])</pre>
plot(binningDepth2D(data2011, nbins = 8, k = 0.5, remove_borders = TRUE))
```

combineDepthCurves

Adds plots

Description

Adds plots

Usage

```
combineDepthCurves(x, y, .list = NULL)
## S4 method for signature 'ANY,ANY,list'
combineDepthCurves(x, y, .list = NULL)
## S4 method for signature 'DepthCurveList,DepthCurve,ANY'
combineDepthCurves(x, y, .list = NULL)
## S4 method for signature 'DepthCurve,DepthCurveList,ANY'
combineDepthCurves(x, y, .list = NULL)
## S4 method for signature 'DepthCurve,DepthCurve,ANY'
combineDepthCurves(x, y, .list = NULL)
```

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Arguments

Χ	object
у	object

.list list of plots to combine.

Details

See DepthCurve-class for description.

CovDepthWeighted-class

CovLP

Description

This class, derived from the virtual class "CovRobust" accommodates weighted by L^p depth multivariate location and scatter estimator.

Details

See CovLP for the function used to calculate weighted by L^p depth covariance matrix.

CovLp CovLp

Description

Weighted by L^p depth (outlyingness) multivariate location and scatter estimators.

Usage

$$CovLP(x, pdim = 2, la = 1, lb = 1)$$

X	The data as a matrix or data frame. If it is a matrix or data frame, then each row is viewed as one multivariate observation.
pdim	The parameter of the weighted L^pdim depth
la	parameter of a simple weight function $w = ax + b$
lb	parameter of a simple weight function $w = ax + b$

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Details

Using depth function one can define a depth-weighted location and scatter estimators. In case of location estimator we have

$$L(F) = \int x w_1(D(x,F)) dF(x) / w_1(D(x,F)) dF(x)$$

Subsequently, a depth-weighted scatter estimator is defined as

$$S(F) = \frac{\int (x - L(F))(x - L(F))^{T} w_{2}(D(x, F)) dF(x)}{\int w_{2}(D(x, F)) dF(x)},$$

where $w_2(\cdot)$ is a suitable weight function that can be different from $w_1(\cdot)$.

The **DepthProc** package offers these estimators for weighted L^p depth. Note that $L(\cdot)$ and $S(\cdot)$ include multivariate versions of trimmed means and covariance matrices. Their sample counterparts take the form

$$T_{WD}(X^{n}) = \sum_{i=1}^{n} d_{i} X_{i} / \sum_{i=1}^{n} d_{i},$$

$$DIS(X^{n}) = \frac{\sum_{i=1}^{n} d_{i} (X_{i} - T_{WD}(X^{n})) (X_{i} - T_{WD}(X^{n}))^{T}}{\sum_{i=1}^{n} d_{i}},$$

where d_i are sample depth weights, $w_1(x) = w_2(x) = x$.

Value

loc: Robust Estimate of Location:

cov: Robust Estimate of Covariance:

Returns depth weighted covariance matrix.

Author(s)

Daniel Kosiorowski and Zygmunt Zawadzki from Cracow University of Economics.

See Also

depthContour and depthPersp for depth graphics.

```
# EXAMPLE 1
x <- mvrnorm(n = 100, mu = c(0, 0), Sigma = 3 * diag(2))
cov_x <- CovLP(x, 2, 1, 1)

# EXAMPLE 2
data(under5.mort, inf.mort, maesles.imm)
data1990 <- na.omit(cbind(under5.mort[, 1], inf.mort[, 1], maesles.imm[, 1]))
CovLP(data1990)</pre>
```

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 $\verb|cracow.airpollution||$

Air pollution with PM10 in Cracow within day and night in December 2016

Description

Air pollution with PM10 in Cracow within day and night in December 2016

Usage

```
data("cracow.airpollution")
```

Format

data frame containing 744 rows.

References

- 1. Kosiorowski D, Rydlewski J P, Zawadzki Z (2017). 'Functional Outliers Detection By The Example Of Air Quality Monitoring.' submitted.
- 2. Kosiorowski D, Szlachtowska E (2017). 'K- local Median Algorithm for Functional Data in Empirical Analysis of Air Pollution Data.' Proceedings from the 11th Professor A. Zelias International Conference, pp. 153-162. Cracow University of Economics.

ddmvnorm

Normal depth versus depth plot

Description

Produces a normal DD plot of a multivariate dataset.

Usage

```
ddMvnorm(
    x,
    size = nrow(x),
    robust = FALSE,
    alpha = 0.05,
    title = "ddMvnorm",
    depth_params = list()
)
```

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Arguments

X	The data sample for DD plot.
size	size of theoretical set
robust	Logical. Default FALSE. If TRUE, robust measures are used to specify the parameters of theoretical distribution.
alpha	cutoff point for robust measure of covariance.
title	title of a plot.
depth_params	list of parameters for function depth (method, threads, ndir, la, lb, pdim, mean, cov, exact).

Details

In the first step the location and scale of x are estimated and theoretical sample from normal distribution with those parameters is generated. The plot presents the depth of empirical points with respect to dataset x and with respect to the theoretical sample.

Value

Returns the normal depth versus depth plot of multivariate dataset x.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

References

Liu, R.Y., Parelius, J.M. and Singh, K. (1999), Multivariate analysis by data depth: Descriptive statistics, graphics and inference (with discussion), Ann. Statist., 27, 783–858.

Liu, R.Y., Singh K. (1993), A Quality Index Based on Data Depth and Multivariate Rank Test, *Journal of the American Statistical Association* vol. 88.

See Also

ddPlot to generate ddPlot to compare to datasets or to compare a dataset with other distributions.

```
# EXAMPLE 1
norm <- mvrnorm(1000, c(0, 0, 0), diag(3))
con <- mvrnorm(100, c(1, 2, 5), 3 * diag(3))
sample <- rbind(norm, con)
ddMvnorm(sample, robust = TRUE)

# EXAMPLE 2
data(under5.mort, inf.mort, maesles.imm)
data1990 <- na.omit(cbind(under5.mort[, 1], inf.mort[, 1], maesles.imm[, 1]))
ddMvnorm(data1990, robust = FALSE)</pre>
```

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ddPlot

Depth versus depth plot

Description

Produces a DD plot which allows to compare two multivariate datasets or to compare a subject dataset with theoretical distribution.

Usage

```
ddPlot(
    x,
    y,
    scale = FALSE,
    location = FALSE,
    name = "X",
    name_y = "Y",
    title = "Depth vs. depth plot",
    depth_params = list()
)
```

Arguments

x	The first or only data sample for ddPlot.
у	The second data sample. x and y must be of the same space.
scale	logical. determines whether the dispersion is to be aligned.
location	determines whether the location is to be aligned to 0 vector with depth median.
name	name for data set x. It will be passed to drawing function.
name_y	as above for y
title	title of the plot.
depth_params	list of parameters for function depth (method, threads, ndir, la, lb, pdim, mean, cov, exact).

Details

For two probability distributions F and G, both in \mathbb{R}^d , we can define depth vs. depth plot being very useful generalization of the one dimensional quantile-quantile plot:

$$DD(F,G) = \left\{ (D(z,F), D(z,G)), z \in R^d \right\}$$

Its sample counterpart calculated for two samples $X^n = \{X_1, ..., X_n\}$ from F, and $Y^m = \{Y_1, ..., Y_m\}$ from G is defined as

$$DD(F_n, G_m) = \{(D(z, F_n), D(z, G_m)), z \in \{X^n \cup Y^m\}\}$$

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Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

References

Liu, R.Y., Parelius, J.M. and Singh, K. (1999), Multivariate analysis by data depth: Descriptive statistics, graphics and inference (with discussion), *Ann. Statist.*, **27**, 822–831.

Liu, R.Y., Singh K. (1993), A Quality Index Based on Data Depth and Multivariate Rank Test, *Journal of the American Statistical Association* vol. 88.

Examples

```
library(sn)
library(mvtnorm)

# EXAMPLE 1: Location difference
standard <- mvrnorm(1000, c(0, 0), diag(2))
shift <- mvrnorm(1000, c(0.5, 0), diag(2))
ddPlot(x = standard, y = shift, title = "Difference in position")
ddPlot(x = standard, y = shift, location = TRUE, title = "Location aligned")

# EXAMPLE 2: Scale difference
standard <- mvrnorm(1000, c(0, 0), diag(2))
scale <- mvrnorm(1000, c(0, 0), 4 * diag(2))
ddPlot(x = standard, y = scale)
ddPlot(x = standard, y = scale, scale = TRUE)</pre>
```

DDPlot-class

DDPlot

Description

Class fro DDPlot

Slots

```
X Object of class Depth-class.
```

Y Object of class Depth-class.

title title of a plot.

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deepReg2d

Simple deepest regression method.

Description

This function calculates deepest regression estimator for simple regression.

Usage

```
deepReg2d(x, y)
```

Arguments

```
x Independent variable.
```

y Dependent variable.

Details

Function originates from an original algorithm proposed by Rousseeuw and Hubert. Let $Z^n=(x_1,y_1),...,(x_n,y_n)\subset R^d$ denotes a sample considered from a following semiparametric model: $y_l=a_0+a_1x_{1l}+...+a_{(d-1)l}x_{(d-1)l}+\varepsilon_l, l=1,...,n$, we calculate a depth of a fit $\alpha=(a_0,...,a_{d-1})$ as $RD(\alpha,Z^n)=u\neq 0\min\sharp l:\frac{r_l(\alpha)}{u^Tx_l}<0, l=1,...,n$, where $r(\cdot)$ denotes the regression residual, $\alpha=(a_0,...,a_{d-1}), u^Tx_l\neq 0$. The deepest regression estimator $DR(\alpha,Z^n)$ is defined as $DR(\alpha,Z^n)=\alpha\neq 0$ arg max $RD(\alpha,Z^n)$

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

References

Rousseeuw J.P., Hubert M. (1998), Regression Depth, *Journal of The American Statistical Association*, vol.94.

```
# EXAMPLE 1
data(pension)
plot(pension)
abline(
  lm(Reserves ~ Income, data = pension),
  lty = 3,
  lwd = 2) # lm
abline(
  deepReg2d(pension[, 1], pension[, 2]),
  lwd = 2) # deepreg2d
```

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```
# EXAMPLE 2
data(under5.mort)
data(inf.mort)
data(maesles.imm)
data2011 <- na.omit(</pre>
    cbind(under5.mort[, 22], inf.mort[, 22],
    maesles.imm[, 22]))
x <- data2011[, 3]
y <- data2011[, 2]
plot(
  х, у,
  cex = 1.2,
  ylab = "infant mortality rate per 1000 live birth",
  xlab = "against masles immunized percentage",
  main = "Projection Depth Trimmed vs. LS regressions"
)
abline(lm(x \sim y), lwd = 2, col = "black") # lm
abline(
  deepReg2d (x, y),
  lwd = 2, col = "red"
) # trimmed reg
legend(
  "bottomleft",
  c("LS", "DeepReg"),
  fill = c("black", "red"),
  cex = 1.4,
  bty = "n"
)
```

DeepReg2d-class

DeepReg2d

Description

Class for robust regression methods from depthproc package

Slots

```
coef coefficients of fitted model
depth regression depth of the fitted values
```

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depth

Depth calculation

Description

Calculate depth functions.

Usage

```
depth(u, X, method = "Projection", threads = -1, ...)
```

Arguments

Numerical vector or matrix whose depth is to be calculated. Dimension has to be the same as that of the observations.

The data as a matrix, data frame or list. If it is a matrix or data frame, then each

Χ row is viewed as one multivariate observation. If it is a list, all components must

be numerical vectors of equal length (coordinates of observations).

Character string which determines the depth function. method can be "Promethod

jection" (the default), "Mahalanobis", "Euclidean" or "Tukey". For details see

depth.

threads number of threads used in parallel computations. Default value -1 means that all

possible cores will be used.

parameters specific to method — see depthEuclid

Details

The Mahalanobis depth

$$D_{MAH}(y, X^n) = \frac{1}{1 + (y - \bar{x})^T S^{-1} (y - \bar{x})},$$

where S denotes the sample covariance matrix X^n .

A symmetric projection depth D(x, X) of a point $x \in \mathbb{R}^d$, $d \ge 1$ is defined as

$$D\left(x,X\right)_{PRO} = \left\lceil 1 + sup_{\parallel u \parallel = 1} \frac{\left| u^Tx - Med\left(u^TX\right)\right|}{MAD\left(u^TX\right)} \right\rceil^{-1},$$

where Med denotes the univariate median, MAD(Z) = Med(|Z - Med(Z)|). Its sample version denoted by $D(x, X^n)$ or $D(x, X^n)$ is obtained by replacing F by its empirical counterpart F_n calculated from the sample X^n .

Next interesting depth is the weighted L^p depth. The weighted L^p depth D(x, F) of a point $x \in \mathbb{R}^d$, $d \geq 1$ generated by d dimensional random vector X with distribution F, is defined as D(x,F) = $\frac{1}{1+Ew(\|x-X\|_p)}$, where w is a suitable weight function on $[0,\infty)$, and $\|\cdot\|_p$ stands for the L^p norm (when p = 2 we have usual Euclidean norm). We assume that w is non-decreasing and continuous depth 19

on $[0,\infty)$ with $w(\infty-)=\infty$, and for $a,b\in R^d$ satisfying $w(\|a+b\|)\leq w(\|a\|)+w(\|b\|)$. Examples of the weight functions are: $w(x)=a+bx,\,a,b>0$ or $w(x)=x^\alpha$. The empirical version of the weighted L^p depth is obtained by replacing distribution F of X in $Ew(\|x-X\|_p)=\int w(\|x-t\|_p)dF(t)$ by its empirical counterpart calculated from the sample X^n ...

The Projection and Tukey's depths are calculated using an approximate algorithm. Calculations of Mahalanobis, Euclidean and L^p depths are exact. Returns the depth of multivariate point u with respect to data set X.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

References

Liu, R.Y., Parelius, J.M. and Singh, K. (1999), Multivariate analysis by data depth: Descriptive statistics, graphics and inference (with discussion), Ann. Statist., 27, 783–858.

Mosler K (2013). Depth statistics. In C Becker, R Fried, K S (eds.), Robustness and Complex Data Structures, Festschrift in Honour of Ursula Gather, pp. 17–34. Springer.

Rousseeuw, P.J. and Struyf, A. (1998), Computing location depth and regression depth in higher dimensions, Stat. Comput., 8, 193–203.

Zuo, Y. and Serfling, R. (2000), General Notions of Statistical Depth Functions, Ann. Statist., 28, no. 2, 461–482.

See Also

depthContour and depthPersp for depth graphics.

```
library(robustbase)

# Calculation of Projection depth
data(starsCYG, package = "robustbase")
depth(t(colMeans(starsCYG)), starsCYG)

# Also for matrices
depth(starsCYG, starsCYG)

# Projection depth applied to a large bivariate data set
x <- matrix(rnorm(9999), nc = 3)
depth(x, x)</pre>
```

20 depthContour

Depth-class

Depth

Description

Virtual class with structure for every depth class from depthproc package.

Slots

```
u data set.X reference set.method depth type.
```

 ${\tt depthContour}$

Approximate depth contours

Description

Draws an approximate contours of depth for bivariate data.

Usage

```
depthContour(
 xlim = extendrange(x[, 1], f = 0.1),
 ylim = extendrange(x[, 2], f = 0.1),
 n = 50,
 pmean = TRUE,
 mcol = "blue",
  pdmedian = TRUE,
 mecol = "brown",
  legend = TRUE,
  points = FALSE,
  colors = heat_hcl,
  levels = 10,
  depth_params = list(),
 graph_params = list(),
  contour_method = c("auto", "convexhull", "contour")
)
```

depthContour 21

Arguments

x	Bivariate data
xlim	Determines the width of x-axis.
ylim	Determines the width of y-axis.
n	Number of points in each coordinate direction to be used in contour plot.
pmean	Logical. If TRUE mean will be marked.
mcol	Determines the color of lines describing the mean.
pdmedian	Logical. If TRUE depth median will be marked.
mecol	Determines the color of lines describing the depth median.
legend	Logical. If TRUE legend for mean and depth median will be drawn.
points	Logical. If TRUE points from matrix x will be drawn.
colors	function for colors pallete (e.g. gray.colors).
levels	number of levels for color scale.
depth_params	list of parameters for function depth (method, threads, ndir, la, lb, pdim, mean, cov, exact).
graph_params	list of graphical parameters for functions filled.contour and contour (e.g. lwd, lty, main).
contour_method	determines the method used to draw the contour lines. The default value ("auto") tries to determine the best method for given depth function. "convexhull" uses a convex hull algorithm to determine boundaries. "contour" uses the algorithm from filled.contour.

Details

The set of all points that have depth at least α is called α -trimmed region. The α -trimmed region w.r.t. F is denoted by $D_{\alpha}(F)$, i.e.,

$$D_{\alpha}(F) = \left\{ z \in R^d : D(z, F) \ge \alpha \right\}.$$

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

See Also

depthPersp

```
# EXAMPLE 1
set.seed(123)
x <- mvrnorm(1000, c(0, 0), diag(2))
depthContour(x, colors = gray.colors)
# with points</pre>
```

22 DepthCurve-class

```
depthContour(x, points = TRUE)
depthContour(x, points = FALSE, levels = 10)
# EXAMPLE 2
data(inf.mort, maesles.imm)
data1990 <- na.omit(cbind(inf.mort[, 1], maesles.imm[, 1]))</pre>
depthContour(data1990, n = 50, pmean = TRUE, mcol = "blue",
             pdmedian = TRUE, mecol = "brown", legend = TRUE, points = TRUE,
             depth_params = list(method = "LP"),
             graph_params = list(
               xlab = "infant mortality rate per 1000 live birth",
               ylab = "against masles immunized percentage",
               main = "L2 depth, UN Fourth Goal 2011 year"))
#EXAMPLE 3
data("france")
depthContour(france,
   depth_params = list(method = "Tukey"),
   points = TRUE
)
```

DepthCurve-class

DepthCurve

Description

This page describes mechanism behavior of ScaleCurve and AsymmetryCurve

Details

DepthCurve is a virtual class that contains methods (getPlot(...) and plot(...)) for rendering single curve such as ScaleCurve or AsymmetryCurve. Such object can be combined by overloaded operator '

Slots

```
depth object of Depth-class
name name of dataset used on plot
title title of a plot
alpha central area values
```

DepthCurveList-class 23

Examples

```
library(mvtnorm)
x <- mvrnorm(n = 100, mu = c(0, 0), Sigma = 2 * diag(2))
y <- rmvt(n = 100, sigma = diag(2), df = 4)
s1 <- scaleCurve(x, depth_params = list(method = "Projection"))
s2 <- scaleCurve(y, depth_params = list(method = "Projection"), name = "Set2")
sc_list <- combineDepthCurves(s1, s2) # Add one curve to another

plot(sc_list) # Draw plot with two curves

z <- mvrnorm(n = 100, mu = c(0, 0), Sigma = 1 * diag(2))
s3 <- scaleCurve(z, depth_params = list(method = "Projection"))
plot(combineDepthCurves(sc_list, s3)) # Add third curve and draw a plot</pre>
```

DepthCurveList -class DepthCurveList

Description

DepthCurveList is a special container for DepthCurve objects. See DepthCurve-class

depthDensity

Depth weighted density estimator

Description

Experimental function used to fit depth weighted density estimator.

Usage

```
depthDensity(x, y, nx = 5, ny = 32, xg = NULL, yg = NULL, ...)
```

X	numeric vector
у	numeric vector
nx	the number of equally spaced points at which the density is to be estimated in x-dimension.
ny	the number of equally spaced points at which the density is to be estimated in x-dimension.
xg	vector of point at which the density is to be estimated.
уg	vector of point at which the density is to be estimated.
	arguments passed to depthLocal.

24 depthEuclid

References

Kosiorowski D. and Zawadzki Z. (2014) Notes on optimality of predictive distribution pseudo-estimators in the CHARME models and automatic trading strategies, FindEcon2014, submitted

Examples

```
## Not run:
# .sampleData is special function for creating
# data for testing conditional denisty estimators
data <- DepthProc:::.sampleData(1:5, 100)
x <- data[, 1]
y <- data[, 2]
plot(x, y)
dep <- depthDensity(x, y)
plot(dep, type = "raw")
plot(dep, type = "depth")
## End(Not run)</pre>
```

DepthDensity-class

DepthDensity

Description

Class for depth based density estimator.

Details

depthDensity

depthEuclid

Euclidean Depth

Description

Computes the euclidean depth of a point or vectors of points with respect to a multivariate data set.

Usage

```
depthEuclid(u, X)
```

depthLocal 25

Arguments

Χ

u	Numerical vector or matrix whose depth is to be calculated. Dimension has to
	be the same as that of the observations.

The data as a matrix, data frame or list. If it is a matrix or data frame, then each row is viewed as one multivariate observation. If it is a list, all components must be numerical vectors of equal length (coordinates of observations).

Details

Calculation of Euclidean depth is exact.

Returns the depth of multivariate point u with respect to data set X.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

Examples

```
x \leftarrow matrix(rnorm(9999), nc = 3)
depthEuclid(x, x)
```

depthLocal

Local depth

Description

Computes local version of depth according to proposals of Paindaveine and Van Bever — see referencess.

Usage

```
depthLocal(
    u,
    X,
    beta = 0.5,
    depth_params1 = list(method = "Projection"),
    depth_params2 = depth_params1
)
```

26 depthLocal

Arguments

Numerical vector or matrix whose depth is to be calculated. Dimension has to be the same as that of the observations.

X The data as a matrix, data frame. If it is a matrix or data frame, then each row is viewed as one multivariate observation.

beta cutoff value for neighbourhood

depth_params1 list of parameters for function depth (method, threads, ndir, la, lb, pdim, mean, cov, exact).

depth_params2 as above — default is depth_params1.

Details

A successful concept of local depth was proposed by Paindaveine and Van Bever (2012). For defining a neighbourhood of a point authors proposed using idea of symmetrisation of a distribution (a sample) with respect to a point in which depth is calculated. In their approach instead of a distribution P^X , a distribution $P_x = \frac{1}{2}P^X + \frac{1}{2}P^{2x-X}$ is used. For any $\beta \in [0,1]$, let us introduce the smallest depth region bigger or equal to β ,

$$R^{\beta}(F) = \bigcap_{\alpha \in A(\beta)} D_{\alpha}(F),$$

where $A(\beta) = \{\alpha \geq 0 : P[D_{\alpha}(F)] \geq \beta\}$. Then for a locality parameter β we can take a neighbourhood of a point x as $R_x^{\beta}(P)$.

Formally, let $D(\cdot, P)$ be a depth function. Then the local depth with the locality parameter β and w.r.t. a point x is defined as

$$LD^{\beta}(z,P): z \to D(z,P_x^{\beta}),$$

where $P_x^{\beta}(\cdot) = P\left(\cdot | R_x^{\beta}(P)\right)$ is cond. distr. of P conditioned on $R_x^{\beta}(P)$.

References

Paindaveine, D., Van Bever, G. (2013) From depth to local depth: a focus on centrality. Journal of the American Statistical Association 105, 1105–1119.

depthLP 27

```
depthContour(data1990,
             depth_params = list(
               method = "Local",
               depth_params1 = list(method = "LP"),
               beta = 0.3
             ))
# EXAMPLE 3
Sigma1 <- matrix(c(10, 3, 3, 2), 2, 2)
X1 \leftarrow mvrnorm(n = 8500, mu = c(0, 0), Sigma1)
Sigma2 <- matrix(c(10, 0, 0, 2), 2, 2)
X2 \leftarrow mvrnorm(n = 1500, mu = c(-10, 6), Sigma2)
BALLOT <- rbind(X1, X2)
train <- sample(1:10000, 100)</pre>
data <- BALLOT[train, ]</pre>
depthContour(data,
            depth_params = list(
              method = "Local",
              beta = 0.3,
              depth_params1 = list(method = "Projection")
            ))
## End(Not run)
```

 ${\sf depthLP}$

LP Depth

Description

Computes the LP depth of a point or vectors of points with respect to a multivariate data set.

Usage

```
depthLP(u, X, pdim = 2, la = 1, lb = 1, threads = -1, func = NULL)
```

u	Numerical vector or matrix whose depth is to be calculated. Dimension has to be the same as that of the observations.
X	The data as a matrix, data frame or list. If it is a matrix or data frame, then each row is viewed as one multivariate observation. If it is a list, all components must be numerical vectors of equal length (coordinates of observations).
pdim	dimension used in calculating depth function.
la	slope the weighing function.
1b	intercept in the weighing function.

28 depthMah

threads number of threads used in parallel computations. Default value -1 means that all

possible cores will be used.

func the weighing function. Currently it is not supported.

Details

Returns the depth of multivariate point u with respect to data set X.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

Examples

```
x <- matrix(rnorm(3000), ncol = 3)
# Same results
depthLP(x, x, pdim = 2)</pre>
```

depthMah

Mahalanobis Depth

Description

Computes the mahalanobis depth of a point or vectors of points with respect to a multivariate data set.

Usage

```
depthMah(u, X, cov = NULL, mean = NULL, threads = -1)
```

u	Numerical vector or matrix whose depth is to be calculated. Dimension has to be the same as that of the observations.
X	The data as a matrix, data frame or list. If it is a matrix or data frame, then each row is viewed as one multivariate observation. If it is a list, all components must be numerical vectors of equal length (coordinates of observations).
COV	custom covariance matrix passed. If NULL standard calculations will be based on standard covariance estimator.
mean	custom mean vector. If null — mean average will be used.
threads	number of threads used in parallel computations. Default value -1 means that all possible cores will be used.

depthMedian 29

Details

Calculation of Mahalanobis depth is exact.

Returns the depth of multivariate point u with respect to data set X.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

Examples

```
x \leftarrow matrix(rnorm(9999), nc = 3)
depthMah(x, x)
```

depthMedian

Depth median

Description

Return point with maximum depth function value. If multiple points have the same value, mean average of them will be returned.

Usage

```
depthMedian(x, depth_params = list(), convex = FALSE)
## S4 method for signature 'matrix'
depthMedian(x, depth_params = list(), convex = FALSE)
## S4 method for signature 'data.frame'
depthMedian(x, depth_params = list(), convex = FALSE)
## S4 method for signature 'Depth'
depthMedian(x, convex = FALSE)
```

Arguments

x object of class Depth or matrix.

depth_params list of parameters for function depth (method, threads, ndir, la, lb, pdim, mean,

cov, exact).

convex logical. If true, than centroid of the convex hull created from deepest points is

returned.

30 depthPersp

Examples

```
# depthMedian for matrix
x <- matrix(rnorm(600), nc = 3)
depthMedian(x)

# depthMedian works with object of class Depth
dp <- depth(x)
depthMedian(dp)</pre>
```

depthPersp

Perspective plot for depth functions

Description

Draws a perspective plot of depth function over x-y plane.

Usage

```
depthPersp(
    x,
    plot_method = "lattice",
    xlim = extendrange(x[, 1], f = 0.1),
    ylim = extendrange(x[, 2], f = 0.1),
    n = 50,
    xlab = "x",
    ylab = "y",
    plot_title = NULL,
    colors = heat_hcl,
    depth_params = list(),
    graph_params = list()
)
```

```
bivariate data
plot_method
                   there are two options "lattice", and "rgl" — see details
xlim
                   limits for x-axis
ylim
                   limits for y-axis
                   number of points that will be used to create plot (n^2)
xlab
                   description of x-axis
ylab
                   description of y-axis
                   plot title (default NULL means paste(depth_params$method, "depth"))
plot_title
colors
                   function for colors pallete (e.g. gray.colors).
                   list of parameters for function depth ("method", "threads", "ndir", "la", "lb",
depth_params
                   "pdim", "mean", "cov", "exact").
                   list of graphical parameters for functions rgl::persp3d and lattice::wireframe.
graph_params
```

depthProjection 31

Details

plot_method — rgl package is not in depends list beacuse it may cause problems when OpenGL is not supported. To use plot_method = "rgl" you must load this package on your own.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

Examples

depthProjection

Projection Depth

Description

Computes the Projection depth of a point or vectors of points with respect to a multivariate data set.

Usage

```
depthProjection(u, X, ndir = 1000, threads = −1)
```

u	Numerical vector or matrix whose depth is to be calculated. Dimension has to be the same as that of the observations.
X	The data as a matrix, data frame or list. If it is a matrix or data frame, then each row is viewed as one multivariate observation. If it is a list, all components must be numerical vectors of equal length (coordinates of observations).
ndir	number of directions used in computations
threads	number of threads used in parallel computations. Default value -1 means that all possible cores will be used.

32 depthTukey

Details

Irrespective of dimension, Projection and Tukey's depth is obtained by approximate calculation. Returns the depth of multivariate point u with respect to data set X.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

Examples

```
x <- matrix(rnorm(3000), nc = 3)
a <- depthProjection(x, x, ndir = 2000)</pre>
```

Tukey Depth

Description

Computes the Tukey depth of a point or vectors of points with respect to a multivariate data set.

Usage

```
depthTukey(u, X, ndir = 1000, threads = -1, exact = FALSE)
```

Arguments

u	Numerical vector or matrix whose depth is to be calculated. Dimension has to be the same as that of the observations.
X	The data as a matrix, data frame or list. If it is a matrix or data frame, then each row is viewed as one multivariate observation. If it is a list, all components must be numerical vectors of equal length (coordinates of observations).
ndir	number of directions used in computations
threads	number of threads used in parallel computations. Default value -1 means that all possible cores will be used.
exact	if TRUE exact almorithm will be used . Currently it works only for 2 dimensional data set.

Details

Irrespective of dimension, Projection and Tukey's depth is obtained by approximate calculation. Returns the depth of multivariate point u with respect to data set X.

fncBoxPlot 33

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

Examples

```
## Not run:
x <- matrix(rnorm(3000), nc = 3)
depthTukey(x, ndir = 2000)

## End(Not run)

# Exact algorithm in 2d
x <- matrix(rnorm(2000), nc = 2)
depthTukey(x, exact = TRUE)</pre>
```

fncBoxPlot

Functional boxplot based on Modified Band Depth

Description

Functional boxplot based on Modified Band Depth

Usage

```
fncBoxPlot(u, X = NULL, bands = c(0, 0.5), method = "MBD", byrow = NULL, ...)
```

Arguments

u data matrix

X reference set. If null u will be used as reference.

bands limits for bands method depth method

byrow byrow

... other arguments passed to fncDepth

```
# some data:
x <- matrix(rnorm(200), ncol = 10)

fncBoxPlot(x, bands = c(0, 0.5, 1), method = "FM")
fncBoxPlot(x, bands = c(0, 0.5, 1), method = "FM", byrow = FALSE)

colnames(x) <- paste0("f", 1:ncol(x))
fncBoxPlot(x, bands = c(0, 0.5, 1), method = "FM")</pre>
```

34 fncDepth

```
# fncBoxPlot handles zoo and xts objects
library(xts)
x <- matrix(rnorm(200), ncol = 10)
time <- as.POSIXct(1:ncol(x) * 86400, origin = "1970-01-01")
x_xts <- xts(t(x), order.by = time)
fncBoxPlot(x_xts, bands = c(0, 0.5, 1), method = "FM")

data("katowice.airpollution")
pl <- fncBoxPlot(katowice.airpollution, bands = c(0, 0.5, 1), method = "MBD")
pl + ggtitle("Air pollution in Katowice") + labs(y= "pollination ", x = "hour ")</pre>
```

fncDepth

Basic function for functional depths

Description

Calculates depth functions.

Usage

```
fncDepth(u, X = NULL, method = "MBD", byrow = NULL, ...)
## S3 method for class 'matrix'
fncDepth(u, X = NULL, method = "MBD", byrow = NULL, ...)
## S3 method for class 'zoo'
fncDepth(u, X = NULL, method = "MBD", byrow = NULL, ...)
```

Arguments

u data
 X reference set. If null u will be used as reference.
 method depth method - "MBD" (default), or "FM" (Frainman-Muniz depth)
 byrow logical or character.
 ... additional arguments passed to fncDepthFM.

```
x <- matrix(rnorm(60), ncol = 20)
fncDepth(x, method = "FM", dep1d = "Mahalanobis")
fncDepth(x, byrow = FALSE)

# zoo and xts
library(xts)
data(sample_matrix)
sample.xts <- as.xts(sample_matrix, descr = "my new xts object")</pre>
```

fncDepthFM 35

```
fncDepth(sample.xts)
```

fncDepthFM	FM Depth
------------	----------

Description

Computes Frainman-Muniz depth for functional data.

Usage

```
fncDepthFM(u, X, dep1d_params = list(method = "Projection"))
```

Arguments

u Numerical vector or matrix whose depth is to be calculated. Dimension has to

be the same as that of the observations.

X The data as a matrix. If it is a matrix or data frame, then each row is viewed as

one multivariate observation.

dep1d_params parameters passed to depth function used in one dimension.

Examples

```
x <- matrix(rnorm(60), nc = 20)
fncDepthFM(x)</pre>
```

depth		
-------	--	--

Description

Computes the modified band depth.

Usage

```
fncDepthMBD(u, X)
```

Arguments

u	Numerical vector or matrix whose depth is to be calculated. Dimension has to
	be the same as that of the observations.

X The data as a matrix. If it is a matrix or data frame, then each row is viewed as one multivariate observation.

36 fncGetBand

Examples

```
x <- matrix(rnorm(60), nc = 20)
fncDepthMBD(x)
fncDepthMBD(x, x)</pre>
```

fncDepthMedian

Functional median

Description

Calculate functional median based on data depth.

Usage

```
fncDepthMedian(u, X = NULL, method = "MBD", byrow = NULL, unique = TRUE, ...)
```

Arguments

u data matrix

X reference set. If null u will be used as reference.

method depth method

byrow byrow unique if true

... other arguments passed to fncDepth

Examples

```
x <- matrix(rnorm(600), nc = 20)
md <- fncDepthMedian(x, method = "FM", dep1d = "Mahalanobis")</pre>
```

fncGetBand

Functional bands

Description

Extract bands from functional depth object.

Usage

```
fncGetBand(obj, band = 0.5)
```

france 37

Arguments

obj object that inherits from FunctionalDepth.

band single numeric value.

Examples

```
x <- matrix(rnorm(600), nc = 20)
obj <- fncDepth(x, method = "FM", dep1d = "Mahalanobis")
fncGetBand(obj)</pre>
```

france

Relation between minimum wage (MW) and unemployment rate (UR) in France.

Description

Relation between minimum wage (MW) and unemployment rate (UR) in France.

Usage

```
data(france)
```

Format

data frame containing 17 rows and two column. MW is a minimum wage, and UR is an unemployment rate.

FunctionalDepth-class Functional Depth

Description

Virtual class with structure for every functional depth class from depthproc package. Inherits from Depth-class.

Slots

index numeric, or time-based object.

38 inf.mort

getPlot	Create ggplot object from DepthCurve, DepthCurveList and DDPlot
	classes.

Description

Create an object of class ggplot from DepthCurve and DepthCurveList.

Usage

```
getPlot(object)
## S4 method for signature 'AsymmetryCurveList'
getPlot(object)
## S4 method for signature 'DDPlot'
getPlot(object)
## S4 method for signature 'ScaleCurveList'
getPlot(object)
```

Arguments

object

a DDPlot ScaleCurve or AsymmetryCurve object class.

inf.mort

Infant mortality rate (0–1 year) per 1,000 live births

Description

Infant mortality rate (0-1 year) per 1,000 live births

Usage

```
data(inf.mort)
```

Format

A data frame with 654 rows and 4 variables

Source

http://mdgs.un.org/unsd/mdg/Data.aspx

internet.users 39

internet.users

Internet view data

Description

Internet view data

Usage

data(internet.users)

Format

data frame containing 17518 rows and 6 columns — 17518 working days of the Internet service considered with respect to variables: service, month, day, hour, unique users and page views.

References

Kosiorowski, Rydlewski, Snarska (2016), Detecting a Structural Change in Functional Time Series Using Local Wilcoxon Statistic, arXiv: 1604.03776v2

katowice.airpollution Air pollution in Katowice city by hour.

Description

Air pollution in Katowice city by hour.

Usage

```
data("katowice.airpollution")
```

Format

data frame containing 181 rows (days) and 24 columns. Each column is an air pollination for given hour.

LSDepth-class

1sdAddContour

Adds location scale depth contour to the existing plot.

Description

This function add one location-scale contour to the existing plot.

Usage

```
lsdAddContour(x, cont = NULL, ...)
## S4 method for signature 'LSDepthContour'
lsdAddContour(x, cont = NULL, ...)
```

Arguments

```
x object of class LSDepthContourcont depth of contour to plot... other arguments passed to polygon function
```

Examples

```
smp <- rf(100, 5, 10)
x <- lsdSampleDepthContours(smp)
plot(x)
lsdAddContour(x, 0.1, col = "grey50")
lsdAddContour(x, 0.3, col = "grey10", border = "red", lwd = 4)</pre>
```

LSDepth-class

Location-Scale depth class

Description

Class used to store maximum location-scale depth results.

Slots

```
max_depth maximum Student depth value.

mu location estimate in the deepest point.

sigma scale estimate in the deepest point.
```

LSDepthContour-class

LSDepthContour-class Location-Scale depth contour class

Description

Class used to store result of location-scale depth contours.

Slots

```
cont_depth depth values used to calculate contours. sample original sample used to calculate depth contours. Data list with estimated values of scale-depth contours.
```

1sdGetContour

Get location-scale contour from LSDepthContour object.

Description

Get numeric values of the location-scale depth contour from existing object of LSDepthContour class

Usage

```
lsdGetContour(x, cont)
## S4 method for signature 'LSDepthContour'
lsdGetContour(x, cont)
```

Arguments

```
x object of class LSDepthContour
cont single numeric — depth of contour to return
```

Details

Calculations are based on Isdepth algorithm written by Ch. Muller.

```
dcont <- lsdSampleDepthContours(rf(200, 4, 7), depth = c(0.1, 0.2))
# get contour that is present in dcont object
lsdGetContour(dcont, 0.1)
# get contour that is not present in dcont
# it will be automatically calculated
lsdGetContour(dcont, 0.3)</pre>
```

lsdSampleDepthContours

Calculate sample Mizera and Muller Student depth contours

Description

Calculate sample one-dimensional Mizera and Muller Student depth contours.

Usage

```
lsdSampleDepthContours(x, depth = c(0.1, 0.2, 0.3, 0.4), lengthmu = 1000)
```

Arguments

x one dimensional vector with sample

depth depth level for contours

lengthmu number of points to evalute depth

Details

Calculations are based on Isdepth algorithm written by Ch. Muller.

References

Mizera, I., Muller, C. H., 2004. Location-scale depth (with discussion). Journal of the American Statistical Association 99, 949–966.

```
# EXAMPLE 1
# F-distribution
dcont <- lsdSampleDepthContours(rf(200, 4, 7))
plot(dcont)

# EXAMPLE 2
# normal distribution - more contours calculated
dcont_norm <- lsdSampleDepthContours(rnorm(100), seq(0.05, 0.4, 0.05))
plot(dcont_norm)</pre>
```

lsdSampleMaxDepth 43

lsdSampleMaxDepth	Calculates the maximum sample location-scale depth	
lsdSampleMaxDepth	Calculates the maximum sample location-scale depth	

Description

Calculates the maximum Student depth estimator of location and scale for one dimensional data (an alternative for MED and MAD or for the mean and standard deviation).

Usage

```
lsdSampleMaxDepth(x, iter = 100, eps = 1e-04, p_length = 10)
```

Arguments

x	one dimensional vector with sample
iter	maximum number of iterations in algorith for calculation Location-Scale Depth
eps	tolerance level
p_length	is the maximum length of the precision step at the end

Details

Calculations are based on Isdepth algorithm written by Ch. Muller.

References

Mizera, I., Muller, C. H., 2004. Location-scale depth (with discussion). Journal of the American Statistical Association 99, 949–966.

```
x <- rnorm(100)
lsdSampleMaxDepth(x)
y <- rf(100, 4, 10)
lsdSampleMaxDepth(y)</pre>
```

44 mWilcoxonTest

maesles.imm

Children 1 year old immunized against measles, percentage

Description

Children 1 year old immunized against measles, percentage

Usage

```
data(maesles.imm)
```

Format

A data frame with 654 rows and 4 variables

Source

http://mdgs.un.org/unsd/mdg/Data.aspx

mWilcoxonTest

Multivariate Wilcoxon test for equality of dispersion.

Description

Depth based multivariate Wilcoxon test for a scale difference.

Usage

```
mWilcoxonTest(x, y, alternative = "two.sided", depth_params = list())
```

Arguments

X	data matrix
у	data matrix

alternative a character string specifying the alternative hypothesis, must be one of "two.sided"

(default), "greater" or "less".

depth_params list of parameters for function depth (method, threads, ndir, la, lb, pdim, mean,

cov, exact).

mWilcoxonTest 45

Details

Having two samples X^n and Y^m using any depth function, we can compute depth values in a combined sample $Z^{n+m} = X^n \cup Y^m$, assuming the empirical distribution calculated basing on all observations, or only on observations belonging to one of the samples X^n or Y^m .

For example if we observe X'_ls depths are more likely to cluster tightly around the center of the combined sample, while Y'_ls depths are more likely to scatter outlying positions, then we conclude Y^m was drawn from a distribution with larger scale.

Properties of the DD plot based statistics in the i.i.d setting were studied by Li & Liu (2004). Authors proposed several DD-plot based statistics and presented bootstrap arguments for their consistency and good effectiveness in comparison to Hotelling T^2 and multivariate analogues of Ansari-Bradley and Tukey-Siegel statistics. Asymptotic distributions of depth based multivariate Wilcoxon rank-sum test statistic under the null and general alternative hypotheses were obtained by Zuo & He (2006). Several properties of the depth based rang test involving its unbiasedness was critically discussed by Jureckova & Kalina (2012). Basing on DD-plot object, which is available within the **DepthProc** it is possible to define several multivariate generalizations of one-dimensional rank and order statistics in an easy way. These generalizations cover well known Wilcoxon rang-sum statistic.

The depth based multivariate Wilcoxon rang sum test is especially useful for the multivariate scale changes detection and was introduced among other by Liu & Singh (2003) and intensively studied by Jureckowa & Kalina (2012) and Zuo & He (2006) in the i.i.d. setting.

```
For the samples X^m=\{X_1,...,X_m\},\,Y^n=\{Y_1,...,Y_n\}, their d_1^X,...,d_m^X,\,d_1^Y,...,d_n^Y, depths w.r.t. a combined sample Z=X^n\cup Y^m the Wilcoxon statistic is defined as S=\sum\limits_{i=1}^m R_i, where R_i denotes the rang of the i-th observation, i=1,...,m in the combined sample R(y_l)=\sharp\{z_j\in Z:D(z_j,Z)\leq D(y_l,Z)\}, l=1,...,m. The distribution of S is symmetric about E(S)=\frac{1}{2}m(m+n+1), its variance is D^2(S)=\frac{1}{2}m(m+n+1)
```

The distribution of S is symmetric about $E(S) = \frac{1}{2}m(m+n+1)$, its variance is $D^2(S) = \frac{1}{12}mn(m+n+1)$.

References

Jureckova J, Kalina J (2012). Nonparametric multivariate rank tests and their unbiasedness. Bernoulli, 18(1), 229–251. Li J, Liu RY (2004). New nonparametric tests of multivariate locations and scales using data depth. Statistical Science, 19(4), 686–696. Liu RY, Singh K (1995). A quality index based on data depth and multivariate rank tests. Journal of American Statistical Association, 88, 252–260. Zuo Y, He X (2006). On the limiting distributions of multivariate depth-based rank sum statistics and related tests. The Annals of Statistics, 34, 2879–2896.

```
# EXAMPLE 1
x <- mvrnorm(100, c(0, 0), diag(2))
y <- mvrnorm(100, c(0, 0), diag(2) * 1.4)
mWilcoxonTest(x, y)
mWilcoxonTest(x, y, depth_params = list(method = "LP"))
# EXAMPLE 2
data(under5.mort)
data(inf.mort)</pre>
```

46 plot

plot

Method for plotting DepthCurve and DDPlot object.

Description

Plot Depth curve

Usage

```
plot(x, y, ...)
## S4 method for signature 'DDPlot,ANY'
plot(x)
## S4 method for signature 'DepthCurve,ANY'
plot(x)
## S4 method for signature 'DepthCurveList,ANY'
plot(x)
```

Arguments

x object that inherits from DepthCurve class (ScaleCurve or AsymmetryCurve), or DDPlot class.

y not supported.

... not supported.

```
x \leftarrow mvrnorm(n = 100, mu = c(0, 0), Sigma = 3 * diag(2)) sc <- scaleCurve(x) plot(sc)
```

```
plot,BinnDepth2d,ANY-method

2d Binning plot
```

Description

Binning 2d

Usage

```
## S4 method for signature 'BinnDepth2d,ANY'
plot(x, ..., alpha = 0.1, bg_col = "red", add_mid = TRUE)
```

Arguments

X	object of class BinnDepth2d
	graphical parameters passed to plot
alpha	alpha value for rgb function
bg_col	backgroud color
add_mid	logical. If TRUE centers of binns will be marked.

See Also

depth

Examples

```
tmp <- binningDepth2D(x = mvrnorm(100, rep(0, 2), diag(2))) plot(tmp)
```

```
plot,DepthDensity,ANY-method
```

Plot function for DepthDensity.

Description

Create plot for DepthDensity. See depthDensity for more information.

Usage

```
## S4 method for signature 'DepthDensity,ANY'
plot(x, type = "depth", ...)
```

Arguments

```
    x object of class DepthDensity
    type type of density that will be plotted. "depth" is a depth scaled density, and "raw" is denisty without scaling.
    graphical arguments.
```

```
plot, LSDepthContour, ANY-method
```

Plot Location-Scale depth contours.

Description

Create location-scale depth plot. See lsdSampleDepthContours for more information.

Usage

```
## $4 method for signature 'LSDepthContour,ANY'
plot(
    x,
    cont = NULL,
    ratio = 1,
    mu_min = NULL,
    mu_max = NULL,
    col = NULL,
    border = NULL,
    ...
)
```

Arguments

```
object of class LSDepthContour
Х
                  plotted contours. Default NULL means that all contours stored in x will be
cont
                  plotted.
                  ratio
ratio
mu_min
                  mu_min
mu_max
                  mu_max
col
                  vectors with area colors passed to polygon function
                  vector with colors for borders
border
                  other parameters passed to polygon
. . .
```

```
 \begin{split} & \text{smp} <- \text{rf}(100, 5, 10) \\ & \text{x} <- \text{lsdSampleDepthContours(smp)} \\ & \text{plot}(\text{x}, \text{col} = \text{paste0("grey", col} = \text{rev(seq(10, 40, 10)))}) \end{split}
```

RobReg-class 49

RobReg-class RobReg

Description

Virtual class for robust regression methods from depthproc package

Slots

coef coefficients of fitted model

runifsphere

Random number generation from unit sphere.

Description

This function generates random numbers from p-dimensional unit sphere.

Usage

```
runifsphere(n, p = 2)
```

Arguments

- n number of random samples.
- p dimension of the unit sphere.

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

```
x <- runifsphere(n = 100)
plot(x)</pre>
```

50 scaleCurve

scaleCurve

Scale curve

Description

Draws a scale curve: measure of dispersion.

Usage

```
scaleCurve(
    x,
    y = NULL,
    alpha = seq(0, 1, 0.01),
    name = "X",
    name_y = "Y",
    title = "Scale Curve",
    depth_params = list(method = "Projection")
)
```

Arguments

x Multivariate data as a matrix.

y Additional matrix with multivariate data.

alpha Vector with values of central area to be used in computation.

name Name of matrix X used in legend.

Name of matrix Y used in legend.

title title of the plot.

depth_params list of parameters for function depth (method, threads, ndir, la, lb, pdim, mean,

cov, exact).

Details

For sample depth function $D(x,Z^n)$, $x \in R^d$, $d \ge 2$, $Z^n = \{z_1,...,z_n\} \subset R^d$, $D_\alpha(Z^n)$ denoting α — central region, we can define the scale curve $SC(\alpha) = (\alpha, vol(D_\alpha(Z^n)) \subset R^2$, for $\alpha \in [0,1]$

The scale curve is a two-dimensional method of describing the dispersion of random vector around the depth induced median.

Function scalecurve for determining the volumes of the convex hull containing points from alpha central regions, uses function convhulln from geometry package.

The minimal dimension of data in X or Y is 2.

ggplot2 package is used to draw a plot.

Value

Returns the volume of the convex hull containing subsequent central points of X.

ScaleCurve-class 51

Author(s)

Daniel Kosiorowski, Mateusz Bocian, Anna Wegrzynkiewicz and Zygmunt Zawadzki from Cracow University of Economics.

References

Liu, R.Y., Parelius, J.M. and Singh, K. (1999), Multivariate analysis by data depth: Descriptive statistics, graphics and inference (with discussion), *Ann. Statist.*, **27**, 783–858.

Chaudhuri, P. (1996), On a Geometric Notion of Quantiles for Multivariate Data, *Journal of the American Statistical Association*, 862–872.

Dyckerhoff, R. (2004), Data Depths Satisfying the Projection Property, *Allgemeines Statistisches Archiv.*, **88**, 163–190.

See Also

depthContour and depthPersp for depth graphics.

Examples

ScaleCurve-class

ScaleCurve and ScaleCurveList

Description

ScaleCurve is a class that stores results of scaleCurve function.

Details

ScaleCurve intherits behviour from numeric vector, so raw values of ScaleCurve can be accessed via as.numeric(...).

The mechanism of creating plots with multiple curves is shown in DepthCurve-class (same mechanism is applied for AsymmetryCurve).

52 trimProjReg2d

Examples

```
library(mvtnorm)
x <- mvrnorm(n = 100, mu = c(0, 0), Sigma = 2 * diag(2))
y <- rmvt(n = 100, sigma = diag(2), df = 4)
s1 <- scaleCurve(x, depth_params = list(method = "Projection"))
s2 <- scaleCurve(y, depth_params = list(method = "Projection"), name = "Set2")
sc_list <- combineDepthCurves(s1, s2) # Add one curve to another

plot(sc_list) # Draw plot with two curves

z <- mvrnorm(n = 100, mu = c(0, 0), Sigma = 1 * diag(2))
s3 <- scaleCurve(z, depth_params = list(method = "Projection"))
plot(combineDepthCurves(sc_list, s3)) # Add third curve and draw a plot</pre>
```

trimProjReg2d

trimProjReg2d

Description

Computes projection trimmed regression in 2 dimensions.

Usage

```
trimProjReg2d(x, y, alpha = 0.1)
```

Arguments

x Independent variabley Dependent variablealpha Percentage of trimmed observations

Author(s)

Zygmunt Zawadzki from Cracow University of Economics.

```
# EXAMPLE 1
data(pension)
plot(pension)
abline(lm(Reserves ~ Income, data = pension), lty = 3, lwd = 2) # lm
abline(trimProjReg2d(pension[, 1], pension[, 2]), lwd = 2) # trimprojreg2d
legend("bottomright", c("OLS", "TrimLS"), lty = 1:2)
# EXAMPLE 2
data(under5.mort)
```

TrimReg2d-class 53

```
data(inf.mort)
data(maesles.imm)
data2011 <- na.omit(cbind(under5.mort[, 22], inf.mort[, 22],</pre>
                          maesles.imm[, 22]))
x <- data2011[, 3]
y <- data2011[, 2]
plot(x, y, cex = 1.2, ylab = "infant mortality rate per 1000 live birth",
     xlab = "against masles immunized percentage",
     main = "Projection Depth Trimmed vs. LS regressions")
abline(lm(x \sim y), lwd = 2, col = "black") # lm
abline(trimProjReg2d(x, y), lwd = 2, col = "red") # trimmed reg
legend("bottomleft", c("LS", "TrimReg"), fill = c("black", "red"), cex = 1.4,
       bty = "n")
##### Comparsion of a few regression methods #####
library(DepthProc)
library(MASS)
data("france")
plot(UR ~ MW, pch = 19, data = france)
# linear regression
lm.fit <- lm(UR ~ MW, data = france)</pre>
abline(lm.fit, lwd=2, cex=3, col='red')
# M-estimator
rlm.fit <- rlm(UR ~ MW, data = france)</pre>
abline(rlm.fit, lwd = 2,col = "blue")
# LMS
lqs.lms <- lqs(UR ~ MW, method = "lms", data = france) #least median of squares#
lqs.lts <- lqs(UR ~ MW, method = "lts", data = france) #least trimmed squares#
abline(lqs.lms, lwd = 2, col="green")
abline(lqs.lts, lwd = 2, col="pink")
# Lowess
lines(lowess(france$MW, france$UR, f = 0.5, iter = 0), lwd = 2) # loess
# Depth trimmed regression
trim.reg <- trimProjReg2d(france$MW, france$UR) #trimprojreg2d</pre>
abline(trim.reg, lwd = 4, col = 'orange')
```

TrimReg2d-class

TrimReg2d

Description

Class for robust regression methods from depthproc package

54 USLABOUR

under5.mort

Children under 5 months mortality rate per 1,000 live births

Description

Children under 5 months mortality rate per 1,000 live births

Usage

```
data(under5.mort)
```

Format

A data frame with 654 rows and 4 variables

Source

http://mdgs.un.org/unsd/mdg/Data.aspx

USLABOUR

US Labour dataset

Description

US Labour dataset

Usage

data(USLABOUR)

Format

A data frame with 654 rows and 4 variables

Source

U.S.Department of Labor — Bureau of Labour Statistics FRED

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