CCREPE: Compositionality Corrected by PErmutation and REnormalization

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1 Introduction

ccrepe is a package for analysis of sparse compositional data. Specifically, it determines the significance of association between features in a composition, using any similarity measure (e.g. Pearson correlation, Spearman correlation, etc.) The CCREPE methodology stands

for Compositionality Corrected by Renormalization and Permutation, as detailed below. The package also provides a novel similarity measure, the N-dimensional checkerboard score (NC-score), particularly appropriate to compositions derived from microbial community sequencing data. This results in p-values and false discovery rate q-values corrected for the effects of compositionality. The package contains two functions ccrepe and nc.score and is maintained by the Huttenhower lab (ccrepe-users@googlegroups.com).

2 ccrepe

ccrepe is the main package function. It calculates compositionality-corrected p-values and q-values for a user-selected similarity measure, operating on either one or two input matrices. If given one matrix, all features (columns) in the matrix are compared to each other using the selected similarity measure. If given two matrices, each feature in the first are compared against all features in the second.

2.1 General functionality

Compositional data induces spurious correlations between features due to the nonindependence of values that must sum to a fixed total. CCREPE abrogates this when determining the significance of a similarity measure for each feature pair using two main steps, permutation/renormalization and bootstrapping. First, given two features to compare, CCREPE generates a null distribution of the similarity expected just due to compositionality by iteratively permuting one feature, renormalizing all samples in the composition to their previous sum, and computing the resulting similarity measures. Second, CCREPE bootstraps over sample subsets in order to assess confidence in the "true" similarity measure. Finally, the two resulting distributions are compared using a pooled-variance Z-test to give a compositionality-corrected p-value. False discovery rate q-values are additionally calculated using the Benjamin-Hochberg-Yekutieli procedure. For greater detail, see Faust et al. [2012] and Schwager and Colleagues.

CCREPE employs several filtering steps before the data are processed. It removes any missing subjects using na.omit: in the two dataset case, any subjects missing in *either* dataset will be removed. Any subjects or features which are all zero are removed as well: an all-zero subject cannot be normalized (its sum is 0) and an all-zero feature has standard deviation 0 (in addition to being uninteresting biologically).

2.2 Arguments

- x First dataframe or matrix containing relative abundances. Columns are features, rows are samples. Rows should therefore sum to a constant. Row names are used for identification if present.
- y Second *dataframe* or *matrix* (optional) containing relative abundances. Columns are features, rows are samples. Rows should therefore sum to a constant. If both x and y are specified, they will be merged by row names. If no row names are specified for either or both datasets, the default is to merge by row number.

sim.score Similarity measure, such as cor or nc.score. This can be either an existing R function or user-defined. If the latter, certain properties should be satisfied as detailed below (also see examples). The default similarity measure is Spearman correlation.

A user-defined similarity measure should mimic the interface of cor:

- 1. Take either two *vector* inputs one *matrix* or *dataframe* input.
- 2. In the case of two inputs, return a single number.
- 3. In the case of one input, return a matrix in which the (i,j)th entry is the similarity score for column i and column j in the original matrix.
- 4. The resulting matrix (in the case of one input) must be symmetric.
- 5. The inputs must be named x and y.
- sim.score.args An optional list of arguments for the measurement function. When given, they are passed to the sim.score function directly. For example, in the case of cor, the following would be acceptable:

sim.score.args = list(method="spearman", use="complete.obs")

- min.subj Minimum number (count) of samples that must be non-missing in order to apply the similarity measure. This is to ensure that there are sufficient samples to perform a bootstrap (default: 20).
- **iterations** The number of iterations for both bootstrap and permutation calculations (de-fault: 1000).
- subset.cols.x A vector of column indices from x to indicate which features to compare
- subset.cols.y A vector of column indices from y to indicate which features to compare
- ${\it errthresh}$ If feature has number of zeros greater than $\ errthresh^{1/n}$, that feature is excluded
- verbose If TRUE, print periodic progress of the algorithm through the dataset(s), as well as including more detailed debugging output. (default: FALSE).
- **iterations.gap** If verbose=TRUE, the number of iterations between issuing status messages (default: 100).
- distributions Optional output file for detailed log (if given) of all intermediate permutation and renormalization distributions.
- compare.within.x A boolean value indicating whether to do comparisons given by taking all subsets of size 2 from subset.cols.x or to do comparisons given by taking all possible combinations of subset.cols.x and subset.cols.y. If TRUE but subset.cols.y=NA, returns all comparisons involving any features in subset.cols.x. This argument is only used when y=NA.

concurrent.output Optional output file to which each comparison will be written as it is calculated.

make.output.table A boolean value indicating whether to include table-formatted output.

2.3 Output

ccrepe returns a *list* containing both the calculation results and the parameters used:

- sim.score matrix of similarity scores for all requested comparisons. The (i,j)th element corresponds to the similarity score of column i (or the ith column of subset.cols.1) and column j (or the jth column of subset.cols.1) in one dataset, or to the similarity score of column i (or the ith column of subset.cols.1) in dataset x and column j (or the jth column of subset.cols.2) in dataset y in the case of two datasets.
- **p.values** matrix of the corrected p-values for all requested comparisons. The (i,j)th element corresponds to the p-value of the (i,j)th element of sim.score.
- **q.values** matrix of the Benjamini-Hochberg-Yekutieli corrected p-values. The (i,j)th element corresponds to the p-value of the (i,j)th element of sim.score.
- z.stat matrix of the z-statistics used in generating the p-values for all requested comparisons. The (i,j)th element corresponds to the z-statistic generating the (i,j)th element of p.values.

2.4 Usage

```
ccrepe(
x = NA,
y = NA,
sim.score = cor,
sim.score.args = list(),
min.subj = 20,
iterations = 1000,
subset.cols.x = NULL,
subset.cols.y = NULL,
errthresh = 1e - 04,
verbose = FALSE,
iterations.gap = 100,
distributions = NA,
compare.within.x = TRUE,
concurrent.output = NA,
make.output.table = FALSE)
```

2.5 Example 1

An example of how to use ccrepe with one dataset.

```
data <- matrix(rlnorm(40,meanlog=0,sdlog=1),nrow=10,ncol=4)</pre>
data[,1] = 2*data[,2] + rnorm(10,0,0.01)
data.rowsum <- apply(data,1,sum)</pre>
data.norm <- data/data.rowsum
apply(data.norm,1,sum) # The rows sum to 1, so the data are normalized
## [1] 1 1 1 1 1 1 1 1 1 1
test.input <- data.norm</pre>
dimnames(test.input) <- list(c(</pre>
 "Sample 1", "Sample 2", "Sample 3", "Sample 4", "Sample 5",
 "Sample 6", "Sample 7", "Sample 8", "Sample 9", "Sample 10"),
 c("Feature 1", "Feature 2", "Feature 3", "Feature 4"))
test.output <- ccrepe(x=test.input, iterations=20, min.subj=10)</pre>
par(mfrow=c(1,2))
plot(data[,1],data[,2],xlab="Feature 1",ylab="Feature 2",main="Non-normalized")
plot(data.norm[,1],data.norm[,2],xlab="Feature 1",ylab="Feature 2",
     main="Normalized")
```





Figure 1: Non-normalized and normalized associations between feature 1 and feature 2 In this case we would expect feature 1 and feature 2 to be associated. In the output we see this by the positive sim.score value in the [1,2] element of test.output\$sim.score and the small q-value in the [1,2] element of test.output\$q.values.

```
test.output
## $p.values
##
                Feature 1
                             Feature 2 Feature 3 Feature 4
                       NA 8.573412e-09 0.7331363 0.3909805
## Feature 1
## Feature 2 8.573412e-09
                                    NA 0.9482526 0.1225692
## Feature 3 7.331363e-01 9.482526e-01
                                               NA 0.7851792
## Feature 4 3.909805e-01 1.225692e-01 0.7851792
                                                         NA
##
## $z.stat
##
              Feature 1
                          Feature 2
                                      Feature 3 Feature 4
```

```
## Feature 1 NA 5.75677883 0.34095654 -0.8578406
## Feature 2 5.7567788 NA -0.06490133 -1.5440789
## Feature 3 0.3409565 -0.06490133
                                        NA -0.2725759
## Feature 4 -0.8578406 -1.54407889 -0.27257589
                                                  NA
##
## $sim.score
##
     Feature 1 Feature 2 Feature 3 Feature 4
## Feature 1 NA 0.9999313 -0.3305689 -0.7218832
## Feature 2 0.9999313 NA -0.3245007 -0.7262973
## Feature 3 -0.3305689 -0.3245007
                                     NA -0.4144722
## Feature 4 -0.7218832 -0.7262973 -0.4144722
                                                NA
##
## $q.values
##
             Feature 1 Feature 2 Feature 3 Feature 4
## Feature 1 NA 1.218612e-07 2.605173 1.8524462
## Feature 2 1.218612e-07 NA 2.246387 0.8710903
                                         NA 2.2320841
## Feature 3 2.605173e+00 2.246387e+00
## Feature 4 1.852446e+00 8.710903e-01 2.232084
                                                  NΑ
```

2.6 Example 2

An example of how to use ccrepe with two datasets.

```
data <- matrix(rlnorm(40,meanlog=0,sdlog=1),nrow=10,ncol=4)</pre>
data[,1] = 2*data[,2] + rnorm(10,0,0.01)
data.rowsum <- apply(data,1,sum)</pre>
data.norm <- data/data.rowsum</pre>
apply(data.norm,1,sum) # The rows sum to 1, so the data are normalized
## [1] 1 1 1 1 1 1 1 1 1 1
test.input <- data.norm
data2 <- matrix(rlnorm(105,meanlog=0,sdlog=1),nrow=15,ncol=7)</pre>
aligned.rows <- c(seg(1,4), seg(6,9), 11, 12) # The datasets dont need
                                               # to have subjects line up exactly
data2[aligned.rows,1] <- 2*data[,3] + rnorm(10,0,0.01)</pre>
data2.rowsum <- apply(data2,1,sum)</pre>
data2.norm <- data2/data2.rowsum</pre>
apply(data2.norm,1,sum) # The rows sum to 1, so the data are normalized
## [1] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
test.input.2 <- data2.norm</pre>
dimnames(test.input) <- list(paste("Sample", seq(1,10)), paste("Feature", seq(1,4)))</pre>
dimnames(test.input.2) <- list(paste("Sample", c(seq(1,4), 11, seq(5,8), 12, 9, 10, 13, 14, 15)), paste("Feature", seq(</pre>
test.output.two.datasets <- ccrepe(x=test.input, y=test.input.2, iterations=20, min.subj=10)</pre>
```

```
## Warning in preprocess_data(CA): Removing subjects Sample 11, Sample 12, Sample
13, Sample 14, Sample 15 from dataset y because they are not in dataset x.
```

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Please note that we receive a warning because the subjects don't match - only paired observations.



Figure 2: Non-normalized and normalized associations between feature 1 and feature 2 In this case we would expect feature 1 and feature 2 to be associated. In the output we see this by the positive sim.score value in the [1,2] element of test.output\$sim.score and the small q-value in the [1,2] element of test.output\$q.values.

```
test.output.two.datasets
```

```
## $p.values
##
               Feature 1 Feature 2 Feature 3 Feature 4 Feature 5 Feature 6
## Feature 1 0.847956207 0.7274587 0.4273717 0.63592307 0.3071794 0.4738992
## Feature 2 0.647639168 0.7037248 0.7356738 0.36334917 0.2876963 0.6458935
## Feature 3 0.009035582 0.1032896 0.6271319 0.05858394 0.5242910 0.9310562
## Feature 4 0.292344371 0.3486323 0.5550629 0.21109657 0.1742696 0.5097704
##
             Feature 7
## Feature 1 0.2600484
## Feature 2 0.2571129
## Feature 3 0.4951129
## Feature 4 0.3055695
##
## $z.stat
              Feature 1 Feature 2 Feature 3 Feature 4 Feature 5
##
                                                                      Feature 6
## Feature 1 -0.1917268 -0.3485080 -0.7936972 -0.4734067 1.0211583 0.71614923
## Feature 2 0.4570444 -0.3802973 -0.3375879 -0.9090018 1.0631889
                                                                     0.45947439
## Feature 3 2.6107049 -1.6291106 -0.4857676 -1.8913028 0.6367449 0.08651599
## Feature 4 -1.0529926 0.9372456 0.5901906 1.2505558 -1.3586120 -0.65919532
##
              Feature 7
## Feature 1 -1.1262767
## Feature 2 -1.1332414
## Feature 3 -0.6821993
## Feature 4 1.0245628
##
```

```
## $sim.score
##
               Feature 1 Feature 2 Feature 3 Feature 4
                                                           Feature 5
## Feature 1 -0.012251973 -0.2656656 -0.4510982 0.09702061 0.28529670
## Feature 2 -0.003044496 -0.2762636 -0.4466416 0.10278514 0.27938733
## Feature 3 0.819528248 -0.3775869 -0.2948543 -0.45927849 0.09756766
## Feature 4 -0.293424585 0.3918625 0.5307292 0.07639391 -0.30192272
##
              Feature 6 Feature 7
## Feature 1 0.34840438 -0.20135946
## Feature 2 0.34464995 -0.19675594
## Feature 3 -0.02541462 -0.01669655
## Feature 4 -0.31651048 0.19373236
##
## $q.values
           Feature 1 Feature 2 Feature 3 Feature 4 Feature 5 Feature 6
##
## Feature 1 3.4377955 3.185215 3.341551 3.314787 3.056820 3.458319
## Feature 2 3.0823053 3.209682 3.097293 3.059505 3.936540 3.213724
## Feature 3 0.9890688 3.768823 3.432411 3.206409 3.188382 3.639890
## Feature 4 3.5556795 3.180217 3.197857 4.621485 4.769051 3.282434
##
            Feature 7
## Feature 1 4.066554
## Feature 2 4.690758
## Feature 3 3.387308
## Feature 4 3.344879
```

2.7 Example 3

An example of how to use ccrepe with nc.score as the similarity score.

```
data <- matrix(rlnorm(40,meanlog=0,sdlog=1),nrow=10,ncol=4)
data[,1] = 2*data[,2] + rnorm(10,0,0.01)
data.rowsum <- apply(data,1,sum)
data.norm <- data/data.rowsum
apply(data.norm,1,sum) # The rows sum to 1, so the data are normalized
## [1] 1 1 1 1 1 1 1 1 1
test.input <- data.norm
dimnames(test.input) <- list(paste("Sample",seq(1,10)),paste("Feature",seq(1,4)))
test.output.nc.score <- ccrepe(x=test.input, sim.score=nc.score, iterations=20, min.subj=10)
par(mfrow=c(1,2))
plot(data[,1],data[,2],xlab="Feature 1",ylab="Feature 2",main="Non-normalized")
plot(data.norm[,1],data.norm[,2],xlab="Feature 1",ylab="Feature 2",main="Non-normalized")</pre>
```

```
main="Normalized")
```



Figure 3: Non-normalized and normalized associations between feature 1 and feature 2 In this case we would expect feature 1 and feature 2 to be associated. In the output we see this by the positive sim.score value in the [1,2] element of test.output\$sim.score and the small q-value in the [1,2] element of test.output\$q.values. In this case, however, the sim.score represents the NC-Score between two features rather than the Spearman correlation.

```
test.output.nc.score
## $p.values
                Feature 1
                            Feature 2 Feature 3 Feature 4
##
## Feature 1
                      NA 7.654382e-08 0.3800029 0.34976867
## Feature 2 7.654382e-08
                                    NA 0.4940947 0.07892183
## Feature 3 3.800029e-01 4.940947e-01
                                              NA 0.15214635
## Feature 4 3.497687e-01 7.892183e-02 0.1521463
                                                         NA
##
## $z.stat
##
              Feature 1 Feature 2 Feature 3 Feature 4
                    NA 5.3750914 -0.8778909 -0.9350381
## Feature 1
## Feature 2 5.3750914
                                NA -0.6838108 -1.7569764
## Feature 3 -0.8778909 -0.6838108
                                           NA 1.4319912
## Feature 4 -0.9350381 -1.7569764 1.4319912
                                                      NA
##
## $sim.score
##
             Feature 1 Feature 2 Feature 3 Feature 4
                         0.8125 -0.59375 -0.65625
## Feature 1
                   NA
## Feature 2
              0.81250
                             NA
                                 -0.50000 -0.81250
## Feature 3 -0.59375
                        -0.5000
                                        NA
                                             0.34375
##
  Feature 4 -0.65625
                        -0.8125
                                  0.34375
                                                  NA
##
## $q.values
                            Feature 2 Feature 3 Feature 4
##
                Feature 1
## Feature 1
                      NA 1.087982e-06 1.0802610 1.2428899
## Feature 2 1.087982e-06
                                   NA 1.1704980 0.5608915
## Feature 3 1.080261e+00 1.170498e+00
                                             NA 0.7208618
## Feature 4 1.242890e+00 5.608915e-01 0.7208618
                                                        NA
```

2.8 Example 4

An example of how to use ccrepe with a user-defined sim.score function.

```
data <- matrix(rlnorm(40,meanlog=0,sdlog=1),nrow=10,ncol=4)
data[,1] = 2*data[,2] + rnorm(10,0,0.01)
data.rowsum <- apply(data,1,sum)
data.norm <- data/data.rowsum
apply(data.norm,1,sum) # The rows sum to 1, so the data are normalized
## [1] 1 1 1 1 1 1 1 1 1 1
test.input <- data.norm
dimnames(test.input) <- list(paste("Sample",seq(1,10)),paste("Feature",seq(1,4)))
my.test.sim.score <- function(x,y=NA,constant=0.5){
    if(is.vector(x) && is.vector(y)) return(constant)
        if(is.matrix(x) && is.na(y)) return(matrix(rep(constant,ncol(x)^2),ncol=ncol(x)))
        if(is.data.frame(x) && is.na(y)) return(matrix(rep(constant,ncol(x)^2),ncol=ncol(x)))
        else stop('ERROR')
    }
```

test.output.sim.score <- ccrepe(x=test.input, sim.score=my.test.sim.score, iterations=20, min.subj=10, sin</pre>



Figure 4: Non-normalized and normalized associations between feature 1 and feature 2 In this case we would expect feature 1 and feature 2 to be associated. Note that the values of sim.score are all 0.6 and none of the p-values are very small because of the arbitrary definition of the similarity score.

```
test.output.sim.score
## $p.values
## Feature 1 Feature 2 Feature 3 Feature 4
## Feature 1 NA NaN NaN NaN
```

```
## Feature 2
                                         NaN
                                                    NaN
                    NaN
                               NA
## Feature 3
                    NaN
                               NaN
                                          NA
                                                    NaN
## Feature 4
                    NaN
                               NaN
                                         NaN
                                                    NA
##
## $z.stat
## Feature 1 Feature 2 Feature 3 Feature 4
## Feature 1 NA NaN
                                        NaN
                                                    NaN
## Feature 2NaN## Feature 3NaN## Feature 4NaN
                              NA
                                         NaN
                                                    NaN
                             NaN
                                         NA
                                                    NaN
                              NaN
                                         NaN
                                                    NA
##
## $sim.score
## Feature 1 Feature 2 Feature 3 Feature 4
## Feature 1 NA 0.6 0.6
                                                    0.6

        ## Feature 2
        0.6
        NA

        ## Feature 3
        0.6
        0.6

        ## Feature 4
        0.6
        0.6

                              NA
                                         0.6
                                                    0.6
                                         NA
                                                    0.6
                              0.6
                                         0.6
                                                    NA
##
## $q.values
## Feature 1 Feature 2 Feature 3 Feature 4
## Feature 1
               NA NaN
                                         NaN
                                                    NaN
## Feature 2 NaN
## Feature 3 NaN
                              NA
                                         NaN
                                                    NaN
                              NaN
                                         NA
                                                    NaN
                NaN
## Feature 4
                              NaN
                                         NaN
                                                     NA
```

2.9 Example 5

An example of how to use ccrepe when specifying column subsets.

```
data <- matrix(rlnorm(40,meanlog=0,sdlog=1),nrow=10,ncol=4)</pre>
data.rowsum <- apply(data,1,sum)</pre>
data.norm <- data/data.rowsum</pre>
apply(data.norm,1,sum) # The rows sum to 1, so the data are normalized
## [1] 1 1 1 1 1 1 1 1 1 1
test.input <- data.norm</pre>
dimnames(test.input) <- list(paste("Sample", seq(1,10)), paste("Feature", seq(1,4)))</pre>
test.output.1.3
                   <- ccrepe(x=test.input, iterations=20, min.subj=10, subset.cols.x=c(1,3))
                   <- ccrepe(x=test.input, iterations=20, min.subj=10, subset.cols.x=c(1), compare.within.x=
test.output.1
test.output.12.3 <- ccrepe(x=test.input, iterations=20, min.subj=10, subset.cols.x=c(1,2),subset.cols.y=c</pre>
test.output.1.3$sim.score
##
             Feature 1 Feature 3
## Feature 1 NA -0.2989951
## Feature 3 -0.2989951 NA
test.output.1$sim.score
##
               Feature 1 Feature 2 Feature 3 Feature 4
                 NA -0.4585934 -0.2989951 -0.02703028
## Feature 1
```

<pre>## Feature 2 ## Feature 3</pre>				-	NA NA
## Feature 4	0.20000020			-	NA
test.output.12.3\$sim.score					
##	Feature 1	Feature 2	Feature 3	Feature 4	
## Feature 1	NA	NA	-0.2989951	NA	
## Feature 2	NA	NA	-0.2313468	NA	
## Feature 3	-0.2989951	-0.2313468	NA	NA	

3 nc.score

The nc.score similarity measure is an N-dimensional extension of the checkerboard score particularly suited to similarity score calculations between compositions derived from ecological relative abundance measurements. In such cases, features typically represent species abundances, and the NC-score discretizes these continuous values into one of N bins before computing a normalized similarity of co-occurrence or co-exclusion. This can be used as a standalone function or with ccrepe as above to obtain compositionality-corrected p-values.

3.1 General Functionality

The NC-score is an extension to Diamond's checkerboard score (see Cody and Diamond [1975]) to ordinal data, and simplifies to a calculation of Kendall's τ on binned data instead of ranked data. Let two features in a dataset with n subjects be denoted by

Γ	x_1	x_2	 x_n]
L	y_1	y_2	 y_n] .

The binning function maps from the original data to b numbered bins in $\{1, ..., b\}$. Let the binning function be denoted by $B(\cdot)$. The co-variation and co-exclusion patterns are the same as concordant and discordant pairs in Kendall's τ . Considering a 2×2 submatrix of the form

$\begin{bmatrix} B(x_i) \end{bmatrix}$	$B(x_j)$	
$B(y_i)$	$B(y_j)$,

a co-variation pattern is counted when $(B(x_i) - B(x_j))(B(y_i) - B(y_j)) > 0$ and a co-exclusion pattern, conversely, when $(B(x_i) - B(x_j))(B(y_i) - B(y_j)) < 0$. The NC-score statistic for features x and y is then defined as

(number of co-variation patterns) – (number of co-exclusion patterns),

normalized by the Kendall's τ normalization factor accounting for ties described in Kendall [1970].

3.2 Arguments

x First numerical *vector*, or single *dataframe* or *matrix*, containing relative abundances. If the latter, columns are features, rows are samples. Rows should therefore sum to a constant.

- y If provided, second numerical *vector* containing relative abundances. If given, x must be a *vector* as well.
- **nbins** A non-negative integer of the number of bins to generate (cutoffs will be generated by the discretize function from the infotheo package).
- **bin.cutoffs** A list of values demarcating the bin cutoffs. The binning is performed using the findInterval function.
- use An optional character string givinga method for computing covariances in the presence of missing values. This must be (an abbreviaion of) on of the strings "everything", "all.obs", "complete.obs", "na.or.complete", or "pairwise.complete.obs".

3.3 Output

nc.score returns either a single number (if called with two vectors) or a *matrix* of all pairwise scores (if called with a *matrix*) of normalized scores. This behaviour is precisely analogous to the cor function in R

3.4 Usage

```
nc.score(
    x,
    y = NULL,
    use = "everything",
    nbins = NULL,
    bin.cutoffs=NULL)
```

3.5 Example 1

An example of using nc.score to get a single similarity score or a matrix.

```
data <- matrix(rlnorm(40,meanlog=0,sdlog=1),nrow=10,ncol=4)
data.rowsum <- apply(data,1,sum)
data[,1] = 2*data[,2] + rnorm(10,0,0.01)
data.norm <- data/data.rowsum
apply(data.norm,1,sum) # The rows sum to 1, so the data are normalized
## [1] 1.2350789 0.5795900 1.0304077 0.7010814 1.4731699 0.9181681 2.2812828
## [8] 1.1264995 0.9960406 2.0174150
test.input <- data.norm
dimnames(test.input) <- list(paste("Sample",seq(1,10)),paste("Feature",seq(1,4)))
test.output.matrix <- nc.score(x=test.input)
test.output.num <- nc.score(x=test.input[,1],y=test.input[,2])
par(mfrow=c(1, 2))
plot(data[,1],data[,2],xlab="Feature 1",ylab="Feature 2",main="Non-normalized")</pre>
```

CCREPE: Compositionality Corrected by PErmutation and REnormalization



Figure 5: Non-normalized and normalized associations between feature 1 and feature 2 of the second example Again, we expect to observe a positive association between feature 1 and feature 2. In terms of generalized checkerboard scores, we would expect to see more co-variation patterns than co-exclusion patterns. This is shown by the positive and relatively high value of the [1,2] element of test.output.matrix (which is identical to test.output.num)

```
test.output.matrix
```

```
##
             Feature 1 Feature 2 Feature 3 Feature 4
## Feature 1
                1.000
                           1.000
                                   0.12500
                                             0.00000
## Feature 2
                 1.000
                           1.000
                                   0.12500
                                             0.00000
## Feature 3
                 0.125
                           0.125
                                   1.00000 -0.59375
## Feature 4
                 0.000
                           0.000
                                 -0.59375
                                             1.00000
test.output.num
```

test.output.n

[1] 1

3.6 Example 2

An example of using nc.score with an aribitrary bin number.



Figure 6: Non-normalized and normalized associations between feature 1 and feature 2 of the second example Again, we expect to observe a positive association between feature 1 and feature 2. In terms of generalized checkerboard scores, we would expect to see more co-variation patterns than co-exclusion patterns. This is shown by the positive and relatively high value in the [1,2] element of test.output. In this case, the smaller bin number yields a smaller NC-score because of the coarser partitioning of the data.

```
test.output

## Feature 1 Feature 2 Feature 3 Feature 4

## Feature 1 1.00000000 1.0000000 -0.22857143 -0.02857143

## Feature 2 1.00000000 1.0000000 -0.22857143 -0.02857143

## Feature 3 -0.22857143 -0.22857143 1.0000000 0.05714286

## Feature 4 -0.02857143 -0.02857143 0.05714286 1.00000000
```

3.7 Example 3

An example of using nc.score with user-defined bin edges.



Figure 7: Non-normalized and normalized associations between feature 1 and feature 2 of the second example Again, we expect to observe a positive association between feature 1 and feature 2. In terms of generalized checkerboard scores, we would expect to see more co-variation patterns than co-exclusion patterns. This is shown by the positive and relatively high value in the [1,2] element of test.output. The bin edges specified here represent almost absent ([0,0.001)), low abundance ([0.001,0.1)), medium abundance ([0.1,0.25)), and high abundance ([0.6,1)).

ccsc.oucpuc				
##	Feature 1	Feature 2	Feature 3	Feature 4
## Feature 1	1.0000000	1.0000000	-0.4493457	0.0000000
## Feature 2	1.0000000	1.0000000	-0.4493457	0.0000000
## Feature 3	-0.4493457	-0.4493457	1.0000000	-0.2428707
## Feature 4	0.0000000	0.0000000	-0.2428707	1.0000000

4 References

test output

References

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