

Package ‘randRotation’

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Title Random Rotation Methods for High Dimensional Data with Batch Structure

Version 1.0.0

Description A collection of methods for performing random orthogonal transformations (random rotations) on high-dimensional data (e.g. microarray or RNA-seq data) with batch structure. The random rotation approach allows exact testing of dependent test statistics with linear models following arbitrary, particularly non-linear, batch effect correction methods. The package further provides methods for estimating the local degrees of freedom of data mappings.

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randRotation-package *randRotation: Random Rotation Methods for High Dimensional Data with Batch Structure*

Description

A collection of methods for performing random orthogonal transformations (random rotations) on high-dimensional data (e.g. microarray or RNA-seq data) with batch structure. The random rotation approach allows exact testing of dependent test statistics with linear models following arbitrary, particularly non-linear, batch effect correction methods. The package further provides methods for estimating the local degrees of freedom of data mappings.

Details

Please refer to the package vignette for further details on usage and for a "quick start". `rotateStat` is basically the central function of the package.

Author(s)

Maintainer: Peter Hettegger <p.hettegger@gmail.com> ([ORCID](#))

See Also

Useful links:

- <https://github.com/phettegger/randRotation>
- Report bugs at <https://github.com/phettegger/randRotation/issues>

df_estimate	<i>Estimation of degrees of freedom (df) for an arbitrary mapping function</i>
-------------	--

Description

This function estimates the local degrees of freedom (df) of mapped data for an arbitrary mapping function. The estimation is done for a set of selected features.

Usage

```
df_estimate(
  data,
  features = sample(nrow(data), 10),
  mapping,
  ...,
  delta = sqrt(.Machine$double.eps)
)
```

Arguments

data	A numerical data matrix.
features	Features for which the df should be estimated (default <code>sample(nrow(data), 10)</code>).
mapping	A mapping function that takes a matrix <code>features x samples</code> dimensions as first argument and returns a matrix of mapped data with the same dimensions. Any further arguments can be passed to <code>mapping</code> through <code>...</code>
...	Additional arguments passed to <code>mapping</code> .
delta	A numeric delta for the finite differences (default <code>sqrt(.Machine\$double.eps)</code>).

Details

The df are estimated as the rank of the local Jacobian matrix. It is thus the rank of the local linear approximation of the mapping function, where linearisation is performed around `data`. The Jacobian matrix `J` for a certain feature `j` is calculated with finite differences:

```
data2 <- data
data2[j, i] <- data2[j, i] + delta
J[, i] = (mapping(data2, ...) - mapping(data, ...)) / delta
```

In the current implementation, the rank of `J` is calculated as sum of the singular values of `J`. So for each feature, a SVD decomposition of the `ncol(data) x ncol(data)` matrix `J` is calculated.

This function should be considered experimental due to the common numerical issues associated with finite differences and numerical calculation of matrix ranks. So always check results for plausibility.

An estimation of df is generated for each feature.

Value

A named numeric vector of estimated df for each feature. Names correspond to features.

Examples

```
#set.seed(0)

# Dataframe of phenotype data (sample information)
# We simulate 2 sample classes processed in 3 batches
pdata <- data.frame(batch = rep(1:3, c(10,10,10)),
                    phenotype = rep(c("Control", "Cancer"), c(5,5)))
features <- 100

# Matrix with random gene expression data
edata <- matrix(rnorm(features * nrow(pdata)), features)
rownames(edata) <- paste("feature", 1:nrow(edata))

mod1 <- model.matrix(~phenotype, pdata)

# The Combat function is a commonly used (mapping) function for batch effect correction:
mapping <- function(Y, batch, mod) {
  sva::ComBat(Y, batch, mod)
}

dfs <- df_estimate(edata, features = 1, mapping = mapping, batch = pdata$batch, mod = mod1)
dfs
```

dim,initRandrot-method

Dimensions of an Object

Description

Retrieve the dimensions of an object.

Usage

```
## S4 method for signature 'initRandrot'
dim(x)

## S4 method for signature 'initBatchRandrot'
dim(x)
```

Arguments

x An object of class `initRandrot-class` or `initBatchRandrot-class`.

Value

Vector of length two with number of features and number of samples. See also `initRandrot`.

dimnames,initRandrot-method

Dimnames of an Object

Description

Retrieve the dimnames of an object.

Usage

```
## S4 method for signature 'initRandrot'  
dimnames(x)
```

```
## S4 method for signature 'initBatchRandrot'  
dimnames(x)
```

Arguments

x An object of class [initRandrot-class](#) or [initBatchRandrot-class](#).

Value

A list with names of features and samples, see [initRandrot](#).

initBatchRandrot-class

Initialised random rotation batch object

Description

This class contains [initRandrot](#) or [initRandrotW](#) class objects for each batch. See also descriptions in [initRandrot](#) and [initRandrot-class](#).

Components

batch.obj List of [initRandrot](#) or [initRandrotW](#) class objects for each batch.

split.by List of sample indices for each batch.

Author(s)

Peter Hettegger

initRandrot

Initialisation of a random rotation Object

Description

Initialization of a linear model for subsequent generation of randomly rotated data (`randrot`) associated with the null hypothesis $H_0 : \beta_{coef.h} = 0$. Basics of rotation tests are found in (Langsrud 2005).

Usage

```
initRandrot(Y = NULL, X = NULL, coef.h = NULL, weights = NULL, cormat = NULL)
```

```
initBatchRandrot(
  Y = NULL,
  X = NULL,
  coef.h = NULL,
  batch = NULL,
  weights = NULL,
  cormat = NULL
)
```

```
## S4 method for signature 'list'
```

```
initBatchRandrot(
  Y = NULL,
  X = Y$design,
  coef.h = NULL,
  batch = NULL,
  weights = Y$weights,
  cormat = NULL
)
```

```
## S4 method for signature 'list'
```

```
initRandrot(
  Y = NULL,
  X = Y$design,
  coef.h = NULL,
  weights = Y$weights,
  cormat = NULL
)
```

Arguments

- | | |
|---|--|
| Y | a data matrix with features x samples dimensions or a list with elements E, design and weights (see Details). Missing values (NA) are allowed but e.g. lead to NAs for all samples of the respective features in the rotated dataset and should thus be avoided. We highly recommend avoiding missing values by e.g. replacing them by imputation or removing features containing NAs. |
| X | the design matrix of the experiment with samples x coefficients dimensions. For <code>initBatchRandrot</code> , specify the design matrix without the batch variable. A warning is generated if <code>X[, coef.d]</code> does not have full rank, see Details. |

coef.h	single integer or vector of integers specifying the "hypothesis coefficients" (H_0 coefficients). coef.h should correspond to the last columns in X (see Details). By default, all coefficients are set as H_0 coefficients. If coef.h is set -1, no coefficient is set as H_0 coefficient.
weights	numerical matrix of finite positive weights > 0 (as in weighted least squares regression). Dimensions must be equal to dimensions of Y .
cormat	the sample correlation matrix with <code>samples x samples</code> dimensions. Must be a real symmetric positive-definite square matrix. See Details for usage in <code>initBatchRandrot</code> .
batch	Batch covariate of the same length as <code>ncol(Y)</code> .

Details

This function performs basic initial checks and preparatory calculations for random rotation data generation, see (Langsrud 2005). Nomenclature of variables is mainly as in (Langsrud 2005). See also package `vignette` for application examples.

Y can also be a list with elements `E`, `design` and `weights`. `Y$E` is thereby used as Y , `Y$design` is used as X and `Y$weights` is used as `weights`. By this, the functions are compatible with results from e.g. `voom` (`limma` package), see Examples.

`coef.h` specifies the model coefficients associated with the null hypothesis ("hypothesis coefficients"). All other model coefficients are considered as "determined coefficients" `coef.d` (Langsrud 2005). The design matrix is rearranged so that `coef.h` correspond to the last columns of the design matrix and `coef.d` correspond to the first columns of the design matrix. This is necessary for adequate transformation of the combined null-hypothesis $H_0 : \beta_{coef.h} = 0$ by QR decomposition. If `X[,coef.d]` does not have full rank, a warning is generated and `coef.d` is set to `coef.d <- seq_len(qr(X[,coef.d])$rank)`.

Weights must be finite positive numerics greater zero. This is necessary for model (QR) decomposition and for back transformation of the rotated data into the original variance structure, see also `randrot`. Weights as estimated e.g. by `voom` (Law et al. 2014) are suitable and can be used without further processing. Note that due to the whitening transformation (i.e. by using the arguments `weights` and/or `cormat`) the rank of the transformed (whitened) design matrix X could change (become smaller), which could become dangerous for the fitting procedures. If you get errors using `weights` and/or `cormat`, try the routine without using `weights` and/or `cormat` to exclude this source of errors.

The following section provides a brief summary how rotations are calculated. A more general introduction is given in (Langsrud 2005) For reasons of readability, we omit writing `%%` for matrix multiplication and write `*` for transposed matrix. The rotation is done by multiplying the features \times `samples` data matrix Y with the transpose of the restricted random rotation matrix R_t

$$R_t = X_d X_d^* + [X_h X_e] R [X_h X_e]^*$$

with R being a (reduced) random rotation matrix and X_d , X_h and X_e being columns of the full QR decomposition of the design matrix X . `[X_d X_h X_e] = qr.Q(qr(X), complete = TRUE)`, where X_d correspond to columns `coef.d`, X_h to columns `coef.h` and X_e to the remaining columns.

If `weights` and/or `cormat` are specified, each feature $Y[i,]$ and the design matrix X are whitening transformed before rotation. The whitening matrix T is defined as $T = \text{solve}(C) w$, where `solve(C)` is the inverse Cholesky decomposition of the correlation matrix (`cormat = CC*`) and w is a diagonal matrix of the square roots of the sample weights for the according feature ($w = \text{diag}(\text{sqrt}(\text{weights}[i,]))$).

The rotated data for one feature $y.r[i,]$ is thus calculated as

$$y.r[i,] = (\text{solve}(T) R_t T (y[i,])^*)^* \text{ and } [X_d X_h X_e] = \text{qr.Q}(\text{qr}(TX), \text{complete} = \text{TRUE})$$

For `weights = NULL` and `cormat = NULL`, `T` is the identity matrix.

Note that a separate QR decomposition is calculated for each feature if `weights` are specified. The restricted random orthogonal matrix `Rt` is calculated with the same reduced random orthogonal matrix `R` for all features.

When using `initBatchRandrot`, `initRandrot` is called for each batch separately. When using `initBatchRandrot` with `cormat`, `cormat` needs to be a list of correlation matrices with one matrix for each batch. Note that this implicitly assumes a block design of the sample correlation matrix, where sample correlation coefficients between batches are zero. For a more general sample correlation matrix, allowing non-zero sample correlation coefficients between batches, see package vignette. Batches are split according to `split(seq_along(batch), batch)`.

Value

An initialised `initRandrot`, `initRandrotW` or `initBatchRandrot` object.

Author(s)

Peter Hettegger

References

Langsrud O (2005). "Rotation tests." *Statistics and Computing*, **15**, 53–60. doi: [10.1007/s11222-00547895](https://doi.org/10.1007/s11222-00547895), C\$`delimiter`026E30F\$: /Users/hetteggerp/Desktop/Skripten{ }Ebooks/Mendeley{ }bib/Langsrud{ }2005{ }Rotationtests.pdf.

Law CW, Chen Y, Shi W, Smyth GK (2014). "Voom: Precision weights unlock linear model analysis tools for RNA-seq read counts." *Genome Biology*, **15**, 1–17. doi: [10.1186/gb2014152r29](https://doi.org/10.1186/gb2014152r29), C\$`delimiter`026E30F\$: /Users/hetteggerp/Desktop/Skripten{ }Ebooks/Mendeley{ }bib/Lawetal.{ }2014{ }VoomPrecisionweightsunlocklinearmodelanalysistoolsforRNA-seqreadcounts.pdf.

See Also

[randrot](#), [rotateStat](#)

Examples

```
# For further examples see '?rotateStat' and package vignette.

# Example 1: Compatibility with limma::voom

## Not run:
v <- voom(counts, design)
ir <- initRandrot(v)
## End(Not run)

# Example 2:

#set.seed(0)

# Dataframe of phenotype data (sample information)
# We simulate 2 sample classes processed in 3 batches
pdata <- data.frame(batch = rep(1:3, c(10,10,10)),
                    phenotype = rep(c("Control", "Cancer"), c(5,5)))
```

```

features <- 100

# Matrix with random gene expression data
edata <- matrix(rnorm(features * nrow(pdata)), features)
rownames(edata) <- paste("feature", 1:nrow(edata))

mod1 <- model.matrix(~phenotype, pdata)

# Initialisation of the random rotation class
init1 <- initBatchRandrot(Y = edata, X = mod1, coef.h = 2, batch = pdata$batch)
init1
# See '?rotateStat'

```

initRandrot-class *Initialised random rotation class*

Description

List-based S4 class containing all information necessary to generate randomly rotated data with the [randrot](#) method. `initRandrot` and `initRandrotW` objects are created with the [initRandrot](#) method.

`initRandrotW` is organised as its base class `initRandrot`, although some components are changed or added.

Components

The following components are included as list elements:

`X` Original (non-transformed) design matrix.
`Xhe`, `Xhe.Y.w`, `Yd` Pre-multiplied matrix products needed for generation of rotated data ([randrot](#)).
`coef.h`, `coef.d` Indices of H_0 coefficients (`coef.h` or "hypothesis coefficients") and indices of all other coefficients (`coef.d` or "determined coefficients").
`cormat` Correlation matrix, see [initRandrot](#).
`tcholC` Cholesky decomposition of `cormat`: `cormat = crossprod(tcholC)`.
`rank` Rank of the qr decomposition of (transformed/whitened) `X`

The following components are changed or added in `initRandrotW`-class as compared to `initRandrot`-class:

`decomp.list` List containing `Xd`, `Xhe` and rank of the transformed/whitened design matrix for each feature, see also [X_decomp](#).
`w` Numeric matrix with dimensions `features x samples` containing component wise square root of the weight matrix, see [initRandrot](#).

Author(s)

Peter Hettegger

pFdr

*Calculate resampling based p-values and FDRs***Description**

This function calculates either (1) resampling based p-values with subsequent p-value adjustment using `stats::p.adjust` or (2) resampling based false-discovery-rates (FDRs) for rotated statistics from a `rotateStat` object.

Usage

```
pFdr(obj, method = "none", pooled = TRUE, na.rm = FALSE, beta = 0.05)
```

Arguments

<code>obj</code>	A <code>rotateStat</code> object as returned by <code>rotateStat</code> .
<code>method</code>	Can be either "none" (default), "fdr.q", "fdr.qu" or any term that can be passed as method argument to <code>stats::p.adjust</code> , see Details. If method = "none", resampling based p-values without further adjustment are calculated.
<code>pooled</code>	logical. TRUE (default) if marginal distributions are exchangeable for all features so that rotated stats can be pooled, see Details.
<code>na.rm</code>	logical. NA values are ignored if set TRUE. NA values should be avoided and could e.g. be removed by imputation in original data or by removing features that contain NA values. Few NA values do not have a large effect, but many NA values can lead to wrong estimations of p-values and FDRs. We highly recommend avoiding NA values.
<code>beta</code>	numeric between 0 and 1. Corresponds to beta in (Yekutieli and Benjamini 1999).

Details

Larger values of `obj$s0` are considered more significant when compared to the empirical distribution. E.g. for calculation of resampling based p-values (with `pooled = FALSE`) we in principle use `p.val <- rowMeans(obj$stats >= obj$s0)`. We take `>=` instead of `>` when comparing rotated statistics against non-rotated statistics, as this is safer for discrete statistics.

`method = "fdr.q"` and `method = "fdr.qu"` are resampling based fdr estimates and can only be used with `pooled = TRUE`. `method = "fdr.q"` is the FDR local estimator and `method = "fdr.qu"` is the FDR upper limit, see (Reiner et al. 2003; Yekutieli and Benjamini 1999). For all other method arguments resampling based p-values are calculated and passed to `stats::p.adjust` for p-value adjustment. So these methods provide resampling based p-values with (non-resampling based) p-value adjustment.

When `pooled = TRUE`, marginal distributions of the test statistics are considered exchangeable for all features. The resampling based p-values of each feature are then calculated from all rotated statistics (all features, all rotations). For these cases, if the number of features is reasonably large, usually only few resamples (argument `R` in `rotateStat`) are required. We want to emphasize that in order for the marginal distributions to be exchangeable, the statistics must be a pivotal quantity (i.e. it must be scale independent) Pivotal quantities are e.g. t values. Using e.g. linear models with `coef` as statistics is questionable if the different features are measured on different scales. The

resampled coefficients then have different variances and `pooled = TRUE` is not applicable. We thus highly recommend using pivotal quantities as statistics in `rotateStat` if possible.

When `pooled = FALSE` the resampling based p-values are calculated for each feature separately. This is required if one expects the resampling based statistics to be distributed differently for individual features. For most common applications this should not be the case and the marginal distribution are exchangeable for all features, hence `pooled = TRUE` by default.

If `method = "fdr.q"` or `method = "fdr.qu"` and `weights` were specified when initialising the random rotation object (see parameter `initialised.obj` in `rotateStat`), a warning is displayed. The correlation structure (dependence structure) of linear model coefficients between different features is not preserved if different weights are used for different features. Methods `fdr.q` and `fdr.qu` rely on preserved correlation structure of dependent statistics and thus should not be used if statistics based on model coefficients (e.g. t statistics of model coefficients) are used in combination with different weights.

`method = "fdr.q"` and `method = "fdr.qu"` were adapted from package `fdrane` (Benjamini et al. 2019; Reiner et al. 2003).

P-values and FDRs are calculated for each column of `obj$s0` separately.

Value

A numeric matrix of corrected p-values or FDRs with dimension `dim(obj$s0)`.

Author(s)

Peter Hettegger

References

Benjamini Y, Kenigsberg E, Reiner A, Yekutieli D (2019). *fdrane: FDR adjustments of Microarray Experiments (FDR-AME)*. R package version 1.56.0.

Reiner A, Yekutieli D, Benjamini Y (2003). "Identifying differentially expressed genes using false discovery rate controlling procedures." *Bioinformatics*, **19**, 368–375. doi: [10.1093/bioinformatics/btf877](https://doi.org/10.1093/bioinformatics/btf877), `C:\delimiter"026E30F$: /Users/phett/Desktop/Skripten{ }Ebooks/Mendeley{ }bib/Reiner, Yekutieli, Benjamini{ }2003{ }Identifyingdifferentiallyexpressedgenesusingfalsediscoveryrate.pdf`.

Yekutieli D, Benjamini Y (1999). "Resampling-based false discovery rate controlling multiple test procedures for correlated test statistics." *Journal of Statistical Planning and Inference*, **82**, 171–196. doi: [10.1016/S03783758\(99\)000415](https://doi.org/10.1016/S03783758(99)000415), `C:\delimiter"026E30F$: /Users/phett/Desktop/Skripten{ }Ebooks/Mendeley{ }bib/Yekutieli, Benjamini{ }1999{ }Resampling-basedfalsediscoveryrate.pdf`.

See Also

[rotateStat](#)

Examples

```
# See also '?rotateStat':

#set.seed(0)

# Dataframe of phenotype data (sample information)
```

```

# We simulate 2 sample classes processed in 3 batches
pdata <- data.frame(batch = rep(1:3, c(10,10,10)),
                    phenotype = rep(c("Control", "Cancer"), c(5,5)))
features <- 100

# Matrix with random gene expression data
edata <- matrix(rnorm(features * nrow(pdata)), features)
rownames(edata) <- paste("feature", 1:nrow(edata))

mod1 <- model.matrix(~phenotype, pdata)

# Initialisation of the random rotation class
init1 <- initBatchRandrot(Y = edata, X = mod1, coef.h = 2, batch = pdata$batch)
init1

# Definition of the batch effect correction procedure with subsequent calculation
# of two-sided test statistics
statistic <- function(., batch, mod, coef){

  # The "capture.output" and "suppressMessages" simply suppress any output
  capture.output(suppressMessages(
    Y.tmp <- sva::ComBat(., batch = batch, mod)
  ))

  fit1 <- lm.fit(mod, t(Y.tmp))
  abs(coef(fit1)[coef,])
}

# We calculate test statistics for the second coefficient

res1 <- rotateStat(initialised.obj = init1,
                  R = 10,
                  statistic = statistic,
                  batch = pdata$batch, mod = mod1, coef = 2)

hist(pFdr(res1))

```

qqunif

Quantile-Quantile plot of data sample against uniform theoretical quantiles

Description

qqunif produces a QQ plot of the values in ps against the theoretical quantiles of the uniform distribution.

Usage

```

qqunif(
  ps,
  log = "xy",
  pch = 20,
  xlab = "theoretical quantiles",
  ylab = "sample quantiles",

```

```
) ...
```

Arguments

ps	numeric vector of values (e.g. p-values). Values must be between 0 and 1. Values like NA, NaN, Inf etc. produce an error.
log	character indicating whether axis should be plotted in log scale. Either "", "x", "y" or "xy".
pch	Point symbol, see par .
xlab	Label for the x axis.
ylab	Label for the y axis.
...	Graphical parameters forwarded to qqplot

Details

This function can e.g. be used for comparing p-values against the uniform distribution. The log scale of the x and y axes allow a closer look at low p-values.

This function is a modified version of the examples in the [qqnorm](#) documentation page.

Value

qqunif returns NULL.

Examples

```
qqunif(runif(100))
```

randorth	<i>Random orthogonal matrix</i>
----------	---------------------------------

Description

Generation of a random orthogonal n x n matrix.

Usage

```
randorth(n, type = c("orthonormal", "unitary"), I.matrix = FALSE)
```

Arguments

n	numeric of length 1 defining the dimensions of the n x n square matrix.
type	Either "orthonormal" or "unitary" defining whether a real orthonormal matrix or a complex unitary matrix should be returned.
I.matrix	If TRUE, the identity matrix is returned.

Details

A random orthogonal matrix R is generated in order that $t(R)$ (for "orthonormal") or $\text{Conj}(t(R))$ (for "unitary") equals the inverse matrix of R .

This function was adapted from the `pracma` package (`pracma::randortho`).

The random orthogonal matrices are distributed with Haar measure over $O(n)$, where $O(n)$ is the set of orthogonal matrices of order n . The random orthogonal matrices are basically distributed "uniformly" in the space of random orthogonal matrices of dimension $n \times n$. See also the Examples and (Stewart 1980; Mezzadri 2007).

Value

A random orthogonal matrix of dimension $n \times n$.

Author(s)

Peter Hettegger

References

Mezzadri F (2007). "How to generate random matrices from the classical compact groups." *Notices of the American Mathematical Society*, **54**, 592–604. [C:\delimiter"026E30F\\$:/Users/phett/Desktop/Skripten{ }Ebooks/Mendeley{ }bib/Mezzadri{ }2007{ }Howtogeneraterandommatricesfromtheclassicalcompactgroups.pdf](C:\delimiter).

Stewart GW (1980). "The Efficient Generation of Random Orthogonal Matrices with an Application to Condition Estimators." *SIAM Journal on Numerical Analysis*. doi: <10.1137/0717034>, [C\delimiter"026E30F\\$:/Users/hetteggerp/Desktop/Skripten{ }Ebooks/Mendeley{ }bib/Stewart{ }1980{ }Theefficientgenerationofrandomorthogonalmatrixes.pdf](C:\delimiter).

Examples

```
# The following example shows the orthogonality of the random orthogonal matrix:
R1 <- randorth(4)
zapsmall(t(R1) %% R1)

R1 <- randorth(4, "unitary")
zapsmall(Conj(t(R1)) %% R1)

# The following example shows the distribution of 2-dimensional random orthogonal vectors
# on the unit circle.
tmp1 <- vapply(1:400, function(i)randorth(2)[,1], numeric(2))
plot(t(tmp1), xlab = "x", ylab = "y")
```

randpermut

Generate random permutation matrix for n samples

Description

Generate a random permutation matrix for n samples.

Usage

```
randpermut(n)
```

Arguments

n Number of samples

Details

This methods generates an orthogonal matrix with only one entry in each row and column being 1, all other entries being 0.

Value

A random permutation matrix of dimension $n \times n$

Author(s)

Peter Hettegger

Examples

```
tmp1 <- randpermut(5)
t(tmp1) %*% tmp1
```

randrot

Random rotation of initialised object

Description

Perform random data rotation of a previously initialised object (see [initRandrot](#)) associated with the null hypothesis $H_0 : \beta_{coef,h} = 0$.

Usage

```
randrot(object, ...)

## S4 method for signature 'initRandrot'
randrot(object, ...)

## S4 method for signature 'initRandrotW'
randrot(object, ...)

## S4 method for signature 'initBatchRandrot'
randrot(object, ...)
```

Arguments

object An initialised object of class [initRandrot-class](#) or [initBatchRandrot-class](#).
 ... further arguments passed to [randorth](#)

Details

This function generates a randomly rotated dataset from an initialised randrot object (see [initRandrot](#)). See also package vignette for application examples. Only the numerical matrix of rotated data is returned, no design matrix, weights or other info is return for efficiency purposes. Please consider that, if you e.g. use weights or if you use [rotateStat](#), you may need to forward the design matrix X , weights etc. to subsequent analyses. See the example in [rotateStat](#).

Details on the calculation of a rotated dataset are given in [initRandrot](#) and (Langsrud 2005).

Value

numeric matrix of rotated data under the specified combined null hypothesis.

Author(s)

Peter Hettegger

References

Langsrud O (2005). "Rotation tests." *Statistics and Computing*, **15**, 53–60. doi: [10.1007/s11222-00547895](https://doi.org/10.1007/s11222-00547895), C\$\delimitter"026E30F\$: /Users/hetteggerp/Desktop/Skripten[_]Ebooks/Mendelej[_]bib/Langsrud[_]2005[_]Rotationtests.pdf.

Examples

```
# For further examples see '?rotateStat' and package vignette.

#set.seed(0)

# Dataframe of phenotype data (sample information)
# We simulate 2 sample classes processed in 3 batches
pdata <- data.frame(batch = rep(1:3, c(10,10,10)),
                    phenotype = rep(c("Control", "Cancer"), c(5,5)))
features <- 100

# Matrix with random gene expression data
edata <- matrix(rnorm(features * nrow(pdata)), features)
rownames(edata) <- paste("feature", 1:nrow(edata))

mod1 <- model.matrix(~phenotype, pdata)

# Initialisation of the random rotation class
init1 <- initBatchRandrot(Y = edata, X = mod1, coef.h = 2,
                        batch = pdata$batch)

init1

### Fit model to original data

fit.orig <- lm.fit(mod1, t(edata))
head(t(coef(fit.orig)))

### Fit model to rotated data

edata.rot <- randrot(init1)
fit.rot <- lm.fit(mod1, t(edata.rot))
head(t(coef(fit.rot)))
```

```

# Note that the coefficients stay equal if we regress only on the
# non-hypothesis coefficients

mod0 <- model.matrix(~1, pdata)
fit.orig0 <- lm.fit(mod0, t(edata))
fit.rot0 <- lm.fit(mod0, t(edata.rot))
head(t(coef(fit.orig0)))
head(t(coef(fit.rot0)))

```

rotateStat

Generate data rotations and calculate statistics on it

Description

This function generates rotations of data and calculates the provided statistic on each rotation and the non-rotated (original) data. This is the central function of the package.

Usage

```

rotateStat(
  initialised.obj,
  R = 10,
  statistic,
  ...,
  parallel = FALSE,
  BPPARAM = BiocParallel::bpparam()
)

```

Arguments

initialised.obj	An initialised random rotation object as returned by initRandrot and initBatchRandrot .
R	The number of resamples/rotations. Single numeric larger than 1.
statistic	A function which takes a data matrix (same dimensions as Y - see also initRandrot) as first argument and returns a statistic of interest. Any further arguments are passed to it by <code>...</code> . We highly recommend using pivotal quantities as <code>statistic</code> if possible (see also Details in pFdr). Note that pFdr considers larger values of statistics as more significant, so one-tailed tests may require reversal of the sign and two-tailed tests may require taking absolute values, see Examples . The results of <code>statistic</code> for each resample are finally combined with <code>as.matrix</code> and <code>cbind</code> , so ensure that <code>statistic</code> returns either a vector or a matrix. Results with multiple columns are possible and handled adequately in subsequent functions (e.g. pFdr).
...	Further named arguments for <code>statistic</code> which are passed unchanged each time it is called. Avoid partial matching to arguments of <code>rotateStat</code> . See also the Examples .
parallel	logical if parallel computation should be performed, see details for use of parallel computing.
BPPARAM	An optional BiocParallelParam instance, see documentation of BiocParallel package of Bioconductor.

Details

The function takes an initialised randrot object (`initRandrot`) and a function that calculates a statistic on the data. The statistic function thereby takes the a matrix Y as first argument. Any further arguments are passed to it by `...`

Be aware that only data is rotated (see also `randrot`), so any additional information including weights, X etc. need to be provided to `statistic`. See also package vignette and Examples.

Parallel processing is implemented with the `BiocParallel` package of `Bioconductor`. The default argument `BiocParallel::bpparam()` for `BPPARAM` returns the registered default backend. See package documentation for further information and usage options. If `parallel = TRUE` the function calls in `statistic` need to be called explicitly with package name and `"::"`. So e.g. calling `lmFit` from the `limma` package is done with `limma::lmFit(...)`, see also the examples in the package vignette.

Value

An object of class `rotateStat`.

Author(s)

Peter Hettegger

Examples

```
#set.seed(0)

# Dataframe of phenotype data (sample information)
# We simulate 2 sample classes processed in 3 batches
pdata <- data.frame(batch = rep(1:3, c(10,10,10)),
                    phenotype = rep(c("Control", "Cancer"), c(5,5)))
features <- 100

# Matrix with random gene expression data
edata <- matrix(rnorm(features * nrow(pdata)), features)
rownames(edata) <- paste("feature", 1:nrow(edata))

mod1 <- model.matrix(~phenotype, pdata)

# Initialisation of the random rotation class
init1 <- initBatchRandrot(Y = edata, X = mod1, coef.h = 2, batch = pdata$batch)
init1

# Definition of the batch effect correction procedure with subsequent calculation
# of two-sided test statistics
statistic <- function(., batch, mod, coef){

  # The "capture.output" and "suppressMessages" simply suppress any output
  capture.output(suppressMessages(
    Y.tmp <- sva::ComBat(., batch = batch, mod)
  ))

  fit1 <- lm.fit(mod, t(Y.tmp))
  abs(coef(fit1)[coef,])
}

# We calculate test statistics for the second coefficient
```

```
res1 <- rotateStat(initialised.obj = init1,
                  R = 10,
                  statistic = statistic,
                  batch = pdata$batch, mod = mod1, coef = 2)

hist(pFdr(res1))
```

rotateStat-class	<i>Rotated object containing rotated and non-rotated statistics</i>
------------------	---

Description

This list based class contains calculated statistics for the original data (s_0) and rotated data (stats). See also [rotateStat](#).

Components

s_0 Calculated statistics for original (non-rotated) data as returned by the `statistic` function ([rotateStat](#)).

stats List of length `ncol.s` containing statistics on rotated data for each column returned by the `statistic` function.

`ncol.s` Number of columns returned by the `statistic` function.

R Number of resamples/rotations.

Author(s)

Peter Hettegger

show,initRandrot-method	<i>Show an Object</i>
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Description

Display the object by printing structured summary information.

Usage

```
## S4 method for signature 'initRandrot'
show(object)

## S4 method for signature 'initBatchRandrot'
show(object)

## S4 method for signature 'rotateStat'
show(object)
```

Arguments

object An object of class [initRandrot-class](#), [initRandrotW-class](#) or [initBatchRandrot-class](#).

Details

The show method always displays the original design matrix (X), not the transformed (whitened) versions.

Value

show returns an invisible NULL.

weights,initRandrot-method

Extract model weights

Description

weights is a generic function which extracts fitting weights from objects returned by modeling functions. NOTE: This man page is for the weights S4 generic function defined in the [randRotation](#) package.

Usage

```
## S4 method for signature 'initRandrot'
weights(object, ...)

## S4 method for signature 'initBatchRandrot'
weights(object, ...)
```

Arguments

object	An object of class initRandrot-class , initRandrotW-class or initBatchRandrot-class .
...	Kept for compatibility with the default method, see <code>?stats::weights</code> . For objects defined in package randRotation , this argument is currently not needed.

Value

Weights extracted from the object object. NULL if no weights were specified. See `?stats::weights` for the value returned by the default method.

Examples

```
weights
showMethods("weights")
selectMethod("weights", "ANY") # the default method
```

Description

Full QR decomposition of the design matrix X . No argument checks are performed, see Details.

Usage

```
X_decomp(X = NULL, coef.d = seq_len(ncol(X) - 1))
```

Arguments

<code>X</code>	Design matrix as generated by <code>model.matrix</code> .
<code>coef.d</code>	Non- H_0 coefficients.

Details

The design matrix X is QR decomposed into $X = X_q X_r$. By performing a full QR decomposition, X_q is automatically extended to a full basis. X_q is further split into X_d and X_{he} , where X_d corresponds to columns `coef.d` (non- H_0 or non-Null-Hypothesis columns) and X_{he} correspond to all other columns (H_0 and error columns), see `initRandrot`. No argument checks are performed for reasons of performance as this function is called frequently by `initRandrot` when weights are used. See (Langsrud 2005) for further details.

Value

A `list` object containing matrices X_d , X_{he} and rank of the qr decomposition.

Author(s)

Peter Hettegger

References

Langsrud O (2005). "Rotation tests." *Statistics and Computing*, **15**, 53–60. doi: [10.1007/s11222-00547895](https://doi.org/10.1007/s11222-00547895), C\$delimiter"026E30F\$:/Users/hetteggerp/Desktop/Skripten{ }Ebooks/Mendeley{ }bib/Langsrud{ }2005{ }Rotationtests.pdf.

Examples

```
design <- cbind(1, rep(0:1, 5))
X_decomp(design)
```

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