# Meta-analysis for Microarray Experiments

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## 1 Introduction

The use of meta-analysis tools and strategies for combining data from microarray experiments seems to be a good and practical idea. Choi et al. (2003) is among the first authors to address these issues. Of great importance in working with these data is the realization that different experiments typically have been designed to address different questions. In general, it will only make sense to combine data sets if the questions are the same, or, if some aspects of the experiments are sufficiently similar that one can hope to make better inference from the whole than from the experiments separately. Just because two experiments were run on the same microarray platform is not sufficient justification for combining them.

In *GeneMeta* we have implemented many of the tools described by (Choi et al., 2003). They focused on the combination of datasets based on two sample comparisons. Hence, their procedures are largely based on the *t*-test. It is not clear whether improvements would eventuate if some of the more popular adjustments to these tests were used instead.

Consider the situation where data from k trials is available and we want to estimate the mean difference in expression, for each gene, between two commonly measured phenotypes (here we use the term phenotype loosely). The setting considered by Choi et al was that of a tumor versus normal comparison.

The general model for this setting, is as follows. Let  $\mu$  denote the parameter of interest (the true difference in mean, say). Let  $y_i$  denote the measure effect for study i, with  $i = 1, \ldots, k$ . Then the hierarchical model is:

$$y_i = \theta_i + \epsilon_i, \qquad \epsilon_i \sim N(0, \sigma_i^2)$$
  
 $\theta_i = \mu + \delta_i, \qquad \delta_i \sim N(0, \tau^2)$ 

where  $\tau^2$  represents the between study variability and  $\sigma_i^2$  denotes the within study variability. The analysis is different depending on whether a fixed effect model (FEM) is deemed appropriate, or a random effects model (REM) is deemed appropriate. Under a FEM, the basic presumption is that  $\tau = 0$ . If this does not hold then a REM will need to be fit. The estimates of the overall effect,  $\mu$ , are different depending on which model is used.

Choi et al. (2003) suggest using an estimator due to DerSimonian and Laird for the REM model. This estimator is computed using the function tau2.DL, and its variance via var.tau2

## Simple Usage

In this vignette we want to show how these methods can be used to combine data sets. Typically matching of identifiers is an important component. We don't want to address the problem here and so just do the following: we split a data set and then combine these two splits. We show that the combination of the splits is as nearly good as the original set. So in this paper we also do not address the problem, that is mentioned above, i.e. to combine only things that are measuring the same thing. In this example we know that the same thing has be measured.

### Getting the data

We first load a data sets that were reported by West et al. (2001) and were collected on patients with breast cancer. **Nevins** includes data from 46 hybridizations on hu6800 Affymetrix chips.

```
> library(GeneMeta)
> library(RColorBrewer)
> #load("~/Bioconductor/Projects/GraphCombine/MetaBreast/data/Nevins.RData")
> data(Nevins)
```

We want to look at the estrogen receptor status and find genes that have a high 't-statistic' for the difference between estrogen receptor positive and negative patients. Actually we don't use the t statistic itself but

$$d = t \cdot \sqrt{\frac{n_1 + n_2}{n_1 \cdot n_2}}$$

oro t is the 'usual' t statistic as

Here t is the 'usual' t-statistic and  $n_1$  and  $n_2$  are the number of elements in the two groups. We create two data sets from the original set by splitting. We make sure that the same fraction of ER positive cases is in each group.

For each data set (Split1 and Split2) we extract the estrogen receptor (ER) status and code it as a 0-1 vector.

```
> #obtain classes
> Split1.ER<-pData(Split1)[,"ER.status"]
> levels(Split1.ER) <- c(0,1)
> Split1.ER<- as.numeric(as.character(Split1.ER))
> Split2.ER<-pData(Split2)[,"ER.status"]
> levels(Split2.ER) <- c(0,1)
> Split2.ER<- as.numeric(as.character(Split2.ER))</pre>
```

## Combining the data

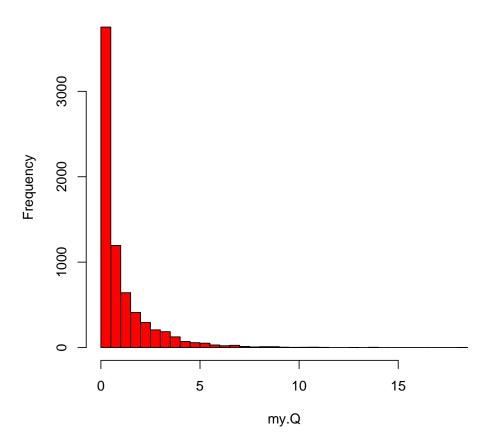
Next we compute the unbiased estimates of the effect (d.adj.Split1 and d.adj.Split2) and its variance (var.d.adj.Split1 and var.d.adj.Split2). Our goal is to compute Cochran's Q statistic to determine whether we should be considering a fixed effects or a random effects model for the data.

Now, with those in hand we can compute Q and then create and display a qq-plot for comparing the observed values to a  $\chi_1^2$  random variable (since we have two experiments).

```
> #calculate Q
> mymns <- cbind(d.adj.Split1, d.adj.Split2)
> myvars <- cbind(var.d.adj.Spli1,var.d.adj.Split2)
> my.Q <- f.Q(mymns, myvars)
> mean(my.Q)

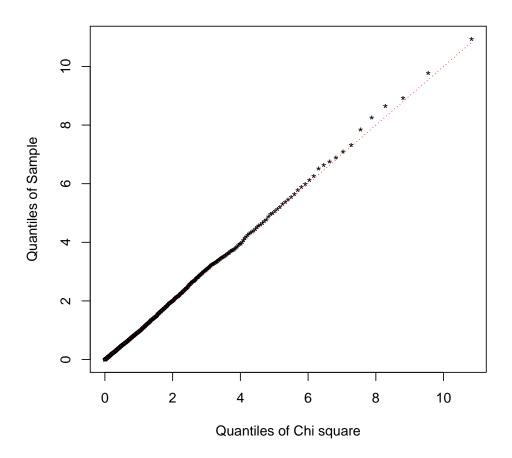
[1] 0.9963985
> hist(my.Q,breaks=50,col="red")
```

## Histogram of my.Q



We can see immediately from the histogram and the mean of the Q values that the hypothesis that these values come from a  $\chi_1^2$  random variable seems to be valid.

## **QQ Plot**



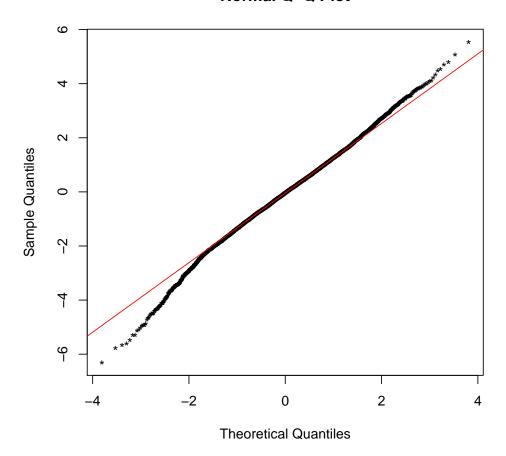
Given that we need to fit a FEM model we next compute the estimated effect sizes. Each effect size is a weighted average of the effects for the individual experiments divided by its standard error. The weights are the reciprocal of the estimated variances.

- > muFEM = mu.tau2(mymns, myvars)
  > sdFEM = var.tau2(myvars)
- > ZFEM = muFEM/sqrt(sdFEM)

Plotting the quantiles of the effects we can see that the presumption of approximate Normality seems to be appropriate.

- > qqnorm(ZFEM,pch="\*")
- > qqline(ZFEM,col="red")

#### Normal Q-Q Plot

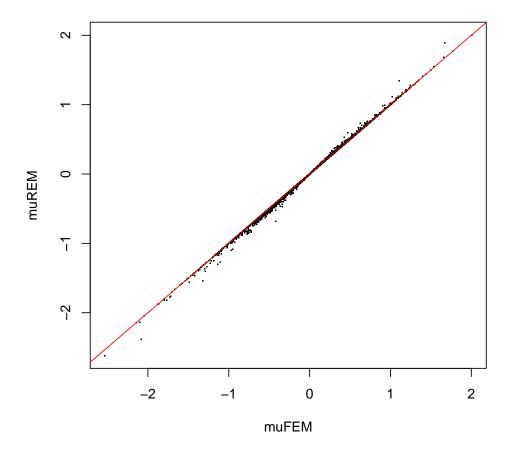


If instead we would have to fit a REM model we would compute the estimated effect sizes using the DerSimonian and Laird estimator. Therefore, we must first estimate the variance  $\tau$  of the 'between experiments' random variable.

- $\verb| > my.tau2.DL < -tau2.DL (my.Q, num.studies, my.weights = 1/myvars)| \\$
- > #obtain new variances s^2+tau^2
- > myvarsDL <- myvars + my.tau2.DL</pre>
- > #compute
- > muREM <- mu.tau2(mymns, myvarsDL)</pre>
- > #cumpute mu(tau)
- > varREM <- var.tau2(myvarsDL)</pre>
- > ZREM <- muREM/sqrt(varREM)</pre>

We can easily compare the two different estimates,

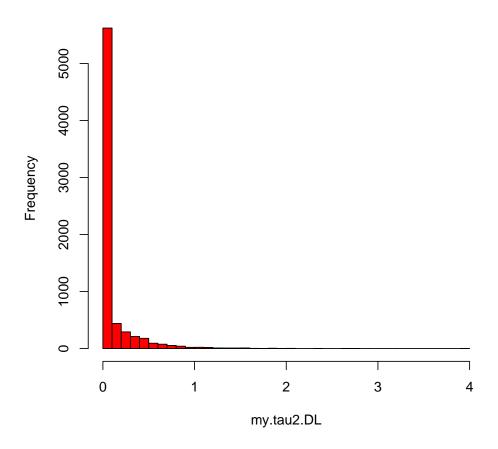
- > plot(muFEM, muREM, pch=".")
- > abline(0,1,col="red")



We do not see much difference here. This is because in the REM model for most of the genes the variance  $\tau$  is estimated as zero.

> hist(my.tau2.DL,col="red",breaks=50,main="Histogram of tau")

#### Histogram of tau



The procedure described above is also implemented in the function zScores (part of this package) and meta.summaries from the package rmeta. While meta.summaries do the calculation for arbitrary effects and their variances, zScores exactly follows the calculation from Choi et al. (2003). The arguments of this function are a list of expression sets and a list of classes. We include our two splits and also the original data set. By default zScores would combine all expression sets in the list, but we only want the combine the first two. So we have to set an additional parameter.

```
> esets <- list(Split1,Split2,Nevins)
> data.ER <-pData(Nevins)[,"ER.status"]
> levels(data.ER) <- c(0,1)
> data.ER<- as.numeric(as.character(data.ER))
> classes <- list(Split1.ER,Split2.ER,data.ER)
> theScores <- zScores(esets,classes,useREM=FALSE,CombineExp=1:2)</pre>
```

We get a matrix in the following form.

> theScores[1:2,]

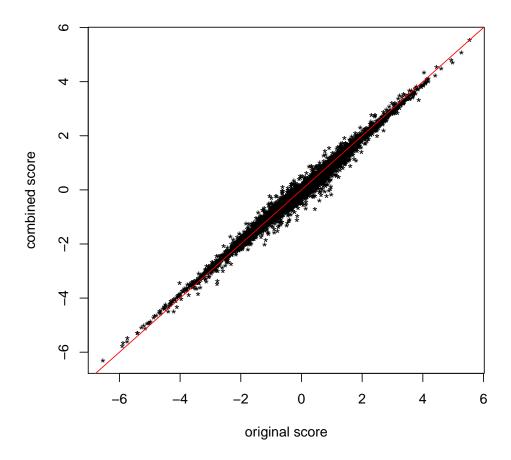
```
zSco_Ex_2 zSco_Ex_3
             zSco_Ex_1
                                                     zSco
                                                              MUvals
                                                                          MUsds
            -0.9743807
A28102 at
                        0.08904902 -0.5794422 -0.6221276 -0.1845920 0.2967108
AB000114_at -0.7422704 -0.17093358 -0.6361189 -0.6445773 -0.1908581 0.2960982
                          Qpvalues
                                        Chisq Effect_Ex_1 Effect_Ex_2
A28102_at
                       1 0.4501378 0.5338580
            0.5703048
                                               -0.4109929
                                                           0.03717436
AB000114_at 0.1647038
                       1 0.6848623 0.5192012 -0.3117136 -0.07137438
            Effect_Ex_3 EffectVar_Ex_1 EffectVar_Ex_2 EffectVar_Ex_3
A28102_at
             -0.1711808
                             0.1779145
                                             0.1742725
                                                           0.08727503
AB000114_at
             -0.1879951
                             0.1763547
                                             0.1743532
                                                           0.08734068
```

Here Effect\_Ex\_1 and Effect\_Ex\_2 are the unbiased estimates of the effect (d.adj.Split1 and d.adj.Split2). EffectVar\_Ex\_1 and EffectVar\_Ex\_2 are the estimated variances of the unbiased effects (var.d.adj.Split1 and var.d.adj.Split2). zSco\_Ex\_1 and zSco\_Ex\_2 are the unbiased estimates of the effects divided by their standard deviation. The same values are also calculated the the complete data set (Effect\_Ex\_3,EffectVar\_Ex\_3, and ZSco\_Ex\_3).

Qvals are the Q statistics (my.Q) and df is the number of combined experiments minus one. MUvals and MUsds are equal to muFEM and sdFEM (the overall mean effect size and its standard deviation). zSco are the z scores (ZFEM). Qpvalues is for each gene the probability that a chisq distribution with df degree of freedom has a higher value than its Q statistic. And Chisq is the probability that a chisq distribution with 1 degree of freedom has a higher value than zSco<sup>2</sup>.

We plot the z scores of original data set against the z scores of the combined data set. We see a good correlation so the combination of the two data sets works quite well. In the next paragraph we want to see how big the benefit of combining data sets really is.

```
> plot(theScores[,"zSco_Ex_3"],theScores[,"zSco"],pch="*",xlab="original score",ylab="
> abline(0,1,col="red")
```

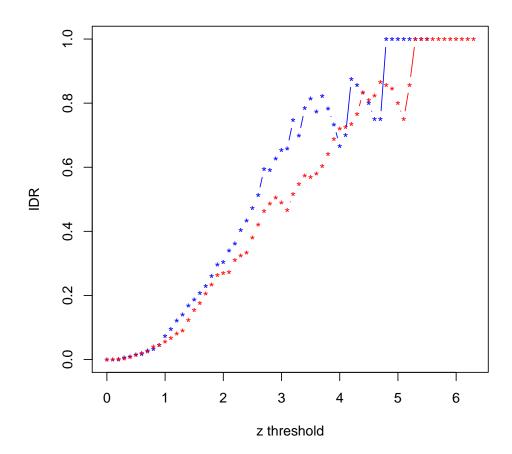


We now will have a look at the IDR plot as it is described in (Choi et al., 2003). For a threshold  $z_t h$  this plot shows the fraction of the genes that have a higher effect size than the threshold for the combined effect z, but not for any of the experiment specific effects  $z_i$ , e.g. we look for genes with

$$z \geq z_{th}$$
 and  $\sum_{i=1}^{k} I(z_i \geq z_{th}) = 0$  for  $z > 0$  or  $z \leq -z_{th}$  and  $\sum_{i=1}^{k} I(z_i \leq -z_{th}) = 0$  for  $z < 0$ 

The IDR was computed for z > 0 (blue) and z < 0 (red) separately. We can see that we get higher z scores by combing the sets.

> IDRplot(theScores,Combine=1:2,colPos="blue", colNeg="red")



## Estimating the false discovery rate

Next Choi et al. (2003) discussed using a SAM (Tusher et al., 2001) type analysis to estimate the false discovery rate(FDR). This is implemented in the function zscoresFDR.

> ScoresFDR <- zScoreFDR(esets, classes, useREM=FALSE, nperm=50,CombineExp=1:2)
This object is a list with three slots

> names(ScoresFDR)

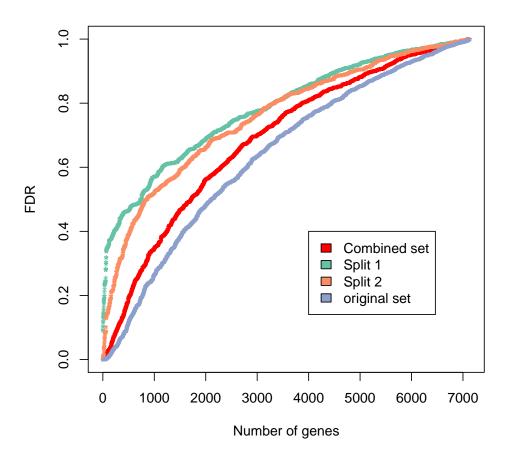
The first slot stores the results of the calculation, if the FDR is computed for the positive scores, the second for the negative scores and the last one for the tow sided situation (i.e. we look at the absolute values of the z scores). Each slot contains a matrix with the values obtained by zScores and additional a FDR for each experiment and the combination of experiments.

#### > ScoresFDR\$pos[1:2,]

```
zSco_Ex_1 FDR_Ex_1
                                  zSco_Ex_2 FDR_Ex_2 zSco_Ex_3 FDR_Ex_3
            -0.9743807 \ 1.070393 \ 0.08904902 \ 0.9738678 \ -0.5794422 \ 1.104358
A28102_at
AB000114_at -0.7422704 1.073673 -0.17093358 1.0073964 -0.6361189 1.108169
                  zSco
                            FDR
                                    MUvals
                                                MUsds
                                                          Qvals df Qpvalues
            -0.6221276 1.093313 -0.1845920 0.2967108 0.5703048 1 0.4501378
A28102_at
AB000114_at -0.6445773 1.093046 -0.1908581 0.2960982 0.1647038 1 0.6848623
                Chisq
A28102_at
            0.5338580
AB000114_at 0.5192012
```

We plot the number of genes and the corresponding FDR. Here the result for the combined set is red and for the result for the original set (without splitting) is blue. We extract the FDR for the two sided situation. It can be see that the combined data set has a lower FDR than the splits and a FDR as good as the original set.

```
> FDRwholeSettwo <- sort(ScoresFDR$"two.sided"[,"FDR"])
> experimentstwo <- list()
> for(j in 1:3){
+ experimentstwo[[j]] <- sort(ScoresFDR$"two.sided"[,paste("FDR_Ex_",j,sep="")])
+ }
> ##################
> # #
> #two sided z values #
> # #
> #################
> plot(FDRwholeSettwo,pch="*",col="red",ylab="FDR",xlab="Number of genes")
> for(j in 1:3)
+ points(experimentstwo[[j]],pch="*", col=theNewC[j])
> legend(4000,0.4,c("Combined set","Split 1" , "Split 2" ,"original set"), c("red",the
```



If we are more interested in the number of gene that are below a given threshold for the FDR we can use the CountPlot. Similar to IDRplot it shows the following: for each study (indicated by different colors) and various thresholds for the FDR (x axis) the number of genes that are below this threshold in the given study but above in all other studies are shown (y axis). The studies that should be considered (apart from the combined set that is always present) can be specified with CombineExp. Here we compare the original data set (green) against the combined data set (red). It can be seen that we do quite well.

```
> #par(mfrow=c(2,2))
```

<sup>&</sup>gt; #CountPlot(ScoresFDR,Score="FDR",kindof="neg",cols=c("red",theNewC),

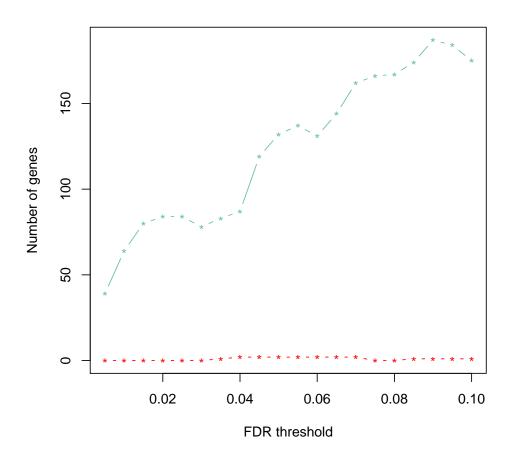
<sup>&</sup>gt; # main="Negative FDR", xlab="FDR threshold", ylab="Number of genes",CombineEx

<sup>&</sup>gt; #CountPlot(ScoresFDR,Score="FDR",cols=c("red",theNewC),kindof="pos",

<sup>&</sup>gt; #main="Positive FDR", xlab="FDR threshold", ylab="Number of genes", Combine=1:2)

<sup>&</sup>gt; CountPlot(ScoresFDR, Score="FDR", kindof="two.sided", cols=c("red", theNewC), main="two s

#### two sided FDR



## References

Choi JK, Yu U, Kim S, Yoo OJ. Combining multiple microarray studies and modeling interstudy variation *BI* 19(1): i84-i90 (2003).

West M, Blanchette C, Dressman H and others. Predicting the clinical status of human breast cancer by using gene expression profiles *Proc Natl Acad Sci U S A* 98(20):11462–11467 (2001).

Tusher VG, Tibshirani R, Chu, G. Significance analysis of microarrays applied to the ionizing radiation response PNAS 98:5116–5121 (2001).