

Gene Selection Using *GeneSelectMMD*

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1 Introduction

This document demonstrates how to use the *GeneSelectMMD* package to detect significant genes and to estimate false discovery rate (FDR), false non-discovery rate (FNDR), false positive rate (FPR), and false negative rate (FNR), for a real microarray data set based on the method proposed by Qiu et al. (2008). It also illustrates how to visualize the fit of the model proposed in Qiu et al. (2008) to the real microarray data set when the marginal correlations among subjects are zero or close to zero.

The *GeneSelectMMD* package is suitable for the case where there are only two tissue types and for the case where tissue samples within a tissue type are conditionally independent given the gene (c.f. Qiu et al., 2008).

2 Methods

MMD assumes that the marginal distribution of a gene profile is a mixture of 3-component multivariate normal distributions with special structure for mean vectors and covariance matrices. The 3 component distributions correspond to 3 gene clusters: (1) cluster of genes over-expressed in the treatment group; (2) cluster of genes non-differentially expressed; and (3) cluster of genes under-expressed in the treatment group. Specifically, the marginal density of a gene profile is assumed to be

$$\begin{aligned} f(\mathbf{x}|\boldsymbol{\theta}_1, \boldsymbol{\theta}_2, \boldsymbol{\theta}_3) &= \pi_1 f_1(\mathbf{x}|\boldsymbol{\theta}_1) + \pi_2 f_2(\mathbf{x}|\boldsymbol{\theta}_2) + \pi_3 f_3(\mathbf{x}|\boldsymbol{\theta}_3), \\ \pi_1 + \pi_2 + \pi_3 &= 1, \pi_i > 0, i = 1, 2, 3, \end{aligned} \quad (1)$$

where π_1, π_2, π_3 are mixture proportions. The $m \times 1$ vector \mathbf{x} is a realization of the random vector \mathbf{X} that represents the transformed gene profile for a randomly selected gene over m tissue samples ($m = m_c + m_n$, where m_c is the number of abnormal tissue samples and m_n normal tissue samples); $\boldsymbol{\theta}_k$, is the parameter set for the k -th component distribution f_k , $k = 1, 2, 3$; and f_1, f_2 , and f_3 are the density functions for multivariate Normal distributions with the mean vectors

$$\boldsymbol{\mu}_1 = \begin{pmatrix} \mu_{c1} \mathbf{1}_{m_c} \\ \mu_{n1} \mathbf{1}_{m_n} \end{pmatrix}, \quad \boldsymbol{\mu}_2 = \mu_2 \mathbf{1}_m, \quad \boldsymbol{\mu}_3 = \begin{pmatrix} \mu_{c3} \mathbf{1}_{m_c} \\ \mu_{n3} \mathbf{1}_{m_n} \end{pmatrix}. \quad (2)$$

and covariance matrices

$$\boldsymbol{\Sigma}_1 = \begin{pmatrix} \sigma_{c1}^2 \mathbf{R}_{c1} & \mathbf{0} \\ \mathbf{0} & \sigma_{n1}^2 \mathbf{R}_{n1} \end{pmatrix}, \quad \boldsymbol{\Sigma}_2 = \sigma_2^2 \mathbf{R}_2, \quad \boldsymbol{\Sigma}_3 = \begin{pmatrix} \sigma_{c3}^2 \mathbf{R}_{c3} & \mathbf{0} \\ \mathbf{0} & \sigma_{n3}^2 \mathbf{R}_{n3} \end{pmatrix}, \quad (3)$$

respectively, where correlation matrix

$$\mathbf{R}_t = (1 - \rho_t) \left[\mathbf{I}_{n_t} + \frac{\rho_t}{(1 - \rho_t)} \mathbf{1}_{n_t} \mathbf{1}_{n_t}^T \right], \quad (4)$$

$t = c_1, n_1, 2, c_3,$ or n_3 . $n_t = m_c$ if $t = c_1$ or c_3 ; $n_t = m$ if $t = 2$; $n_t = m_n$ if $t = n_1,$ or n_3 . Here we assume, without loss of generality, that the first m_c elements of the random vector \mathbf{X} are for the abnormal tissue samples and the remaining m_n elements are for the normal tissue samples. Let $\boldsymbol{\theta}_1 = (\mu_{c_1}, \sigma_{c_1}^2, \rho_{c_1}, \mu_{n_1}, \sigma_{n_1}^2, \rho_{n_1})^T$, $\boldsymbol{\theta}_2 = (\mu_2, \sigma_2^2, \rho_2)^T$, $\boldsymbol{\theta}_3 = (\mu_{c_3}, \sigma_{c_3}^2, \rho_{c_3}, \mu_{n_3}, \sigma_{n_3}^2, \rho_{n_3})^T$. Note that $\mu_{c_1} > \mu_{n_1}$ for component 1 in which genes are overexpressed in abnormal tissue samples, and $\mu_{c_3} < \mu_{n_3}$ for component 3 where genes are underexpressed in abnormal samples. Our prior belief is that the majority of genes are usually non-differentially expressed, so we assume $\pi_2 > \pi_1$ and $\pi_2 > \pi_3$.

The model parameters can be estimated using the EM algorithm (Dempster et al., 1977).

The cluster membership of a gene is determined by the posterior probability that the gene belongs to a cluster given its gene profile. The posterior probability is a function of the 3 component marginal density functions and the mixing proportions:

$$Pr(\text{gene } i \in \text{cluster } k | \mathbf{x}_i) = \frac{\pi_k f_k(\mathbf{x}_i | \boldsymbol{\theta}_k)}{\pi_1 f_1(\mathbf{x}_i | \boldsymbol{\theta}_1) + \pi_2 f_2(\mathbf{x}_i | \boldsymbol{\theta}_2) + \pi_3 f_3(\mathbf{x}_i | \boldsymbol{\theta}_3)}, \quad (5)$$

$$k = 1, 2, 3,$$

Specifically, a gene is assigned to the a gene cluster if the posterior probability that the gene belongs to that gene cluster given its gene profile is larger than the posterior probability that the gene belongs to other gene clusters given its gene profile:

$$k_0 = \arg \max_{k=1,2,3} Pr(\text{gene } i \in C_k | \mathbf{x}_i). \quad (6)$$

An important task is to assess the performance of a gene selection method so that different methods can be objectively compared. To evaluate the performance of a gene selection method, investigators usually compare the error rates, such as FDR, FNDR, FPR, and FNR, via simulation studies. However, when analyzing a real microarray data set, investigators are more interested in what the values of FDR, FNDR, FPR, and FNR are for this specific real microarray set. It is challenging to estimate FDR, FNDR, FPR, and FNR for real microarray data sets since the true gene cluster membership is unknown for real data sets. However, model-based gene clustering methods, such as Bayesian hierarchical models and MMD, can provide such estimates since these error rates can be expressed as functions of marginal density functions and mixing proportions, where the model parameters and mixing proportions can be estimated from the real microarray data. It is easy to use MMD to estimate the four error rates since MMD describes the distributions of gene expression levels directly via the marginal distributions, while it is usually difficult to derive the marginal density functions for Bayesian hierarchical models.

It is of practical importance to evaluate if a model fits a real microarray data set well. If a model does not fit well for the real microarray data set, then it makes no sense to estimate the error rates based on the model. Although it is quite challenging to asses the goodness of fit for multivariate data, especially for non-normal multivariate data, it is possible to do so for some special cases. For example, when tissue samples are marginally independent, we could pool the gene expression levels across tissue samples for each type of tissue samples since they are all independent. We then could impose the theoretical density curve on the histogram of the pooled expression levels for each type of tissue samples. The parameters $\rho_{c_1}, \rho_{n_1}, \rho_2, \rho_{c_3},$ and ρ_{n_3} indicates the marginal correlations among tissue samples. Assuming that the marginal correlations are ignorable, we then could produce such a plot to evaluate the goodness of fit of MMD to the real microarray data set.

3 Gene selection via *GeneSelectMMD*

The *GeneSelectMMD* includes four functions for gene selection: `gsMMD`, `gsMMD.default`, `gsMMD2`, and `gsMMD2.default`.

The functions `gsMMD` and `gsMMD2` accept the object derived from the class of *Bioconductor*'s `ExpressionSet` as data input, while the functions `gsMMD.default` and `gsMMD2.default` accept data matrix as data input.

The functions `gsMMD` and `gsMMD.default` will provide initial 3-cluster gene partitions (cluster of genes over-expressed in treatment group, cluster of genes non-differentially expressed, and cluster of genes under-expressed in treatment group) based on the gene-wise two-sample t-test or two-sample Wilcoxon rank-sum test. In situations where the user would like to provide the initial 3-cluster partition other than that provided by the gene-wise two-sample t-test or two sample Wilcoxon rank-sum test, the functions `gsMMD2` and `gsMMD2.default` could be used.

The rows of the input data matrix (or the data matrix derived from the object derived from the class `ExpressionSet`) are genes, while the columns are tissue samples. The tissue type of a tissue sample is indicated by the argument `memSubjects`, which is a $m \times 1$ vector, $m = m_c + m_n$, m_c is the number of tissue samples in the treatment group, and m_n is the number of tissue samples in the control group. `memSubjects[j]=1` indicates the j -th tissue sample is from the treatment group. `memSubjects[j]=0` indicates the j -th tissue sample is from the control group.

The output of gene selection functions include `dat`, `memGenes`, `memGenes2`, and `para`.

- `dat` is a data matrix with the same dimensions as the input data matrix. If no data transformation is performed, `dat` is the same as the input data matrix. Otherwise, it will be the transformed input data matrix.
- `memGenes` is a $G \times 1$ vector indicating the gene cluster membership, where G is the number of genes (i.e., the number of rows of the input data matrix). `memGenes[g]=1` indicates the g -th gene is assigned to the cluster of genes over-expressed in treatment group; `memGenes[g]=2` indicates the g -th gene is assigned to the cluster of genes non-differentially-expressed; `memGenes[g]=3` indicates the g -th gene is assigned to the cluster of genes under-expressed in treatment group.
- `memGenes2` is a variant of `memGenes`. `memGenes2[g]=1` means the g -th gene is differentially expressed, while `memGenes2[g]=0` means the g -th gene is non-differentially expressed, $g = 1, \dots, G$.
- `para` is a 18×1 vector of parameters $(\pi_1, \pi_2, \pi_3, \mu_{c1}, \sigma_{c1}^2, \rho_{c1}, \mu_{n1}, \sigma_{n1}^2, \rho_{n1}, \mu_2, \sigma_2^2, \rho_2, \mu_{c3}, \sigma_{c3}^2, \rho_{c3}, \mu_{n3}, \sigma_{n3}^2, \rho_{n3},)$ for the model described in Equations (1)- (4), which can be estimated by the EM algorithm. `para[1]`, `para[2]`, and `para[3]` are the cluster proportions for the 3 gene clusters (over-expressed, non-differentially expressed, and under-expressed). `para[4]`, `para[5]`, and `para[6]` are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for diseased subjects; `para[7]`, `para[8]`, and `para[9]` are the marginal mean, variance, and correlation of gene expression levels of cluster 1 (up-regulated genes) for non-diseased subjects; `para[10]`, `para[11]`, and `para[12]` are the marginal mean, variance, and correlation of gene expression levels of cluster 2 (non-differentially expressed genes); `para[13]`, `para[14]`, and `para[15]` are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for diseased subjects; `para[16]`, `para[17]`, and `para[18]` are the marginal mean, variance, and correlation of gene expression levels of cluster 3 (up-regulated genes) for non-diseased subjects.

Note that genes in cluster 2 are non-differentially expressed across abnormal and normal tissue samples. Hence there are only 3 parameters for cluster 2.

For example, to obtain differentially expressed genes for the ALL data (Chiaretti et al., 2004), we can run either

```
> library(GeneSelectMMD)
> library(ALL)
> data(ALL)
> eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]
> mem.str <- as.character(eSet1$BT)
```

```

> nSubjects <- length(mem.str)
> memSubjects <- rep(0, nSubjects)
> memSubjects[mem.str == "T2"] <- 1
> obj.gsMMD <- gsMMD(eSet1, memSubjects, transformFlag = TRUE,
+   transformMethod = "boxcox", scaleFlag = TRUE, quiet = FALSE)

Programming is running. Please be patient...
Data transformation ( boxcox ) performed
Gene profiles are scaled so that they have mean zero and variance one!
Programming is running. Please be patient...
***** initial parameter estimates method>> Ttest *****
paraIniMat[,i]>>
      pi.1      pi.2      pi.3      mu.c1 sigma2.c1      rho.c1      mu.n1 sigma2.n1
      0.050      0.870      0.080      0.556      0.604      0.003      -0.363      0.947
      rho.n1      mu.2      sigma2.2      rho.2      mu.c3      sigma2.c3      rho.c3      mu.n3
      0.001      0.000      1.000      0.000      -0.659      0.513      0.097      0.430
sigma2.n3      rho.n3
      0.812      0.028

llkhVec>>
      Ttest
-5284.364

*****

Initial parameter estimates>>
      Ttest
pi.1      0.050
pi.2      0.870
pi.3      0.080
mu.c1      0.556
sigma2.c1  0.604
rho.c1      0.003
mu.n1      -0.363
sigma2.n1  0.947
rho.n1      0.001
mu.2      0.000
sigma2.2    1.000
rho.2      0.000
mu.c3      -0.659
sigma2.c3   0.513
rho.c3      0.097
mu.n3      0.430
sigma2.n3   0.812
rho.n3      0.028

Initial loglikelihood>>
      Ttest
-5308.485

Final parameter estimates based on initial estimates>>
      Ttest

```

```

pi.1      0.049
pi.2      0.906
pi.3      0.044
mu.c1     0.557
sigma2.c1 0.563
rho.c1    -0.069
mu.n1     -0.363
sigma2.n1 0.908
rho.n1    -0.045
mu.2      0.000
sigma2.2  0.974
rho.2     -0.027
mu.c3     -0.808
sigma2.c3 0.292
rho.c3    0.061
mu.n3     0.527
sigma2.n3 0.715
rho.n3    -0.023

```

Final loglikelihood based on initial estimates>>

```

Ttest
-5284.364

```

Final parameter estimates>>

```

pi.1      pi.2      pi.3      mu.c1 sigma2.c1      rho.c1      mu.n1 sigma2.n1
0.049     0.906     0.044     0.557   0.563   -0.069     -0.363  0.908
rho.n1    mu.2    sigma2.2    rho.2    mu.c3 sigma2.c3    rho.c3    mu.n3
-0.045    0.000    0.974    -0.027   -0.808    0.292    0.061    0.527
sigma2.n3 rho.n3
0.715     -0.023

```

Final loglikelihood>>

```

Ttest
-5284.364

```

```

> para <- obj.gsMMD$para
> print(round(para, 3))

```

```

pi.1      pi.2      pi.3      mu.c1 sigma2.c1      rho.c1      mu.n1 sigma2.n1
0.049     0.906     0.044     0.557   0.563   -0.069     -0.363  0.908
rho.n1    mu.2    sigma2.2    rho.2    mu.c3 sigma2.c3    rho.c3    mu.n3
-0.045    0.000    0.974    -0.027   -0.808    0.292    0.061    0.527
sigma2.n3 rho.n3
0.715     -0.023

```

or

```

> library(GeneSelectMMD)
> library(ALL)
> data(ALL)
> eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]

```

```

> mat <- exprs(eSet1)
> mem.str <- as.character(eSet1$BT)
> nSubjects <- length(mem.str)
> memSubjects <- rep(0, nSubjects)
> memSubjects[mem.str == "T2"] <- 1
> obj.gsMMD <- gsMMD.default(mat, memSubjects, iniGeneMethod = "Ttest",
+   transformFlag = TRUE, transformMethod = "boxcox", scaleFlag = TRUE)

```

Programming is running. Please be patient...

Programming is running. Please be patient...

```

> para <- obj.gsMMD$para
> print(round(para, 3))

```

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.049	0.906	0.044	0.557	0.563	-0.069	-0.363	0.908
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
-0.045	0.000	0.974	-0.027	-0.808	0.292	0.061	0.527
sigma2.n3	rho.n3						
0.715	-0.023						

If we would like to provide the initial 3-cluster partition via the two sample Wilcoxon rank-sum test, then we can run either

```

> library(GeneSelectMMD)
> library(ALL)
> data(ALL)
> eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]
> mem.str <- as.character(eSet1$BT)
> nSubjects <- length(mem.str)
> memSubjects <- rep(0, nSubjects)
> memSubjects[mem.str == "T2"] <- 1
> myWilcox <- function(x, memSubjects, alpha = 0.05) {
+   xc <- x[memSubjects == 1]
+   xn <- x[memSubjects == 0]
+   m <- sum(memSubjects == 1)
+   res <- wilcox.test(x = xc, y = xn, conf.level = 1 - alpha)
+   res2 <- c(res$p.value, res$statistic - m * (m + 1)/2)
+   names(res2) <- c("p.value", "statistic")
+   return(res2)
+ }
> mat <- exprs(eSet1)
> tmp <- t(apply(mat, 1, myWilcox, memSubjects = memSubjects))
> colnames(tmp) <- c("p.value", "statistic")
> memIni <- rep(2, nrow(mat))
> memIni[tmp[, 1] < 0.05 & tmp[, 2] > 0] <- 1
> memIni[tmp[, 1] < 0.05 & tmp[, 2] < 0] <- 3
> print(table(memIni))

```

```

memIni
 1  2  3
 7 85  8

```

```
> obj.gsMMD <- gsMMD2(eSet1, memSubjects, memIni, transformFlag = TRUE,
+   transformMethod = "boxcox", scaleFlag = TRUE, quiet = FALSE)
```

```
Programming is running. Please be patient...
Data transformation ( boxcox ) performed
Gene profiles are scaled so that they have mean zero and variance one!
Programming is running. Please be patient...
```

```
*****
```

```
Initial parameter estimates>>
```

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.070	0.850	0.080	0.494	0.734	0.016	-0.322	0.927
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
0.006	0.000	1.000	0.000	-0.654	0.546	0.096	0.426
sigma2.n3	rho.n3						
0.795	0.030						

```
Initial loglikelihood>>
```

```
[1] -5313.98
```

```
Final parameter estimates>>
```

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.049	0.906	0.044	0.557	0.563	-0.069	-0.363	0.908
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
-0.045	0.000	0.974	-0.027	-0.808	0.292	0.061	0.527
sigma2.n3	rho.n3						
0.715	-0.023						

```
Final loglikelihood>>
```

```
[1] -5284.364
```

```
*****
```

```
> para <- obj.gsMMD$para
> print(round(para, 3))
```

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.049	0.906	0.044	0.557	0.563	-0.069	-0.363	0.908
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
-0.045	0.000	0.974	-0.027	-0.808	0.292	0.061	0.527
sigma2.n3	rho.n3						
0.715	-0.023						

```
or
```

```
> library(GeneSelectMMD)
> library(ALL)
> data(ALL)
> eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]
> mat <- exprs(eSet1)
> mem.str <- as.character(eSet1$BT)
> nSubjects <- length(mem.str)
> memSubjects <- rep(0, nSubjects)
```

```

> memSubjects[mem.str == "T2"] <- 1
> myWilcox <- function(x, memSubjects, alpha = 0.05) {
+   xc <- x[memSubjects == 1]
+   xn <- x[memSubjects == 0]
+   m <- sum(memSubjects == 1)
+   res <- wilcox.test(x = xc, y = xn, conf.level = 1 - alpha)
+   res2 <- c(res$p.value, res$statistic - m * (m + 1)/2)
+   names(res2) <- c("p.value", "statistic")
+   return(res2)
+ }
> tmp <- t(apply(mat, 1, myWilcox, memSubjects = memSubjects))
> colnames(tmp) <- c("p.value", "statistic")
> memIni <- rep(2, nrow(mat))
> memIni[tmp[, 1] < 0.05 & tmp[, 2] > 0] <- 1
> memIni[tmp[, 1] < 0.05 & tmp[, 2] < 0] <- 3
> print(table(memIni))

memIni
 1  2  3
 7 85  8

> obj.gsMMD <- gsMMD2.default(mat, memSubjects, memIni = memIni,
+   transformFlag = TRUE, transformMethod = "boxcox", scaleFlag = TRUE)

```

Programming is running. Please be patient...
Programming is running. Please be patient...

```

> para <- obj.gsMMD$para
> print(round(para, 3))

```

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.049	0.906	0.044	0.557	0.563	-0.069	-0.363	0.908
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
-0.045	0.000	0.974	-0.027	-0.808	0.292	0.061	0.527
sigma2.n3	rho.n3						
0.715	-0.023						

Actually, the two sample Wilcoxon rank-sum test is implemented in the *GeneSelectMMD*. The above code is used as an illustration on how to use the functions *gsMMD2* and *gsMMD2.default*.

Note that the speed of the four functions is slow for large data sets. So we recommend that the program be in background mode if it is run in Unix or Linux environment.

4 Error rates estimated for real microarray data sets

For real microarray data sets, the classical gene selection methods, such as two-sample t-test, two-sample Wilcoxon rank-sum test, could not provide the estimates of error rates such as false discovery rate (denoted as FDR; it is the percentage of nondifferentially expressed genes among selected genes), false non-discovery rate (denoted as FNDR; it is the percentage of differentially expressed genes among unselected genes), false positive rate (denoted as FPR; it is the percentage of selected genes among nondifferentially expressed genes), and false negative rate (denoted as FNR; it is the percentage of un-selected genes among differentially expressed genes), since the true gene cluster membership is unknown.

However, model-based gene selection methods (e.g., eLNN and eGG proposed by Lo and Gottardo (2007), and the method proposed by Qiu et al.'s (2008)) could easily estimate these error rates, since these error rates are functions of some probabilities which are in turn the functions of model parameters.

The function `errRates` is used to estimate FDR, FNDR, FPR, and FNR based on the objects returned by the four gene selection functions mentioned in the previous section. This function returns a 4×1 vector with elements FDR, FNDR, FPR, and FNR.

For example,

```
> library(GeneSelectMMD)
> library(ALL)
> data(ALL)
> eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]
> mem.str <- as.character(eSet1$BT)
> nSubjects <- length(mem.str)
> memSubjects <- rep(0, nSubjects)
> memSubjects[mem.str == "T2"] <- 1
> obj.gsMMD <- gsMMD(eSet1, memSubjects, transformFlag = TRUE,
+   transformMethod = "boxcox", scaleFlag = TRUE, quiet = FALSE)
```

Programming is running. Please be patient...

Data transformation (boxcox) performed

Gene profiles are scaled so that they have mean zero and variance one!

Programming is running. Please be patient...

***** initial parameter estimates method>> Ttest *****

paraIniMat[,i]>>

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.050	0.870	0.080	0.556	0.604	0.003	-0.363	0.947
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
0.001	0.000	1.000	0.000	-0.659	0.513	0.097	0.430
sigma2.n3	rho.n3						
0.812	0.028						

llkhVec>>

Ttest
-5284.364

Initial parameter estimates>>

	Ttest
pi.1	0.050
pi.2	0.870
pi.3	0.080
mu.c1	0.556
sigma2.c1	0.604
rho.c1	0.003
mu.n1	-0.363
sigma2.n1	0.947
rho.n1	0.001
mu.2	0.000
sigma2.2	1.000
rho.2	0.000

```
mu.c3      -0.659
sigma2.c3  0.513
rho.c3     0.097
mu.n3      0.430
sigma2.n3  0.812
rho.n3     0.028
```

```
Initial loglikelihood>>
  Ttest
-5308.485
```

```
Final parameter estimates based on initial estimates>>
```

```
      Ttest
pi.1   0.049
pi.2   0.906
pi.3   0.044
mu.c1  0.557
sigma2.c1 0.563
rho.c1 -0.069
mu.n1 -0.363
sigma2.n1 0.908
rho.n1 -0.045
mu.2   0.000
sigma2.2 0.974
rho.2  -0.027
mu.c3  -0.808
sigma2.c3 0.292
rho.c3  0.061
mu.n3  0.527
sigma2.n3 0.715
rho.n3 -0.023
```

```
Final loglikelihood based on initial estimates>>
  Ttest
-5284.364
```

```
Final parameter estimates>>
```

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.049	0.906	0.044	0.557	0.563	-0.069	-0.363	0.908
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
-0.045	0.000	0.974	-0.027	-0.808	0.292	0.061	0.527
sigma2.n3	rho.n3						
0.715	-0.023						

```
Final loglikelihood>>
```

```
  Ttest
-5284.364
```

```
*****
```

```
> print(round(errRates(obj.gsMMD), 3))
```

```
  FDR  FNDR  FPR  FNR
```

0.011 0.005 0.001 0.048

5 Visualizing the fit of the model to a real microarray data set

In general, it is difficult to visualize the fit of the model to a real microarray data set since the data are in high-dimensional space. However, it is possible to do so for the special case where the tissue samples within a tissue type are marginally independent. In this case, we can pool all gene expression levels together since they are all independent, and regard them as one-dimensional data. Next, we can impose the density estimate onto the histogram of this pooled data.

The function `plotHistDensity` is used for such purpose. The following R code illustrates the usage of `plotHistDensity`:

```
> library(GeneSelectMMD)
> library(ALL)
> data(ALL)
> eSet1 <- ALL[1:100, ALL$BT == "B3" | ALL$BT == "T2"]
> mem.str <- as.character(eSet1$BT)
> nSubjects <- length(mem.str)
> memSubjects <- rep(0, nSubjects)
> memSubjects[mem.str == "T2"] <- 1
> obj.gsMMD <- gsMMD(eSet1, memSubjects, transformFlag = TRUE,
+   transformMethod = "boxcox", scaleFlag = TRUE, quiet = FALSE)
```

Programming is running. Please be patient...

Data transformation (boxcox) performed

Gene profiles are scaled so that they have mean zero and variance one!

Programming is running. Please be patient...

***** initial parameter estimates method>> Ttest *****

paraIniMat[,i]>>

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.050	0.870	0.080	0.556	0.604	0.003	-0.363	0.947
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
0.001	0.000	1.000	0.000	-0.659	0.513	0.097	0.430
sigma2.n3	rho.n3						
0.812	0.028						

llkhVec>>

Ttest

-5284.364

Initial parameter estimates>>

	Ttest
pi.1	0.050
pi.2	0.870
pi.3	0.080
mu.c1	0.556
sigma2.c1	0.604
rho.c1	0.003
mu.n1	-0.363
sigma2.n1	0.947

```
rho.n1    0.001
mu.2      0.000
sigma2.2  1.000
rho.2     0.000
mu.c3     -0.659
sigma2.c3 0.513
rho.c3    0.097
mu.n3     0.430
sigma2.n3 0.812
rho.n3    0.028
```

Initial loglikelihood>>

```
  Ttest
-5308.485
```

Final parameter estimates based on initial estimates>>

```
  Ttest
pi.1     0.049
pi.2     0.906
pi.3     0.044
mu.c1    0.557
sigma2.c1 0.563
rho.c1   -0.069
mu.n1   -0.363
sigma2.n1 0.908
rho.n1  -0.045
mu.2     0.000
sigma2.2 0.974
rho.2   -0.027
mu.c3   -0.808
sigma2.c3 0.292
rho.c3   0.061
mu.n3    0.527
sigma2.n3 0.715
rho.n3  -0.023
```

Final loglikelihood based on initial estimates>>

```
  Ttest
-5284.364
```

Final parameter estimates>>

pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.049	0.906	0.044	0.557	0.563	-0.069	-0.363	0.908
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
-0.045	0.000	0.974	-0.027	-0.808	0.292	0.061	0.527
sigma2.n3	rho.n3						
0.715	-0.023						

Final loglikelihood>>

```
  Ttest
-5284.364
```

```
> para <- obj.gsMMD$para  
> print(round(para, 3))
```

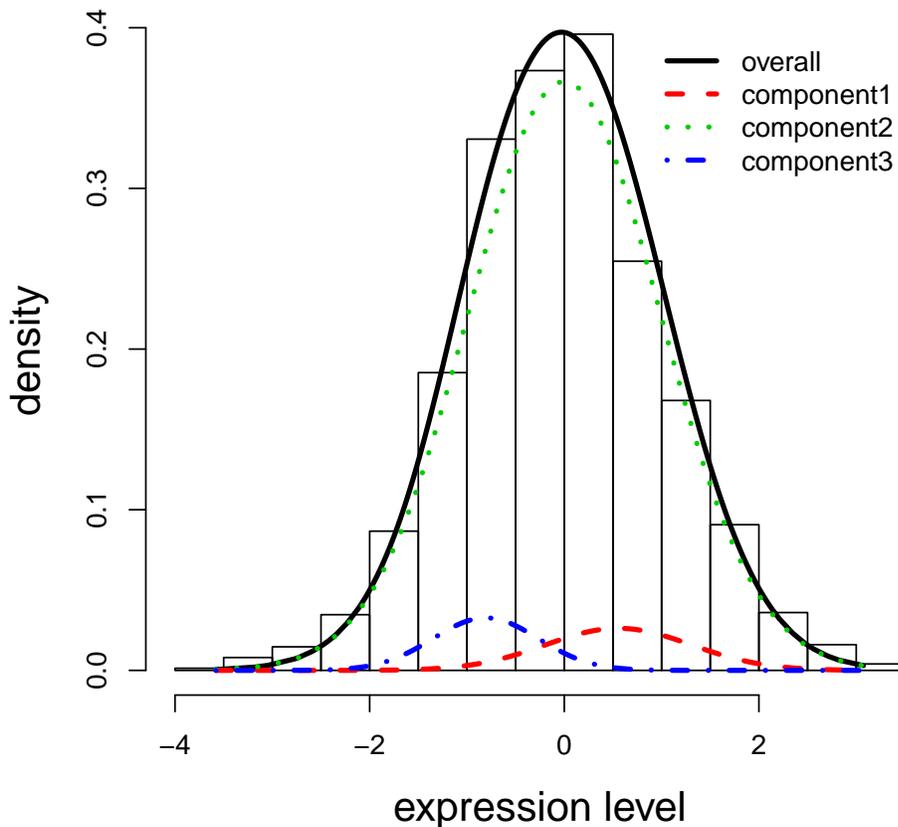
pi.1	pi.2	pi.3	mu.c1	sigma2.c1	rho.c1	mu.n1	sigma2.n1
0.049	0.906	0.044	0.557	0.563	-0.069	-0.363	0.908
rho.n1	mu.2	sigma2.2	rho.2	mu.c3	sigma2.c3	rho.c3	mu.n3
-0.045	0.000	0.974	-0.027	-0.808	0.292	0.061	0.527
sigma2.n3	rho.n3						
0.715	-0.023						

```
> print(round(errRates(obj.gsMMD), 3))
```

FDR	FNDR	FPR	FNR
0.011	0.005	0.001	0.048

```
> plotHistDensity(obj.gsMMD, plotFlag = "case", mytitle = "Histogram of gene expression levels for T2\n",  
+ plotComponent = TRUE, x.legend = c(0.8, 3), y.legend = c(0.3,  
+ 0.4), numPoints = 500, cex.main = 1, cex = 1)
```

**Histogram of gene expression levels for T2
imposed with estimated density (case)**



6 Discussion

The speeds of the four gene selection functions described in Section 3 are slow. One way to improve the speed is to embed Fortran or C code in the R code. We will take such an approach in the future version of the *GeneSelectMMD*.

References

- [1] Chiaretti, S., Li, X., Gentleman, R., Vitale, A., Vignetti, M., Mandelli, F., Ritz, J., and Foa, R. Gene expression profile of adult t-cell acute lymphocytic leukemia identifies distinct subsets of patients with different response to therapy and survival. *Blood*, 103:2771–2778, 2004.
- [2] Dempster, A., Laird, N., and Rubin, D. Likelihood from incomplete data via the em algorithm. *Journal of the Royal Statistical Society, Series B*, 39(1):1–38, 1977.
- [3] Lo, K. and Gottardo, R. Flexible empirical bayes models for differential gene expression. *Bioinformatics*, 23:328–335, 2007.
- [4] Qiu, W.-L., He, W., Wang, X.-G., and Lazarus, R. A marginal mixture model for selecting differentially expressed genes across two types of tissue samples. *The International Journal of Biostatistics*, 4(1):Article 20, 2008.