IPPD package vignette

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This is the vignette of the Bioconductor add-on package IPPD which implements automatic isotopic pattern extraction from a raw protein mass spectrum. Basically, the user only has to provide mass/charge channels and corresponding intensities, which are automatically decomposed into a list of monoisotopic peaks. IPPD can handle several charge states as well as overlaps of peak patterns.

Abstract

1 Aims and scope of IPPD

A crucial challenge in the analysis of protein mass spectrometry data is to automatically process the raw spectrum to a list of peptide masses. IPPD is tailored to spectra where peptides emerge in the form of isotope patterns, i.e. one observes several peaks for each peptide mass at a given charge state due to the natural abundance of heavy isotopes. Datasets with a size of up to 100,000 mass/charge channels and the presence of isotope patterns at multiple charge states frequently exhibiting overlap make the manual annotation of a raw spectrum a tedious task. IPPD provides functionality to perform this task in a fully automatic, transparent and user-customizable way. Basically, one feeds the raw spectrum into one single function to obtain a list of monoisotopic peaks described by a mass/charge channel, a charge and an intensity. What makes our approach particularly user-friendly is its dependence on only a small set of easily interpretable parameters. We also offer a method to display the decomposition of the spectrum graphically, thereby facilitating a manual validation of the output.

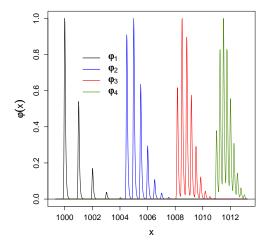
2 Methodology

2.1 Template model

In the context of this package, a protein mass spectrum is understood as a sequence of pairs $\{x_i, y_i\}_{i=1}^n$, where $x_i = m_i/z_i$ is a mass (m_i) per charge (z_i) value (measured in Thomson) and y_i is the intensity, i.e. the abundance of a particular mass (modulo charge state), observed at x_i , i = 1, ..., n, which are assumed to be in an increasing order. The y_i are modeled as a linear combination of template functions representing prior knowledge about

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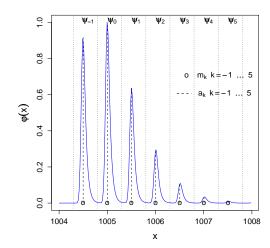


Figure 1: Illustration of the template construction as described in the text. The left panel depicts different templates of different charge states (1 to 4). The right panel zooms at the charge two template φ_2 .

peak shapes and the composition of isotopic patterns. If our model were exact, we could write

$$\mathbf{y} = \mathbf{\Phi} \boldsymbol{\beta}^*, \quad \mathbf{y} = (y_1, \dots, y_n)^\top,$$
 (1)

where Φ is a matrix template functions and β^* a vector of weights for each template. Only a small fraction of all templates are needed to fit the signal, i.e. β^* is highly sparse. Since $y \geq 0$, where ' \geq ' is understood componentwise, all template functions are nonnegative and accordingly $\beta^* \geq 0$. Model (1) can equivalently be written as

$$\boldsymbol{y} = \begin{bmatrix} \boldsymbol{\Phi}_1 & \dots & \boldsymbol{\Phi}_C \end{bmatrix} \begin{bmatrix} \boldsymbol{\beta}_1^* \\ \vdots \\ \boldsymbol{\beta}_C^* \end{bmatrix} = \sum_{c=1}^C \boldsymbol{\Phi}_c \boldsymbol{\beta}_c^*, \tag{2}$$

where Φ_c, β_c^* denote the matrix of template functions and weight vector to fit isotopic patterns of a particular charge state c, c = 1, ..., C. Each submatrix Φ_c can in turn be divided into columns $\varphi_{c,1}, ..., \varphi_{c,p_c}$, where the entries of each column vector store the evaluations of a template φ_{c_j} , $j = 1, ..., p_c$, at the x_i , i = 1, ..., n. Each template $\varphi_{c,j}$ depends on parameter $m_{c,j}$ describing the m/z position at which $\varphi_{c,j}$ is placed. A template $\varphi_{c,j}$ is used to fit an isotopic pattern of peaks composed of several single peaks, which is modeled as

$$\varphi_{c,j} = \sum_{k \in Z_{c,j}} a_{c,j,k} \, \psi_{c,j,k,\boldsymbol{\theta}_{c,j}}, \quad Z_{c,j} \subset \mathbb{Z}$$
(3)

where the $\psi_{c,j,k}$ are functions representing a peak of a single isotope within an isotopic pattern. They depend on $m_{c,j}$ and a parameter vector $\boldsymbol{\theta}_{c,j}$. The nonnegative weights $a_{c,j,k}$ reflect the relative abundance of the isotope indexed by k. The $a_{c,j,k}$ are computed according to the averagine model (Senko et al. [1995]) and hence are fixed in advance. Each $\psi_{c,j,k}$ is linked to a location $m_{c,j,k}$ at which it attains its maximum. The $m_{c,j,k}$ are calculated

from $m_{c,j}$ as $m_{c,j,k} = m_{c,j} + \kappa \frac{k}{c}$, where κ equals 1 Dalton (≈ 1.003). The rationale behind Eq. (3) and the definitions that follow is the fact that the location of the most intense isotope is taken as characteristic location of the template, i.e. we set $m_{c,j,0} = m_{c,j}$ so that the remaining $m_{c,j,k}$, $k \neq 0$, are computed by shifting $m_{c,j}$ in both directions on the m/z axis. By 'most intense isotope', we mean that $a_{c,j,0} = \max_k a_{c,j,k} = 1$. The set $Z_{c,j}$ is a subset of the integers which depends on the averagine model and a pre-specified tolerance, i.e. we truncate summation in Eq. (3) if the weights drop below that tolerance. Figure 1 illustrates the construction scheme and visualizes our notation.

2.2 Peak shape

In an idealized setting, the $\psi_{c,j,k}$ are delta functions at specific locations. In practice, however, the shape of a peak equals that of a bump which may exhibit some skewness. In the case of no to moderate skewness, we model peaks by Gaussian functions:

$$\psi_{c,j,k}(x) = \exp\left(-\frac{(x - m_{c,j,k})^2}{\sigma_{c,j}}\right). \tag{4}$$

The parameter to be determined is $\theta_{c,j} = \sigma_{c,j} > 0$. In the case of considerable skewness, peaks are modeled by exponentially modified Gaussian (EMG) functions, see for instance Grushka [1972], Marco and Bombi [2001], and Schulz-Trieglaff et al. [2007] in the context of protein mass spectrometry:

$$\psi_{c,j,k}(x) = \frac{1}{\alpha_{c,j}} \exp\left(\frac{\sigma_{c,j}^2}{2\alpha_{c,j}^2} + \frac{\mu_{c,j} - (x - m_{c,j,k})}{\alpha_{c,j}}\right) \left(1 - F\left(\frac{\sigma_{c,j}}{\alpha_{c,j}} + \frac{\mu_{c,j} - (x - m_{c,j,k})}{\sigma_{c,j}}\right)\right),$$

$$F(t) = \int_{-\infty}^{t} \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{u^2}{2}\right) du.$$
(5)

The EMG function involves a vector of three parameters $\boldsymbol{\theta}_{c,j} = (\alpha_{c,j}, \sigma_{c,j}, \mu_{c,j})^{\top} \in \mathbb{R}^+ \times \mathbb{R}$. The parameter $\alpha_{c,j}$ controls the additional length of the right tail as compared to a Gaussian. For $\alpha_{c,j} \downarrow 0$, the EMG function becomes a Gaussian. For our fitting approach as outlined in Section 2.3, it is crucial to estimate the $\boldsymbol{\theta}_{c,j}$, which are usually unknown, from the data as good as possible. To this end, we model each component θ_l of $\boldsymbol{\theta}$ as a linear combination of known functions $g_{l,m}$ of x = m/z and an error component ε_l , i.e.

$$\theta_l(x) = \sum_{m=1}^{M_l} \nu_{l,m} g_{l,m}(x) + \varepsilon_l(x). \tag{6}$$

In the case of no prior knowledge about the $g_{l,m}$, we model θ_l as a constant independent of x. In most cases, it is sensible to assume a linear trend, i.e. $\theta_l(x) = \nu_{l,1} + \nu_{l,2}x$. In order to fit a model of the form (6), we have to collect information from the data $\{x_i, y_i\}_{i=1}^n$. To be precise, we proceed according to the following steps.

- 1. We apply a simple peak detection algorithm to the spectrum to identify disjoint regions $\mathcal{R}_r \subset \{1, \dots, n\}, \ r = 1, \dots, R$, of well-resolved peaks.
- 2. For each region r, we fit the chosen peak shape to the data $\{x_i, y_i\}_{i \in \mathcal{R}_r}$ using nonlinear least squares:

$$\min_{\boldsymbol{\theta}} \sum_{i \in \mathcal{R}_r} (y_i - \psi_{\boldsymbol{\theta}}(x_i))^2, \tag{7}$$

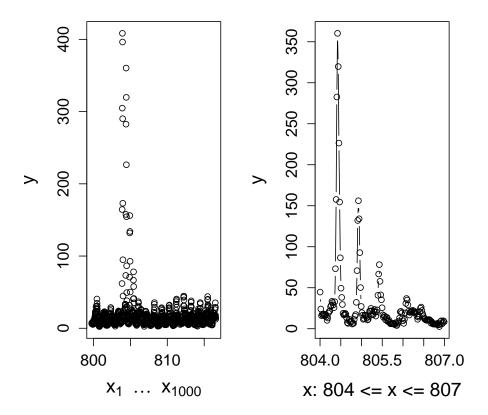
yielding an estimate $\widehat{\boldsymbol{\theta}}_r(\widehat{x}_r)$, where \widehat{x}_r denotes an estimation for the mode of the peak in region \mathcal{R}_r .

3. The sequence $\{\widehat{x}_r, \widehat{\boldsymbol{\theta}}_r\}_{r=1}^R$ is then used as input for the estimation of the parameters $\nu_{l,m}$ in model (6).

Step 2. is easily solved by the general purpose nonnegative least squares routine nls in R:::stats for a Gaussian peak shape. For the EMG, we have to perform a grid search over all three parameters to find a suitable starting value, which is then passed to the general purpose optimization routine optim in R:::stats with the option method = "BFGS" and a specification of a closed form expression of the gradient via the argument gr. For step 3., we use least absolute deviation regression because of the presence of outliers arising from less well-resolved, wiggly or overlapping peaks. The whole procedure is performed by the function fitModelParameters as demonstrated below. After loading the package, we access the real world dataset myo500 and extract m/z channels (x) and the corresponding intensities (y). For computational convenience and since they contain very few relevant information, we discard all channels above 2500.

```
R> library(IPPD)
R> data(myo500)
R> x <- myo500[,"mz"]
R> y <- myo500[,"intensities"]
R> y <- y[x <= 2500]
R> x <- x[x <= 2500]</pre>
```

To have a look at the data, we plot the first 1000 (x,y) pairs:



In the plot, one identifies a prominent peak pattern beginning at about 804, which is zoomed at in the right panel.

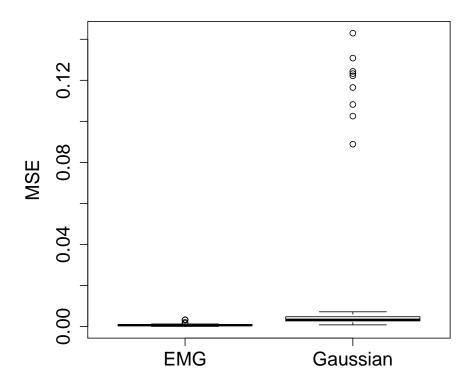
We now apply fitModelParameters to fit model (6) for the width parameter σ of a Gaussian function (4). For simplicity, we take $g_1(x) = 1$, $g_2(x) = x$. The model is specified by using an R formula interface.

An analogous command for the EMG (5) with the model formulae $\alpha(x) = \nu_{1,1} + \nu_{1,2}x$, $\sigma(x) = \nu_{2,1} + \nu_{2,2}x$, $\mu(x) = \nu_{3,1}$ is given by

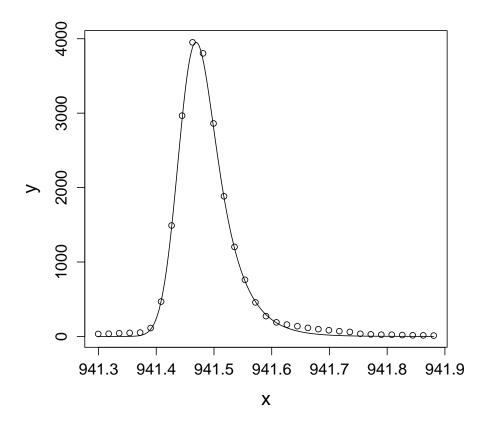
Inspecting the results, we find that R=55 peak regions are used to fit an EMG parameter model. Moreover, it turns out that the EMG model is a more appropriate peak model for the data when visually comparing the list of mean residual sums of squares of the EMG fits and the Gauss fits extracted from slot(fitEMG, "peakfitresults") and

slot(fitGauss, "peakfitresults"), respectively. The figure shows an example where the EMG shape comes relatively close to the observed data. A long right tail indicates that a Gaussian would yield a rather poor fit here.

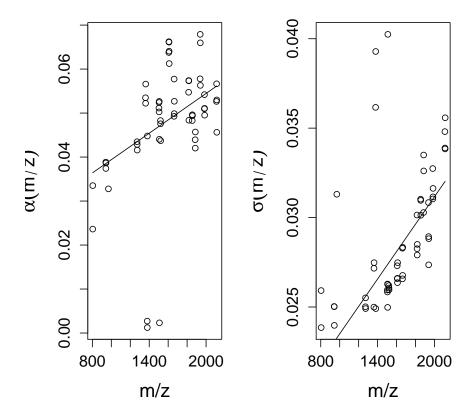
```
R> show(fitEMG)
```



R> visualize(fitEMG, type = "peak", cex.lab = 1.5, cex.axis = 1.25)



To assess the fit of the two linear models for the EMG parameters α and σ , we use again the function visualize as follows:



While the fit for σ seems to be reasonable except for some extreme outliers, the fit for α is not fully convincing. Nevertheless, in the absence of further knowledge, the fit produces good results in the template matching step detailed in the next section.

2.3 Template fitting

Once all necessary parameters have been determined, the positions at which the templates are placed have to be fixed. In general, one has to choose positions from the interval $[x_1, x_n]$. We instead restrict us to a suitable subset of the finite set $\{x_i\}_{i=1}^n$. The deviations from the true positions is then at least in the order of the sampling rate, but this can be improved by means of a postprocessing step described in 2.4. Using the whole set $\{x_i\}_{i=1}^n$ may be computationally infeasible if n is large. Such an approach would be at least computationally wasteful, since 'genuine' peaks patterns occur very sparsely in the spectrum. Therefore, we apply a pre-selection step on the basis of what we term 'local noise level' (LNL). The LNL is defined as a quantile (typically the median) of the intensities y_i falling into a sliding window of fixed width around a specific position. Given the LNL, we place templates on an x_i (one for each charge state) if and only if the corresponding y_i exceeds the LNL at x_i by a factor factor.place, which typically equals three or four and has to be specified by the user. Given the positions of the templates, we compute the matrix Φ according to Eqs. (1) and (3). It then remains to estimate the coefficient vector β^* on the basis of two structural assumptions, sparsity and nonnegativity of all quantities involved. Related approaches in the literature (Du and Angeletti [2006], Renard et al. [2008]) account for sparsity of β^* by using ℓ_1 -regularized regression (Tibshirani [1996]). We here argue empirically that ℓ_1 regularization is not the best to do, since it entails the selection of a tuning parameter which is difficult to choose in our setting, and secondly the structural constraints concerning nonnegativity turn out to be so strong that sparsity is more conveniently achieved by fitting followed by hard thresholding. We first determine

$$\widehat{\boldsymbol{\beta}} \in \underset{\boldsymbol{\beta}}{\operatorname{argmin}} \|\boldsymbol{y} - \boldsymbol{\Phi}\boldsymbol{\beta}\|_{q}^{q}, \quad q = 1 \text{ or } q = 2,$$
subject to $\boldsymbol{\beta} \ge 0.$ (8)

The optimization problem (8) is a quadratic (q = 2) or linear (q = 1) program and is solved using standard techniques (Boyd and Vandenberghe [2004]); we omit further details here. We remark that in the presence of high noise, it is helpful to subtract the LNL from y. Concerning the choice of q, we point out that q = 1 can cope better with deviations from model assumptions, i.e. deviations from the averagine model or from the peak model and thus may lead to a reduction of the number of false positives.

2.4 Postprocessing

Given an estimate $\widehat{\beta}$, we define $\mathcal{M}_c = \{m_{c,j} : \widehat{\beta}_{c,j} > 0\} \subset \{x_i\}_{i=1}^n, c = 1, \ldots, C$, as the set of all template locations where the corresponding coefficient exceeds 0, separately for each charge. Due to a limited sampling rate, different sources of noise and model misfit, the locations in the sets $\{\mathcal{M}_c\}_{c=1}^C$ may still deviate considerably from the set of true peak pattern locations. Specifically, the sets $\{\mathcal{M}_c\}_{c=1}^C$ tend to be too large, mainly caused by what we term 'peak splitting': for the reasons just mentioned, it frequently occurs that several templates are used to fit the same peak. This can at least partially be corrected by means of the following merging procedure.

- 1. Separately for each c, divide the sets \mathcal{M}_c into groups $\mathcal{G}_{c,1}, \ldots, \mathcal{G}_{c,G_c}$ of 'adjacent' positions. Positions are said to be adjacent if their distance on the m/z scale is below a certain tolerance as specified via a parts per million (ppm) value.
- 2. For each c = 1, ..., C and each group $g_c = 1, ..., G_c$, we solve the following optimization problem.

$$(\widetilde{m}_{c,g}, \widetilde{\beta}_{c,g}) = \min_{m_{c,g}, \beta_{c,g}} \left\| \sum_{m_{c,j} \in \mathcal{G}_{c,g}} \widehat{\beta}_{c,j} \psi_{m_{c,j}} - \beta_{c,g} \psi_{m_{c,g}} \right\|_{L^2}^2$$

$$(9)$$

In plain words, we take the fitted function resulting from the functions $\{\psi_{m_{c,j}}\}$ representing the most intense peak of each peak pattern in the same group and then determine a function $\psi_{\widetilde{m}_{c,g}}$ placed at location $\widetilde{m}_{c,g}$ and weighted by $\widetilde{\beta}_{c,g}$ such that $\widetilde{\beta}_{c,g}\psi_{\widetilde{m}_{c,g}}$ approximates the fit of multiple functions $\{\psi_{m_{c,j}}\}$ best (in a least squares sense).

3. One ends up with sets $\widetilde{\mathcal{M}}_c = \{\widetilde{m}_{c,g}\}_{g=1}^{G_c}$ and coefficients $\{\widetilde{\beta}_{c,g}\}_{g=1}^{G_c}, \ c=1,\ldots,C$.

The additional benefit of step 2. as compared to the selection of the function with the largest coefficient as proposed in Renard et al. [2008] is that, in the optimal case, we are able to determine the peak pattern location even more accurate as predetermined by a limited sampling rate. The integral in (9) can be solved analytically for a Gaussian function, and we resort to numeric approximations for the EMG function.

The sets $\{\mathcal{M}_c\}$ tend to be too large in the sense that they still contain noise peak patterns.

Therefore, we apply hard thresholding to the $\{\widetilde{\beta}_{c,g}\}_{g=1}^{G_c}$, $c=1,\ldots,C$, discarding all positions where the corresponding coefficients is less than a significance level times the LNL, where the significance level has to be specified by the user.

3 Case study

R>

We continue the data analysis starting in Section 2.2. The methodology of the Sections 2.3 and 2.4 is implemented in the function getPeaklist. For the computation of the template functions, we recycle the object fitEMG obtained in Section 2.2.

```
R> EMGlist <- getPeaklist(mz = x, intensities = y, model = "EMG",
  model.parameters = fitEMG,
  loss = "L2", trace = FALSE,
  control.localnoise = list(factor.place = 2),
  control.basis = list(charges = c(1, 2)),
  control.postprocessing = list(ppm = 200))
R> show(EMGlist)

An object of class 'peaklist'(with postprocessing)
Loss function used: L2
Peak model used: EMG
number of peaks: 1222
charge states used: 1,2
```

The argument list can be summarized as follows: we compute EMG templates for charges 1 and 2; templates are placed on all m/z-positions in the spectrum where the intensity is at least two times the LNL; the fit is least squares (loss = L2); postprocessing is performed by merging peaks within a tolerance of 200 ppm. Subsequently, only the patterns with signal-to-noise ratio bigger than three are maintained. The result is of the following form.

R> threshold(EMGlist, threshold = 3, refit = TRUE, trace = FALSE)

	loc_init	loc_most_intense	charge	quant	amplitude	localnoise	ratio
[1,]	800.4642	800.4642	1	79.44171	50.27412	9.411770	5.341622
[2,]	808.2414	808.2414	1	80.36531	50.66381	10.196100	4.968940
[3,]	829.2292	829.2292	1	93.77411	58.50957	9.411770	6.216638
[4,]	842.4935	842.4935	1	65.95699	40.88386	8.366010	4.886901
[5,]	864.4065	864.4065	1	142.82412	87.56382	13.333300	6.567303
[6,]	877.0373	877.0373	1	115.96763	70.64737	8.888890	7.947828
[7,]	908.4247	908.4247	1	77.95284	46.74333	8.104580	5.767521
[8,]	908.9339	908.9339	1	57.31053	34.35736	9.411770	3.650467
[9,]	923.4380	923.4380	1	71.87828	42.78496	7.581700	5.643188
[10,]	924.4543	924.4543	1	72.75010	43.28165	8.366010	5.173511
[11,]	927.4746	927.4746	1	109.40242	64.99113	8.888890	7.311501
[12,]	927.9689	927.9689	1	60.24687	35.78139	9.934640	3.601680
[13,]	941.4672	941.4672	1	6891.22617	4065.63758	12.549000	323.981001

[14,]	941.6761	941.6761	1	135.99121	80.21991	13.594800	5.900779
[15,]	942.4249	942.4249	1	271.89433	160.32337	16.732000	9.581841
[16,]	949.4364	949.4364	1	71.81278	42.19824	7.320260	5.764582
[17,]	952.5318	952.5318	1	76.11906	44.65963	7.843140	5.694100
[18,]	954.4820	954.4820	1	106.27461	62.29085	8.104580	7.685882
[19,]	963.4553	963.4553	1	148.93819	86.90358	6.535950	13.296243
[20,]	967.4826	967.4826	1	145.35818	84.64446	8.104580	10.444028
[21,]	969.4694	969.4694	1	262.52701	152.71772	10.457500	14.603655
[22,]	985.4424	985.4424	1	125.56473	72.45638	7.320260	9.898061
[23,]	991.5025	991.5025	1	143.70718	82.66916	9.411770	8.783593
[24,]	992.0244	992.0244	1	126.06477	72.50155	10.196100	7.110714
[25,]	999.4665	999.4665	1	153.63639	88.02239	7.320260	12.024490
[26,]	1023.4509	1023.4509	1	72.97907	41.20077	6.535950	6.303715
[27,]	1057.4478	1057.4478	1	61.59667	34.04018	7.320260	4.650132
[28,]	1086.5573	1086.5573	1	163.01496	88.42496	6.013070	14.705459
[29,]	1125.5187	1125.5187	1	82.19554	43.60907	6.797390	6.415561
[30,]	1151.4789	1151.4789	1	97.86695	51.21042	5.751630	8.903636
[31,]	1168.6235	1168.6235	1	88.00301	45.62521	6.274510	7.271517
[32,]	1192.7011	1192.7011	1	73.30105	37.50774	6.535950	5.738682
	1271.6609	1271.6609	1	3373.48516	1646.58238	10.457500	157.454686
	1297.6800	1297.6800	1	143.23353	68.79630	7.581700	9.073995
	1360.7611	1360.7611	1	3816.68284	1720.04542		131.583428
	1361.7379	1361.7379	1	1393.29903	627.25628	20.653600	30.370312
	1378.8379	1378.8379	1	2998.22323	1325.43023	15.686300	84.496040
	1394.8413	1394.8413	1	133.38789	57.95847	9.150330	6.334030
	1474.6387	1474.6387	1	154.35942	63.76082	9.934640	6.418030
	1484.6606	1484.6606	1	554.63354	227.67786	11.764700	19.352628
	1500.6588	1500.6588	1	186.99609	76.00861	14.902000	5.100564
		1501.6659	1	237.89801	96.64897	20.130700	4.801074
_ , _	1502.6668	1502.6668	1	6512.21157	2644.08690	27.973900	94.519781
		1506.9383	1	1362.31089	551.93861	18.039200	30.596623
	1518.6637	1518.6637	1	3192.22390	1285.24470	14.902000	86.246457
	1519.6113	1519.6113	1	167.63469	67.46108	15.424800	4.373546
	1524.6527	1524.6527	1				
-	1534.6603	1534.6603	1	271.30995		12.287600	
	1546.6550	1546.6550	1	180.74009		10.196100	
-	1588.8538	1588.8538	1	206.83112		12.287600	
-	1589.8317	1589.8317	1	205.68088		14.379100	
-	1606.8601	1606.8601		47656.96135			666.225984
-	1622.8482	1622.8482	1	282.47915		8.104580	13.244181
	1628.8462	1628.8462	1	197.47224			9.531567
-	1632.8754	1632.8754	1	231.61121		9.673200	
	1643.8448	1643.8448	1	295.35582			
	1650.8348	1650.8348	1	219.29940		9.411770	
	1660.8520	1660.8520	1	346.30864		15.424800	8.330289
	1661.8523	1661.8523	1	7081.63368			128.752066
	1675.8106	1675.8106	1	140.11470	51.49230	7.058820	7.294746
	1683.8293	1683.8293	1	115.18095		6.535950	6.443029
	1687.8674	1687.8674	1	138.47207			
-	1712.6676	1712.6676	1				
[03,]	1112.0010	1/12.00/0	1	110.11020	41.11104	0.214010	0.007304

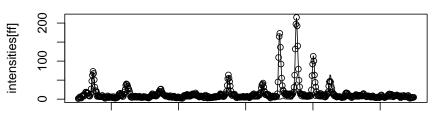
[64,]	1717.8060	1717.8060	1	100.79873	36.15212	6.274510	5.761744
[65,]	1718.8742	1718.8742	1	78.34266	28.08336	6.535950	4.296753
[66,]	1753.7102	1753.7102	1	89.35127	31.47933	5.490200	5.733731
[67,]	1777.8665	1777.8665	1	106.10240	36.93067	6.013070	6.141733
[68,]	1798.8819	1798.8819	1	175.36139	60.38655	7.581700	7.964777
[69,]	1815.9052	1815.9052	1	9222.12485	3149.05349	24.052300	130.925254
[70,]	1831.9004	1831.9004	1	327.93021	111.10564	5.751630	19.317245
[71,]	1837.8935	1837.8935	1	368.32473	124.41966	6.274510	19.829382
[72,]	1847.8954	1848.9034	1	373.93788	125.76833	6.274510	20.044327
[73,]	1852.9575	1853.9655	1	162.82744	54.75911	10.980400	4.986987
[74,]	1853.9657	1854.9737	1	2843.31788	956.19380	12.549000	76.196812
[75,]	1869.9595	1870.9675	1	428.17365	143.94914	6.013070	23.939376
[76,]	1885.0257	1886.0337	1	2133.58694	717.09062	9.150330	78.367734
[77,]	1885.9545	1886.9625	1	157.60503	52.96946	9.673200	5.475898
[78,]	1897.9419	1898.9499	1	73.78262	24.79197	4.44440	5.578199
[79,]	1901.0127	1902.0207	1	88.40222	29.69960	4.705880	6.311168
	1919.0078	1920.0158	1	146.81349	49.26205	6.013070	8.192496
	1937.0230	1938.0310	1	10570.05550	3542.22513	27.712400	127.820944
-	1953.0164	1954.0244	1	116.41570	38.97032	3.660130	10.647250
	1958.9972	1960.0052	1	146.46996	49.01071	3.921570	12.497727
	1963.0361	1964.0441	1	219.18797	73.32246	6.013070	12.193847
	1969.9485	1970.9565	1	300.77511	100.56653	4.44440	22.627492
-	1981.0615	1982.0695	1	244.81955	81.79314	13.594800	6.016502
	1982.0622	1983.0702	1	5026.45614	1679.19922		107.048776
	1994.0448	1995.0528	1	131.82469	44.00292	3.921570	11.220742
	1995.0238	1996.0318	1	80.08516	26.73049	3.660130	7.303152
-	1998.0483	1999.0563	1	86.94324	29.01351	3.398690	8.536674
	2004.0431	2005.0511	1	76.49468	25.51610	3.660130	6.971365
	2008.0804	2009.0884	1	135.36520	45.14050	3.660130	12.333031
	2039.0826	2040.0906	1	56.21756	18.70644	2.875820	6.504732
	2052.9999	2054.0079	1	68.79126	22.86797	2.352940	9.718894
	2092.1287	2093.1367	1	81.25862	26.93851	3.660130	7.359988
	2098.0541	2099.0621	1	76.68580	25.41193	3.137260	8.100039
	2105.0082	2106.0162	1		57.10590	3.398690	
	2109.1722	2110.1802	1	245.67670	81.32109	11.764700	6.912296
	2110.1592	2111.1672	1	5284.76079	1749.11770		123.896250
	2126.1453	2127.1533	1	79.79164	26.36669	2.352940	11.205849
-	2132.1398	2133.1478	1	59.99230	19.81205	2.352940	8.420124
	2136.1764	2137.1844	1	73.48747	24.25883	2.614380	9.279000
	2154.1284	2155.1364	1	41.38812	13.63760	2.091500	6.520490
	2157.9980	2159.0060	1	41.70484	13.73652	1.830070	7.506008
	2166.1065	2167.1145	1	73.99907	24.35330	2.352940	10.350156
-	2172.1089	2173.1169	1	33.40577	10.98727	1.830070	6.003744
	2188.0666	2189.0746	1	36.97282	12.14056	1.633987	7.430022
	2211.1144	2212.1224	1	68.46270	22.42148	2.091500	10.720286
	2226.1425	2227.1505	1	102.27076	33.43036	1.633987	20.459370
	2233.0991	2234.1071	1	33.83560	11.05055	1.633987	6.762931
	2257.0072	2258.0152	1	73.28647	23.86274	1.633987	14.603995
	2283.2155	2284.2235	1	182.54482	59.24115	2.091500	28.324720
-	2284.1744	2285.1824	1	24.07015	7.81053	2.091500	3.734416
			-				

[114,] 2427.2620 2428.2700 1 50.99390 16.21219 1.633987 9.921860

R>

The results can be examined in detail graphically. We finally present some selected regions to demonstrate that our method performs well. The pre-defined method visualize can be used display the template fitting at several stages for regions within selected m/z intervals as specified by the arguments lower and upper.

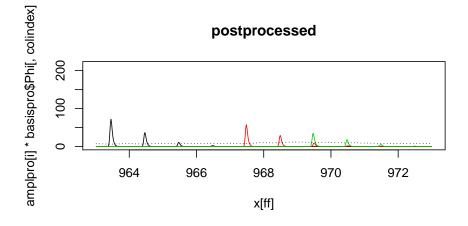
964



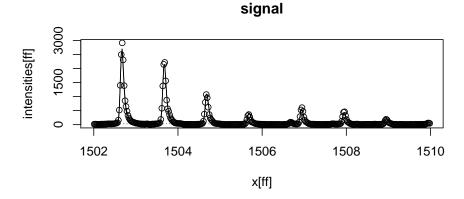
966

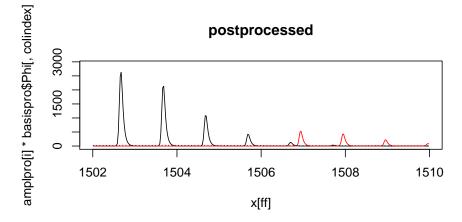
signal



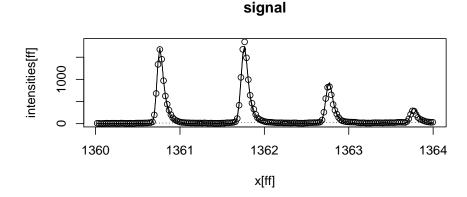


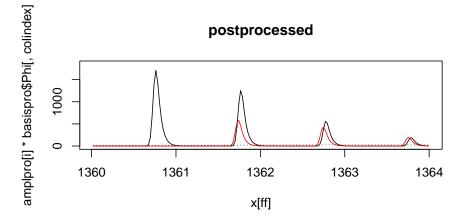
R> R>





In the m/z range [963, 973] a charge-1 peak overlaps with a more intense charge two peak. A further overlap occurs in the interval [1502, 1510], and it is correctly resolved. An even more challenging problem, in which it is already difficult to unravel the overlap by visual inspection, is displayed in the following plot.





4 Extension to process LC-MS runs

In the preceding sections, it has been demonstrated how IPPD can be used to process single spectrums. For LC-MS, multiple spectra, one for a sequence of retention times $\{t_l\}_{l=1}^L$, have to be processed. In this context, a single spectrum is referred to as scan. The resulting data can be displayed as in Figure 2 by plotting intensities over the plane defined by retention times and m/z-values. IPPD offers basic functionality to process this kind of data. Support for mzXML format as well as an implementation of the sweep line scheme as suggested in Schulz-Trieglaff et al. [2008] is provided, which is briefly demonstrated in the sequel.

The sweep line scheme aggregates the peaklists of multiple scans by looking for blocks of consecutive retention times at which there is signal at nearby m/z-positions. The output is a quadruple consisting of a retention time interval, a m/z-position, a charge state and

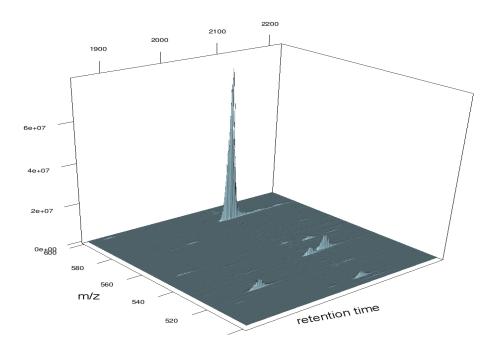


Figure 2: Graphical display of the sample mzXML file used in the code.

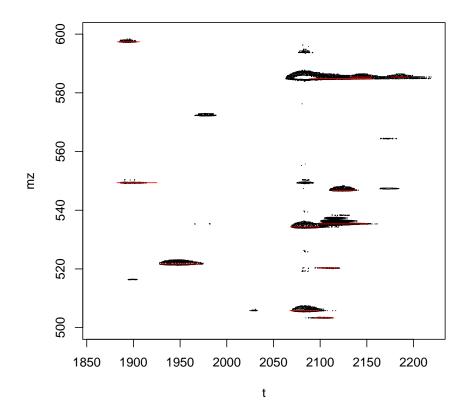
a quantification of the intensity. The intervals are found by sequentially processing the results of getPeaklist, where the results of each peaklist will lead to extensions of existing interval of preceding lists or to the creation of new intervals; intervals are closed once they have not been extended after processing more than gap additional peaklists, where gap is a parameter to be specified by the user. For more details, we refer to Schulz-Trieglaff et al. [2008]. The function analyzeLCMS runs getPeaklist for each scan and then calls the function sweepline, which can as well be run independently from analyzeLCMS to aggregate the results. While there is a default setting, parameters can be changed by passing appropriate arguments.

The output can be displayed as follows. The retention time intervals are given by the two columns rt_begin and rt_end , the corresponding m/z-positions are given by the column loc. Quantitive information is contained in the column quant. The output is visualized by means of a contour plot, where the contour lines depict intensities over the plane defined by m/z-positions and retention times. The intervals of the output are drawn as red lines.

R> print(boxes)

	loc	charge	quant	rt_begin	rt_end	npeaks	gapcount
[1,]	503.3474	1	4804929	2093.26	2113.46	26	6
[2,]	505.8353	2	58628590	2067.62	2097.79	34	13
[3,]	520.3157	1	4060317	2097.79	2118.62	22	11
[4,]	521.6749	3	174362565	1929.97	1971.22	57	6

```
[5,] 534.3278
                    2 82024006 2068.95 2099.10
                                                      35
                                                               12
 [6,] 535.3383
                    1 242848614 2099.10 2150.15
                                                      70
                                                                9
 [7,] 546.8268
                    2 43092586 2112.83 2137.57
                                                                2
                                                      37
 [8,] 549.3673
                    1 10241899 1882.23 1925.06
                                                      56
                                                                8
                    2 358822314 2090.02 2155.51
 [9,] 584.8515
                                                      91
                                                               10
[10,] 585.3650
                    2 17016750 2132.31 2155.51
                                                      31
                                                                5
[11,] 585.3691
                    2 13830263 2175.63 2193.95
                                                                3
                                                      25
[12,] 597.3784
                    2 10873799 1882.96 1906.53
                                                      35
                                                                1
R> rtlist <- lapply(data$scan, function(x)</pre>
                  as.numeric(sub("([^0-9]*)([^0-9]*)", "\\2", x$scanAttr)))
R> rt <- unlist(rtlist)</pre>
R> nscans <- length(rt)</pre>
R> npoints <- length(data$scan[[1]]$mass)</pre>
R> Y <- matrix(unlist(lapply(data$scan, function(x) x$peaks)),</pre>
             nrow = nscans,
             ncol = npoints,
             byrow = TRUE)
R> contour(rt, data$scan[[1]]$mass, Y, xlab = "t", ylab = "mz",
         levels = 10^{(seq(from = 5, to = 6.75, by = 0.25))},
         drawlabels = FALSE)
R> for(i in 1:nrow(boxes))
   lines(c(boxes[i,"rt_begin"], boxes[i,"rt_end"]), rep(boxes[i,"loc"], 2), col = "red")
R>
R>
```



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